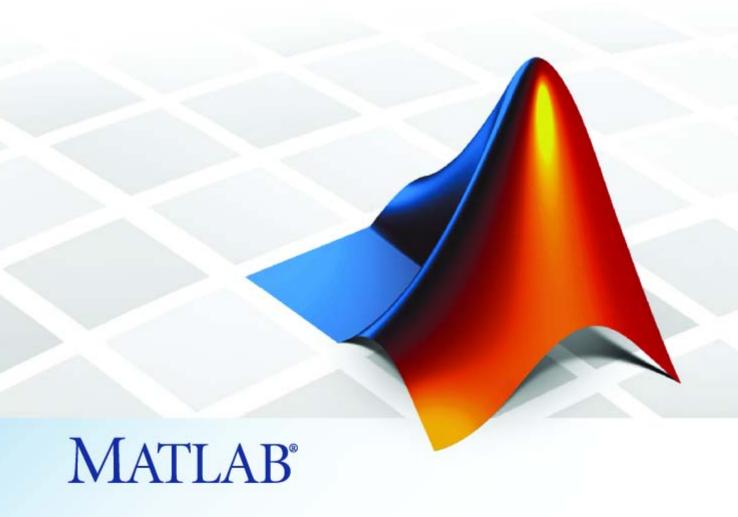
Genetic Algorithm and Direct Search Toolbox 2 User's Guide





How to Contact The MathWorks



www.mathworks.com

comp.soft-sys.matlab Newsgroup

www.mathworks.com/contact_TS.html Technical Support

(a)

suggest@mathworks.com bugs@mathworks.com

doc@mathworks.com

service@mathworks.com
info@mathworks.com

Product enhancement suggestions

Bug reports

Web

Documentation error reports

Order status, license renewals, passcodes Sales, pricing, and general information



508-647-7000 (Phone)



508-647-7001 (Fax)



The MathWorks, Inc. 3 Apple Hill Drive Natick, MA 01760-2098

For contact information about worldwide offices, see the MathWorks Web site.

Genetic Algorithm and Direct Search Toolbox User's Guide

© COPYRIGHT 2004–2007 by The MathWorks, Inc.

The software described in this document is furnished under a license agreement. The software may be used or copied only under the terms of the license agreement. No part of this manual may be photocopied or reproduced in any form without prior written consent from The MathWorks, Inc.

FEDERAL ACQUISITION: This provision applies to all acquisitions of the Program and Documentation by, for, or through the federal government of the United States. By accepting delivery of the Program or Documentation, the government hereby agrees that this software or documentation qualifies as commercial computer software or commercial computer software documentation as such terms are used or defined in FAR 12.212, DFARS Part 227.72, and DFARS 252.227-7014. Accordingly, the terms and conditions of this Agreement and only those rights specified in this Agreement, shall pertain to and govern the use, modification, reproduction, release, performance, display, and disclosure of the Program and Documentation by the federal government (or other entity acquiring for or through the federal government) and shall supersede any conflicting contractual terms or conditions. If this License fails to meet the government's needs or is inconsistent in any respect with federal procurement law, the government agrees to return the Program and Documentation, unused, to The MathWorks, Inc.

Trademarks

MATLAB, Simulink, Stateflow, Handle Graphics, Real-Time Workshop, SimBiology, SimHydraulics, SimEvents, and xPC TargetBox are registered trademarks and The MathWorks, the L-shaped membrane logo, Embedded MATLAB, and PolySpace are trademarks of The MathWorks. Inc.

Other product or brand names are trademarks or registered trademarks of their respective holders.

Patents

The MathWorks products are protected by one or more U.S. patents. Please see www.mathworks.com/patents for more information.

Revision History

January 2004	Online only	New for Version 1.0 (Release 13SP1+)
June 2004	First printing	Revised for Version 1.0.1 (Release 14)
October 2004	Online only	Revised for Version 1.0.2 (Release 14SP1)
March 2005	Online only	Revised for Version 1.0.3 (Release 14SP2)
September 2005	Second printing	Revised for Version 2.0 (Release 14SP3)
March 2006	Online only	Revised for Version 2.0.1 (Release 2006a)
September 2006	Online only	Revised for Version 2.0.2 (Release 2006b)
March 2007	Online only	Revised for Version 2.1 (Release 2007a)
September 2007	Third printing	Revised for Version 2.2 (Release 2007b)

Acknowledgment

The MathWorksTM would like to acknowledge Mark A. Abramson for his contributions to the Genetic Algorithm and Direct Search Toolbox. He researched and helped with the development of the linearly constrained pattern search algorithm.

Dr. Mark A. Abramson is Associate Professor in the Department of Mathematics and Statistics, Air Force Institute of Technology, Wright-Patterson AFB, Ohio. Dr. Abramson is actively engaged in research for pattern search methods. He has published over 26 technical papers and has worked on NOMAD, a software package for pattern search.



2-6

2-6

2-7

2-8

2-10

2-10

2-11

2-11

2-12

~ cure: 130	lbox
What Is Genetic Algorithm and Direct Search Toolbox?	1-2
Writing M-Files for Functions You Want to Optimize	1-3
Computing Objective Functions	1-3
Example — Writing an M-File	1-3 1-4
Getting Started with Direct Sea	_
Getting Started with Direct Sea	arch
Getting Started with Direct Sea	arch
What Is Direct Search?	
	2-2
What Is Direct Search?	2-2 2-3 2-3

Example: Finding the Minimum of a Function Using the GPS Algorithm

Objective Function

Finding the Minimum of the Function

Plotting the Objective Function Values and Mesh Sizes ...

Patterns

Meshes

Polling

Expanding and Contracting

Pattern Search Terminology

Introducing Genetic Algorithm and Direct

How Pattern Search Works	
Context	
Successful Polls	
An Unsuccessful Poll	
Displaying the Results at Each Iteration	
More Iterations	
Stopping Conditions for the Pattern Search	2 -1
Description of the Nonlinear Constraint Solver	2-2
Getting Started with the Genetic A	lgorith
What Is the Genetic Algorithm?	3
Using the Genetic Algorithm, Command Line or	
Tool	
Calling the Function ga at the Command Line	3
Using the Genetic Algorithm Tool	
Example: Rastrigin's Function	3
Rastrigin's Function	
Finding the Minimum of Rastrigin's Function	
Finding the Minimum from the Command Line	
Displaying Plots	3-
Some Genetic Algorithm Terminology	
Fitness Functions	
Individuals	
Populations and Generations	
Diversity	
Fitness Values and Best Fitness Values	
Parents and Children	3-
How the Genetic Algorithm Works	
Outline of the Algorithm	
Initial Population	
Creating the Next Generation	3-

	Plots of Later Generations	3-23 3-23
	Description of the Nonlinear Constraint Solver	3-26
4	Getting Started with Simulated Annealing Threshold Accepta	and nce
-	What Are Simulated Annealing and Threshold Acceptance?	4-2
	Calling the Simulated Annealing and Threshold Acceptance Solvers	4-3
	Example: Minimizing De Jong's Fifth Function	4-4
	Some Simulated Annealing and Threshold Acceptance	4.0
	Terminology Objective Function	4-6 4-6
	Temperature	4-6
	Annealing Schedule	4-6
	Reannealing	4-6
	How Simulated Annealing and Threshold Acceptance	
	Work	4-8
	Outline of the Algorithm	4-8 4-9
	Using Direct Sea	ırch
5		
	Overview of the Pattern Search Tool (GUI)	$\begin{array}{c} 5\text{-}2 \\ 5\text{-}2 \end{array}$
	Opening the Pattern Search Tool	5-2 5-3

alling patternsearch with the Default Options etting Options for patternsearch at the Command Line sing Options and Problems from the Pattern Search Tool ern Search Examples: Setting Options oll Method omplete Poll sing a Search Method esh Expansion and Contraction esh Accelerator sing Cache etting Tolerances for the Solver
alling patternsearch with the Default Options etting Options for patternsearch at the Command Line sing Options and Problems from the Pattern Search Tool ern Search Examples: Setting Options oll Method omplete Poll sing a Search Method esh Expansion and Contraction esh Accelerator sing Cache etting Tolerances for the Solver onstrained Minimization Using patternsearch
alling patternsearch with the Default Optionsetting Options for patternsearch at the Command Line . sing Options and Problems from the Pattern Search
alling patternsearch with the Default Options etting Options for patternsearch at the Command Line sing Options and Problems from the Pattern Search Tool ern Search Examples: Setting Options oll Method omplete Poll sing a Search Method esh Expansion and Contraction esh Accelerator sing Cache
alling patternsearch with the Default Options
alling patternsearch with the Default Options
alling patternsearch with the Default Options
alling patternsearch with the Default Options etting Options for patternsearch at the Command Line . sing Options and Problems from the Pattern Search Tool
alling patternsearch with the Default Options etting Options for patternsearch at the Command Line . sing Options and Problems from the Pattern Search Tool
alling patternsearch with the Default Optionsetting Options for patternsearch at the Command Line .sing Options and Problems from the Pattern Search
alling patternsearch with the Default Optionsetting Options for patternsearch at the Command Line .
ine
ine
orming a Pattern Search from the Command
Comming a Dattorn Secret from the Command
enerating an M-File
apporting and Exporting Options and Problems
etting Options in the Pattern Search Tool
isplaying Plots
ausing and Stopping the Algorithm

Defining an Unconstrained Problem in the Genetic	
Algorithm Tool	
Running the Genetic Algorithm	
Pausing and Stopping the Algorithm	(
Displaying Plots	(
Example — Creating a Custom Plot Function	
Reproducing Your Results	6-
Setting Options in the Genetic Algorithm Tool	6-
Importing and Exporting Options and Problems	6-
Example — Resuming the Genetic Algorithm from the	
Final Population	6-
Generating an M-File	6-
Using the Genetic Algorithm from the Command	
Line	6-
Running ga with the Default Options	6-
Setting Options for ga at the Command Line	6-
Using Options and Problems from the Genetic Algorithm	
Tool	6
Reproducing Your Results	6
Resuming ga from the Final Population of a Previous	
Run	6
Running ga from an M-File	6
Genetic Algorithm Examples	6-
Improving Your Results	6-
Population Diversity	6-
Fitness Scaling	6-
Selection	6
Reproduction Options	6
Mutation and Crossover	6
Setting the Amount of Mutation	6
Setting the Crossover Fraction	6
Comparing Results for Varying Crossover Fractions	6
Global vs. Local Minima	6
Using a Hybrid Function	6
Setting the Maximum Number of Generations	6
Vectorizing the Fitness Function	6
Constrained Minimization Using ga	6
Constrained Minimization Oshig ga	0.
Parameterizing Functions Called by ga	6-
Using Additional Parameters	G.

With ga Parameterizing a Function Using a Nested Function with ga Using the Simulated Annealing and Thresh Acceptance Algorit Using the Simulated Annealing and Threshold Acceptance Algorithms from the Command Line Running simulannealbnd and threshacceptbnd with the Default Options Setting Options for simulannealbnd and threshacceptbnd at the Command Line Reproducing Your Results Imulated Annealing and Threshold Acceptance Examples Options Refere Pattern Search Options Pattern Search Tool vs. Command Line Plot Options Poll Options Search Options Mesh Options Algorithm Settings Cache Options Stopping Criteria Output Function Options Display to Command Window Options Vectorize Option		rizing Functions Using	
Using the Simulated Annealing and Thresh Acceptance Algorit Using the Simulated Annealing and Threshold Acceptance Algorithms from the Command Line Running simulannealbnd and threshacceptbnd with the Default Options Setting Options for simulannealbnd and threshacceptbnd at the Command Line Reproducing Your Results Simulated Annealing and Threshold Acceptance Examples Options Refere Pattern Search Options Pattern Search Tool vs. Command Line Plot Options Poll Options Search Options Mesh Options Algorithm Settings Cache Options Stopping Criteria Output Function Options Display to Command Window Options Vectorize Option			
Acceptance Algorit Using the Simulated Annealing and Threshold Acceptance Algorithms from the Command Line Running simulannealbnd and threshacceptbnd with the Default Options Setting Options for simulannealbnd and threshacceptbnd at the Command Line Reproducing Your Results Cimulated Annealing and Threshold Acceptance Examples Options Refere Pattern Search Options Pattern Search Tool vs. Command Line Plot Options Search Options Mesh Options Mesh Options Algorithm Settings Cache Options Stopping Criteria Output Function Options Display to Command Window Options Vectorize Option		-	
Acceptance Algorithms from the Command Line Running simulannealbnd and threshacceptbnd with the Default Options Setting Options for simulannealbnd and threshacceptbnd at the Command Line Reproducing Your Results Simulated Annealing and Threshold Acceptance Examples Options Refere Pattern Search Options Pattern Search Tool vs. Command Line Plot Options Poll Options Search Options Mesh Options Algorithm Settings Cache Options Stopping Criteria Output Function Options Display to Command Window Options Vectorize Option	Using th	ne Simulated An	nealing and Thres Acceptance Algorit
Setting Options for simulannealbnd and threshacceptbnd at the Command Line Reproducing Your Results Simulated Annealing and Threshold Acceptance Examples Options Refere Pattern Search Options Pattern Search Tool vs. Command Line Plot Options Poll Options Search Options Mesh Options Algorithm Settings Cache Options Stopping Criteria Output Function Options Display to Command Window Options Vectorize Option	Acceptan Running s	ce Algorithms from the simulanneal bnd and the	the Command Line reshacceptbnd with the
Reproducing Your Results Simulated Annealing and Threshold Acceptance Examples Options Refere Pattern Search Options Pattern Search Tool vs. Command Line Plot Options Poll Options Search Options Mesh Options Mesh Options Algorithm Settings Cache Options Stopping Criteria Output Function Options Display to Command Window Options Vectorize Option			
Cattern Search Options Pattern Search Tool vs. Command Line Plot Options Poll Options Pearch Options Search Options Search Options Search Options Search Options Mesh Options Algorithm Settings Cache Options Stopping Criteria Output Function Options Display to Command Window Options Vectorize Option			
Pattern Search Options Pattern Search Tool vs. Command Line Plot Options Poll Options Search Options Mesh Options Algorithm Settings Cache Options Stopping Criteria Output Function Options Display to Command Window Options Vectorize Option	Reproduci	ng Your Results	• • • • • • • • • • • • • • • • • • • •
Pattern Search Options Pattern Search Tool vs. Command Line Plot Options Poll Options Search Options Mesh Options Algorithm Settings Cache Options Stopping Criteria Output Function Options Display to Command Window Options Vectorize Option		_	-
Poll Options Search Options Mesh Options Algorithm Settings Cache Options Stopping Criteria Output Function Options Display to Command Window Options Vectorize Option		_	
Mesh Options Algorithm Settings Cache Options Stopping Criteria Output Function Options Display to Command Window Options Vectorize Option	Example Pattern Sea Pattern Se	arch Options	Options Refer
Algorithm Settings Cache Options Stopping Criteria Output Function Options Display to Command Window Options Vectorize Option	Pattern Sea Pattern Sea Pattern So Plot Optio Poll Optio	arch Options earch Tool vs. Comman ns	Options Refer
Stopping Criteria	Pattern Sea Pattern Sea Pattern So Polt Optio Poll Optio Search Op	arch Options earch Tool vs. Comman ns ns	Options Refer
Output Function Options	Pattern Sea Pattern Sea Pattern So Polt Optio Poll Optio Search Op Mesh Opt	arch Options earch Tool vs. Comman ns ns otions	Options Refer
Display to Command Window Options	Pattern Sea Pattern Sea Pattern So Plot Optio Poll Optio Search Options Search Option Algorithm Cache Options	arch Options earch Tool vs. Comman ns ns otions Settings	Options Refer
	Pattern Sea Pattern Sea Pattern Sea Plot Optio Poll Optio Search Option Mesh Option Algorithm Cache Option Stopping Option	arch Options earch Tool vs. Comman ns ns dions Settings cions Criteria	Options Refer
Options Table for Pattern Search Algorithms	Pattern Sea Pattern Sea Pattern Sea Plot Optio Poll Optio Search Op Mesh Opt Algorithm Cache Opt Stopping O Output Fu Display to	arch Options earch Tool vs. Comman ns ns otions cons Settings cons Criteria unction Options Command Window Op	Options Reference
	Pattern Sea Pattern Sea Pattern Sea Plot Option Poll Option Search Option Mesh Option Algorithm Cache Option Stopping Output Fu Display to Vectorize	arch Options earch Tool vs. Comman ns otions ions Criteria cunction Options Command Window Op Option	Options Refer

8 1	8-23
8	8-23
1	8-24
Population Options	8-27
Fitness Scaling Options	8-29
	8-31
Reproduction Options	8-32
Mutation Options	8-33
	8-35
	8-39
	8-39
	8-40
	8-40
	8-41
11 0	8-41
	8-4 3
1 1	8-44
vectorize Option	0-44
saoptimset At The Command Line Plot Options Temperature Options Algorithm Settings Hybrid Function Options Stopping Criteria Options Output Function Options	8-45 8-45 8-47 8-48 8-49 8-49 8-50
Functions — By Catego	ory
Genetic Algorithm	9-2
Direct Search	9-2
Simulated Annealing and Threshold Acceptance Algorithms	9-3

${\bf Functions-Alphabetical\ List}$

10

Λ	Examp	oles
	Pattern Search	A-2
	Genetic Algorithm	A-2
	Simulated Annealing and Threshold Acceptance Algorithms	A-2
Γ	In	<u>dex</u>

Introducing Genetic Algorithm and Direct Search Toolbox

What Is Genetic Algorithm and Direct Search Toolbox? (p. 1-2)

Writing M-Files for Functions You Want to Optimize (p. 1-3)

Introduces the toolbox and its features.

Explains how to write M-files that compute the functions you want to optimize.

What Is Genetic Algorithm and Direct Search Toolbox?

Genetic Algorithm and Direct Search Toolbox is a collection of functions that extend the capabilities of Optimization Toolbox and the MATLAB® numeric computing environment. Genetic Algorithm and Direct Search Toolbox includes routines for solving optimization problems using

- Direct search
- Genetic algorithm
- Simulated annealing

These algorithms enable you to solve a variety of optimization problems that lie outside the scope of Optimization Toolbox.

All the toolbox functions are MATLAB M-files made up of MATLAB statements that implement specialized optimization algorithms. You can view the MATLAB code for these functions using the statement

type function_name

You can extend the capabilities of Genetic Algorithm and Direct Search Toolbox by writing your own M-files, or by using the toolbox in combination with other toolboxes, or with MATLAB or Simulink[®].

Writing M-Files for Functions You Want to Optimize

In this section...

"Computing Objective Functions" on page 1-3

"Example — Writing an M-File" on page 1-3

"Maximizing vs. Minimizing" on page 1-4

Computing Objective Functions

To use Genetic Algorithm and Direct Search Toolbox, you must first write an M-file (or else an anonymous function) that computes the function you want to optimize. The M-file should accept a vector, whose length is the number of independent variables for the objective function, and return a scalar. This section explains how to write the M-file.

Example – Writing an M-File

The following example shows how to write an M-file for the function you want to optimize. Suppose that you want to minimize the function

$$f(x_1, x_2) = x_1^2 - 2x_1x_2 + 6x_1 + x_2^2 - 6x_2$$

The M-file that computes this function must accept a vector x of length 2, corresponding to the variables x_1 and x_2 , and return a scalar equal to the value of the function at x. To write the M-file, do the following steps:

- 1 Select **New** from the MATLAB **File** menu.
- **2** Select **M-File**. This opens a new M-file in the editor.
- **3** In the M-file, enter the following two lines of code:

function
$$z = my_fun(x)$$

 $z = x(1)^2 - 2*x(1)*x(2) + 6*x(1) + x(2)^2 - 6*x(2);$

4 Save the M-file in a directory on the MATLAB path.

To check that the M-file returns the correct value, enter

Maximizing vs. Minimizing

The optimization functions in Genetic Algorithm and Direct Search Toolbox minimize the objective or fitness function. That is, they solve problems of the form

$$\min_{x} \inf f(x)$$

If you want to maximize f(x), you can do so by minimizing -f(x), because the point at which the minimum of -f(x) occurs is the same as the point at which the maximum of f(x) occurs.

For example, suppose you want to maximize the function

$$f(x_1, x_2) = x_1^2 - 2x_1x_2 + 6x_1 + x_2^2 - 6x_2$$

described in the preceding section. In this case, you should write your M-file to compute

$$-f(x_1, x_2) = -x_1^2 + 2x_1x_2 - 6x_1 - x_2^2 + 6x_2$$

and minimize this function.

Getting Started with Direct Search

What Is Direct Search? (p. 2-2) Introduces direct search and pattern

Performing a Pattern Search (p. 2-3) Explains the main function in the

toolbox for performing pattern

search.

Example: Finding the Minimum of a

Function Using the GPS Algorithm (p. 2-6)

Pattern Search Terminology (p. 2-10)

How Pattern Search Works (p. 2-13)

Description of the Nonlinear Constraint Solver (p. 2-22)

search.

Provides an example of solving an optimization problem using pattern

search.

Explains some basic pattern search

terminology.

Provides an overview of direct search

algorithms.

Explains the Augmented Lagrangian

Pattern Search (ALPS).

What Is Direct Search?

Direct search is a method for solving optimization problems that does not require any information about the gradient of the objective function. Unlike more traditional optimization methods that use information about the gradient or higher derivatives to search for an optimal point, a direct search algorithm searches a set of points around the current point, looking for one where the value of the objective function is lower than the value at the current point. You can use direct search to solve problems for which the objective function is not differentiable, stochastic, or even continuous.

The Genetic Algorithm and Direct Search Toolbox implements two direct search algorithms called the generalized pattern search (GPS) algorithm and the mesh adaptive search (MADS) algorithm. Both are *pattern search* algorithms that compute a sequence of points that get closer and closer to an optimal point. At each step, the algorithm searches a set of points, called a *mesh*, around the *current point*—the point computed at the previous step of the algorithm. The mesh is formed by adding the current point to a scalar multiple of a set of vectors called a *pattern*. If the pattern search algorithm finds a point in the mesh that improves the objective function at the current point, the new point becomes the current point at the next step of the algorithm.

The MADS algorithm is a modification of the GPS algorithm. The algorithms differ in how the set of points forming the mesh is computed. The GPS algorithm uses fixed direction vectors, whereas the MADS algorithm uses a random selection of vectors to define the mesh.

Performing a Pattern Search

In this section...

"Calling patternsearch at the Command Line" on page 2-3

"Using the Pattern Search Tool" on page 2-3

Calling patternsearch at the Command Line

To perform a pattern search on an unconstrained problem at the command line, call the function patternsearch with the syntax

```
[x fval] = patternsearch(@objfun, x0)
```

where

- @objfun is a handle to the objective function.
- x0 is the starting point for the pattern search.

The results are:

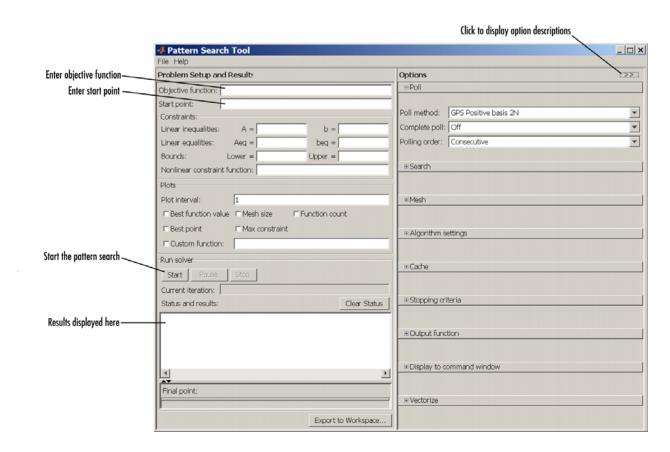
- x Point at which the final value is attained
- fval Final value of the objective function

"Performing a Pattern Search from the Command Line" on page 5-19 explains in detail how to use the patternsearch function.

Using the Pattern Search Tool

To open the Pattern Search Tool, enter

psearchtool



To use the Pattern Search Tool, first enter the following information:

- **Objective function** The objective function you want to minimize. Enter the objective function in the form @objfun, where objfun.m is an M-file that computes the objective function. The @ sign creates a function handle to objfun.
- **Start point** The initial point at which the algorithm starts the optimization.

In the **Constraints** pane, enter linear constraints, bounds, or a nonlinear constraint function for the problem. If the problem is unconstrained, leave these fields blank.

Then, click **Start**. The tool displays the results of the optimization in the **Status and results** pane.

In the **Options** pane, set the options for the pattern search. To view the options in a category, click the + sign next to it.

"Finding the Minimum of the Function" on page 2-7 gives an example of using the Pattern Search Tool.

"Overview of the Pattern Search Tool (GUI)" on page 5-2 provides a detailed description of the Pattern Search Tool.

Example: Finding the Minimum of a Function Using the GPS Algorithm

In this section...

"Objective Function" on page 2-6

"Finding the Minimum of the Function" on page 2-7

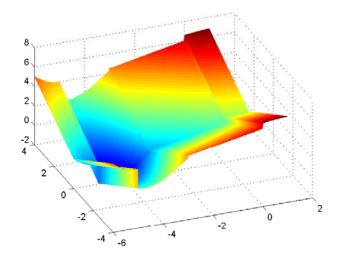
"Plotting the Objective Function Values and Mesh Sizes" on page 2-8

Objective Function

This example uses the objective function, ps_example, which is included with the Genetic Algorithm and Direct Search Toolbox software. View the code for the function by entering

type ps_example

The following figure shows a plot of the function.



Finding the Minimum of the Function

To find the minimum of ps example, do the following steps:

1 Enter

psearchtool

to open the Pattern Search Tool.

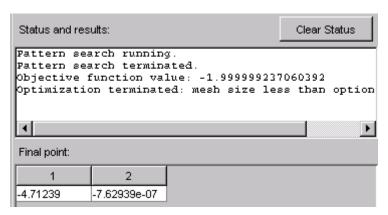
- 2 In the **Objective function** field of the Pattern Search Tool, enter @ps example.
- **3** In the **Start point** field, type [2.1 1.7].



Leave the fields in the **Constraints** pane blank because the problem is unconstrained.

4 Click **Start** to run the pattern search.

The **Status and results** pane displays the results of the pattern search.

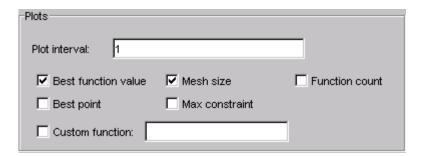


The reason the optimization terminated is that the mesh size became smaller than the acceptable tolerance value for the mesh size, defined by the **Mesh tolerance** parameter in the **Stopping criteria** pane. The minimum function value is approximately –2. The **Final point** pane displays the point at which the minimum occurs.

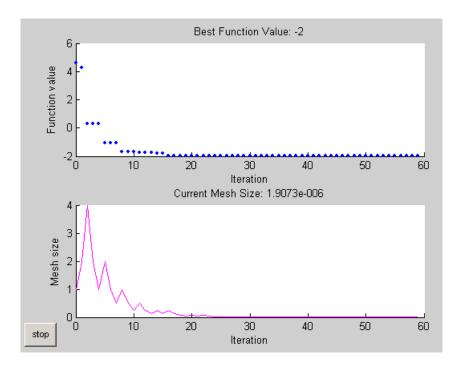
Plotting the Objective Function Values and Mesh Sizes

To see the performance of the pattern search, display plots of the best function value and mesh size at each iteration. First, select the following check boxes in the **Plots** pane:

- Best function value
- Mesh size



Then click **Start** to run the pattern search. This displays the following plots.



The upper plot shows the objective function value of the best point at each iteration. Typically, the objective function values improve rapidly at the early iterations and then level off as they approach the optimal value.

The lower plot shows the mesh size at each iteration. The mesh size increases after each successful iteration and decreases after each unsuccessful one, explained in "How Pattern Search Works" on page 2-13.

Pattern Search Terminology

In this section...

"Patterns" on page 2-10

"Meshes" on page 2-11

"Polling" on page 2-11

"Expanding and Contracting" on page 2-12

Patterns

A pattern is a set of vectors $\{v_i\}$ that the pattern search algorithm uses to determine which points to search at each iteration. The set $\{v_i\}$ is defined by the number of independent variables in the objective function, N, and the positive basis set. Two commonly used positive basis sets in pattern search algorithms are the maximal basis, with 2N vectors, and the minimal basis, with N+1 vectors.

With GPS, the collection of vectors that form the pattern are fixed-direction vectors. For example, if there are three independent variables in the optimization problem, the default for a 2N positive basis consists of the following pattern vectors:

$$v_1 = [1 \quad 0 \quad 0]$$
 $v_2 = [0 \quad 1 \quad 0]$ $v_3 = [0 \quad 0 \quad 1]$ $v_4 = [-1 \quad 0 \quad 0]$ $v_5 = [0 \quad -1 \quad 0]$ $v_6 = [0 \quad 0 \quad -1]$

An N+1 positive basis consists of the following default pattern vectors.

With MADS, the collection of vectors that form the pattern are randomly selected by the algorithm. Depending on the poll method choice, the number of vectors selected will be 2N or N+1. As in GPS, 2N vectors consist of N vectors and their N negatives, while N+1 vectors consist of N vectors and one that is the negative of the sum of the others.

Meshes

At each step, the pattern search algorithm searches a set of points, called a *mesh*, for a point that improves the objective function. The GPS and MADS algorithms form the mesh by

- **1** Generating a set of vectors $\{d_i\}$ by multiplying each pattern vector v_i by a scalar Δ^m . Δ^m is called the *mesh size*.
- **2** Adding the $\{d_i\}$ to the *current point*—the point with the best objective function value found at the previous step.

For example, using the GPS algorithm. suppose that:

- The current point is [1.6 3.4].
- The pattern consists of the vectors

$$\begin{aligned} v_1 &= \begin{bmatrix} 1 & 0 \end{bmatrix} \\ v_2 &= \begin{bmatrix} 0 & 1 \end{bmatrix} \\ v_3 &= \begin{bmatrix} -1 & 0 \end{bmatrix} \\ v_4 &= \begin{bmatrix} 0 & -1 \end{bmatrix} \end{aligned}$$

• The current mesh size Δ^m is 4.

The algorithm multiplies the pattern vectors by 4 and adds them to the current point to obtain the following mesh.

```
[1.6 \ 3.4] + 4*[1 \ 0] = [5.6 \ 3.4]

[1.6 \ 3.4] + 4*[0 \ 1] = [1.6 \ 7.4]

[1.6 \ 3.4] + 4*[-1 \ 0] = [-2.4 \ 3.4]

[1.6 \ 3.4] + 4*[0 \ -1] = [1.6 \ -0.6]
```

The pattern vector that produces a mesh point is called its *direction*.

Polling

At each step, the algorithm polls the points in the current mesh by computing their objective function values. When the **Complete poll** option has the (default) setting Off, the algorithm stops polling the mesh points as soon as it

finds a point whose objective function value is less than that of the current point. If this occurs, the poll is called *successful* and the point it finds becomes the current point at the next iteration.

The algorithm only computes the mesh points and their objective function values up to the point at which it stops the poll. If the algorithm fails to find a point that improves the objective function, the poll is called *unsuccessful* and the current point stays the same at the next iteration.

When the **Complete poll** option has the setting On, the algorithm computes the objective function values at all mesh points. The algorithm then compares the mesh point with the smallest objective function value to the current point. If that mesh point has a smaller value than the current point, the poll is successful.

Expanding and Contracting

After polling, the algorithm changes the value of the mesh size Δ^m . The default is to multiply Δ^m by 2 after a successful poll, and by 0.5 after an unsuccessful poll.

How Pattern Search Works

In this section...

"Context" on page 2-13

"Successful Polls" on page 2-13

"An Unsuccessful Poll" on page 2-16

"Displaying the Results at Each Iteration" on page 2-17

"More Iterations" on page 2-18

"Stopping Conditions for the Pattern Search" on page 2-19

Context

The pattern search algorithms find a sequence of points, x0, x1, x2, ..., that approaches an optimal point. The value of the objective function either decreases or remains the same from each point in the sequence to the next. This section explains how pattern search works for the function described in "Example: Finding the Minimum of a Function Using the GPS Algorithm" on page 2-6.

To simplify the explanation, this section describes how the generalized pattern search (GPS) works using a maximal positive basis of 2N, with **Scale** set to 0ff in **Mesh** options.

Successful Polls

The pattern search begins at the initial point x0 that you provide. In this example, $x0 = [2.1 \ 1.7]$.

Iteration 1

At the first iteration, the mesh size is 1 and the GPS algorithm adds the pattern vectors to the initial point $x0 = [2.1 \ 1.7]$ to compute the following mesh points:

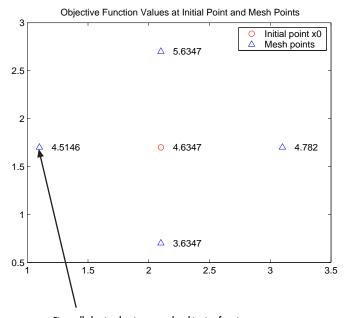
```
\begin{bmatrix} 1 & 0 \end{bmatrix} + x0 = \begin{bmatrix} 3.1 & 1.7 \end{bmatrix}

\begin{bmatrix} 0 & 1 \end{bmatrix} + x0 = \begin{bmatrix} 2.1 & 2.7 \end{bmatrix}

\begin{bmatrix} -1 & 0 \end{bmatrix} + x0 = \begin{bmatrix} 1.1 & 1.7 \end{bmatrix}
```

$$[0 -1] + x0 = [2.1 0.7]$$

The algorithm computes the objective function at the mesh points in the order shown above. The following figure shows the value of ps_example at the initial point and mesh points.



First polled point that improves the objective function

The algorithm polls the mesh points by computing their objective function values until it finds one whose value is smaller than 4.6347, the value at x0. In this case, the first such point it finds is [1.1 1.7], at which the value of the objective function is 4.5146, so the poll at iteration 1 is *successful*. The algorithm sets the next point in the sequence equal to

$$x1 = [1.1 \ 1.7]$$

Note By default, the GPS pattern search algorithm stops the current iteration as soon as it finds a mesh point whose fitness value is smaller than that of the current point. Consequently, the algorithm might not poll all the mesh points. You can make the algorithm poll all the mesh points by setting **Complete poll** to On.

Iteration 2

After a successful poll, the algorithm multiplies the current mesh size by 2, the default value of **Expansion factor** in the **Mesh** options pane. Because the initial mesh size is 1, at the second iteration the mesh size is 2. The mesh at iteration 2 contains the following points:

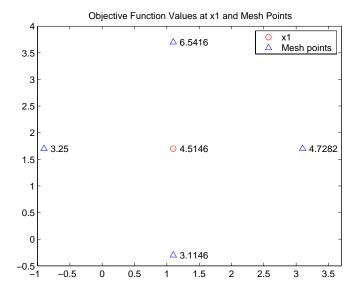
```
2*[1 \ 0] + x1 = [3.1 \ 1.7]

2*[0 \ 1] + x1 = [1.1 \ 3.7]

2*[-1 \ 0] + x1 = [-0.9 \ 1.7]

2*[0 \ -1] + x1 = [1.1 \ -0.3]
```

The following figure shows the point x1 and the mesh points, together with the corresponding values of ps_example.



The algorithm polls the mesh points until it finds one whose value is smaller than 4.5146, the value at x1. The first such point it finds is [-0.9 1.7], at which the value of the objective function is 3.25, so the poll at iteration 2 is again successful. The algorithm sets the second point in the sequence equal to

$$x2 = [-0.9 \ 1.7]$$

Because the poll is successful, the algorithm multiplies the current mesh size by 2 to get a mesh size of 4 at the third iteration.

An Unsuccessful Poll

By the fourth iteration, the current point is

$$x3 = [-4.9 \ 1.7]$$

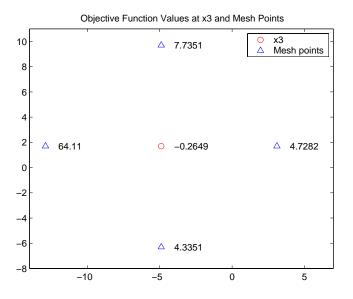
and the mesh size is 8, so the mesh consists of the points

$$8*[1 \ 0] + x3 = [3.1 \ 1.7]$$

 $8*[0 \ 1] + x3 = [-4.9 \ 9.7]$
 $8*[-1 \ 0] + x3 = [-12.9 \ 1.7]$

$$8*[0 -1] + x3 = [-4.9 -1.3]$$

The following figure shows the mesh points and their objective function values.



At this iteration, none of the mesh points has a smaller objective function value than the value at x3, so the poll is *unsuccessful*. In this case, the algorithm does not change the current point at the next iteration. That is,

$$x4 = x3;$$

At the next iteration, the algorithm multiplies the current mesh size by 0.5, the default value of **Contraction factor** in the **Mesh** options pane, so that the mesh size at the next iteration is 4. The algorithm then polls with a smaller mesh size.

Displaying the Results at Each Iteration

You can display the results of the pattern search at each iteration by setting **Level of display** to Iterative in the **Display to command window**

options. This enables you to evaluate the progress of the pattern search and to make changes to options if necessary.

With this setting, the pattern search displays information about each iteration at the command line. The first four lines of the display are

Iter	f-count	f(x)	MeshSize	Method
0	1	4.63474	1	
1	4	4.51464	2	Successful Poll
2	7	3.25	4	Successful Poll
3	10	-0.264905	8	Successful Poll

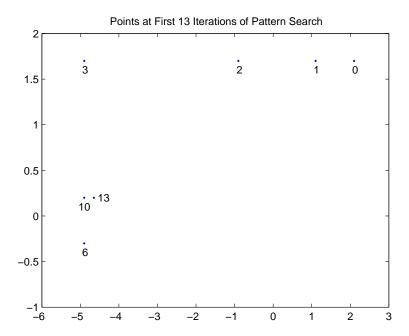
The entry Successful Poll below Method indicates that the current iteration was successful. For example, the poll at iteration 2 is successful. As a result, the objective function value of the point computed at iteration 2, displayed below f(x), is less than the value at iteration 1.

At iteration 3, the entry Refine Mesh below Method tells you that the poll is unsuccessful. As a result, the function value at iteration 4 remains unchanged from iteration 3.

By default, the pattern search doubles the mesh size after each successful poll and halves it after each unsuccessful poll.

More Iterations

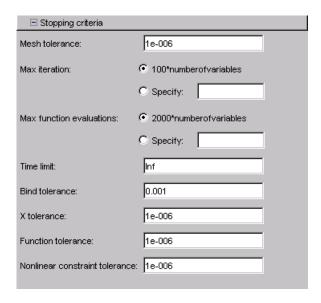
The pattern search performs 88 iterations before stopping. The following plot shows the points in the sequence computed in the first 13 iterations of the pattern search.



The numbers below the points indicate the first iteration at which the algorithm finds the point. The plot only shows iteration numbers corresponding to successful polls, because the best point doesn't change after an unsuccessful poll. For example, the best point at iterations 4 and 5 is the same as at iteration 3.

Stopping Conditions for the Pattern Search

The criteria for stopping the pattern search algorithm are listed in the **Stopping criteria** section of the Pattern Search Tool.



The algorithm stops when any of the following conditions occurs:

- The mesh size is less than **Mesh tolerance**.
- The number of iterations performed by the algorithm reaches the value of Max iteration.
- The total number of objective function evaluations performed by the algorithm reaches the value of **Max function evaluations**.
- The time, in seconds, the algorithm runs until it reaches the value of **Time** limit.
- The distance between the point found in two consecutive iterations and the mesh size are both less than **X tolerance**.
- The change in the objective function in two consecutive iterations and the mesh size are both less than Function tolerance.

Neither the Bind tolerance nor the Nonlinear constraint tolerance are used as stopping criterion. The **Bind tolerance** option identifies active constraints for constrained problems, and the Nonlinear constraint **tolerance** determines the feasibility with respect to nonlinear constraints.

The MADS algorithm uses the relationship between the mesh size, Δ^m , and an additional parameter, called the poll parameter, Δ^p , to determine the stopping criteria. For positive basis N+1, the poll parameter is $N\sqrt{\Delta^m}$, and for positive basis 2N, the poll parameter is $\sqrt{\Delta^m}$. The relationship for MADS stopping criteria is $\Delta^m \leq \mathbf{Mesh}$ tolerance.

Description of the Nonlinear Constraint Solver

The pattern search algorithm uses the Augmented Lagrangian Pattern Search (ALPS) algorithm to solve nonlinear constraint problems. The optimization problem solved by the ALPS algorithm is

$$\min_{x} f(x)$$

such that

$$\begin{split} &C_i(x) \leq 0, i = 1...m \\ &C_i(x) = 0, \, i = m+1...mt \\ &Ax \leq b \\ &A_{eq}x = beq \\ &LB \leq x \leq UB \end{split}$$

where C(x) represents the nonlinear inequality and equality constraints, m is the number of nonlinear inequality constraints, and mt is the total number of nonlinear constraints.

The ALPS algorithm attempts to solve a nonlinear optimization problem with nonlinear constraints, linear constraints, and bounds. In this approach, bounds and linear constraints are handled separately from nonlinear constraints. A subproblem is formulated by combining the objective function and nonlinear constraint function using the Lagrangian and the penalty parameters. A sequence of such optimization problems are approximately minimized using a pattern search algorithm such that the linear constraints and bounds are satisfied.

A subproblem formulation is defined as

$$\Theta(x, \lambda, s, \rho) = f(x) - \sum_{i=1}^{m} \lambda_i s_i \log(s_i - c_i(x)) + \sum_{i=m+1}^{mt} \lambda_i c_i(x) + \frac{\rho}{2} \sum_{i=m+1}^{mt} c_i(x)^2$$

where

- the components λ_i of the vector λ are nonnegative and are known as Lagrange multiplier estimates
- the elements s_i of the vector s are nonnegative shifts
- ρ is the positive penalty parameter.

The algorithm begins by using an initial value for the penalty parameter (InitialPenalty).

The pattern search algorithm minimizes a sequence of the subproblem, which is an approximation of the original problem. When the subproblem is minimized to a required accuracy and satisfies feasibility conditions, the Lagrangian estimates are updated. Otherwise, the penalty parameter is increased by a penalty factor (PenaltyFactor). This results in a new subproblem formulation and minimization problem. These steps are repeated until the stopping criteria are met.

For a complete description of the algorithm, see the following references:

- [1] Lewis, Robert Michael and Virginia Torczon, "A Globally Convergent Augmented Lagrangian Pattern Search Algorithm for Optimization with General Constraints and Simple Bounds", SIAM Journal on Optimization, Volume 12, Number 4, 2002, 1075–1089.
- [2] Conn, A. R., N. I. M. Gould, and Ph. L. Toint. "A Globally Convergent Augmented Lagrangian Pattern Search Algorithm for Optimization with General Constraints and Simple Bounds", *SIAM Journal on Numerical Analysis*, Volume 28, Number 2, 1991, 545–572.
- [3] Conn, A. R., N. I. M. Gould, and Ph. L. Toint. "A Globally Convergent Augmented Lagrangian Pattern Search Algorithm for Optimization with General Constraints and Simple Bounds", *Mathematics of Computation*, Volume 66, Number 217, 1997, 261–288.

Getting Started with the Genetic Algorithm

What Is the Genetic Algorithm? (p. 3-2)

Using the Genetic Algorithm, Command Line or Tool (p. 3-3)

Example: Rastrigin's Function (p. 3-7)

Some Genetic Algorithm Terminology (p. 3-16)

How the Genetic Algorithm Works (p. 3-19)

Description of the Nonlinear Constraint Solver (p. 3-26) Introduces the genetic algorithm.

Explains how to use the Genetic Algorithm Tool.

Presents an example of solving an optimization problem using the genetic algorithm.

Explains some basic terminology for the genetic algorithm.

Presents an overview of how the genetic algorithm works.

Explains the Augmented Lagrangian Genetic Algorithm (ALGA).

What Is the Genetic Algorithm?

The genetic algorithm is a method for solving both constrained and unconstrained optimization problems that is based on natural selection, the process that drives biological evolution. The genetic algorithm repeatedly modifies a population of individual solutions. At each step, the genetic algorithm selects individuals at random from the current population to be parents and uses them to produce the children for the next generation. Over successive generations, the population "evolves" toward an optimal solution. You can apply the genetic algorithm to solve a variety of optimization problems that are not well suited for standard optimization algorithms, including problems in which the objective function is discontinuous, nondifferentiable, stochastic, or highly nonlinear.

The genetic algorithm uses three main types of rules at each step to create the next generation from the current population:

- *Selection rules* select the individuals, called *parents*, that contribute to the population at the next generation.
- *Crossover rules* combine two parents to form children for the next generation.
- *Mutation rules* apply random changes to individual parents to form children.

The genetic algorithm differs from a classical, derivative-based, optimization algorithm in two main ways, as summarized in the following table.

Classical Algorithm	Genetic Algorithm
Generates a single point at each iteration. The sequence of points approaches an optimal solution.	Generates a population of points at each iteration. The best point in the population approaches an optimal solution.
Selects the next point in the sequence by a deterministic computation.	Selects the next population by computation which uses random number generators.

Using the Genetic Algorithm, Command Line or Tool

In this section...

"Calling the Function ga at the Command Line" on page 3-3

"Using the Genetic Algorithm Tool" on page 3-4

Calling the Function ga at the Command Line

To use the genetic algorithm at the command line, call the genetic algorithm function ga with the syntax

```
[x fval] = ga(@fitnessfun, nvars, options)
```

where

- @fitnessfun is a handle to the fitness function.
- nvars is the number of independent variables for the fitness function.
- options is a structure containing options for the genetic algorithm. If you do not pass in this argument, ga uses its default options.

The results are given by

- x Point at which the final value is attained
- fval Final value of the fitness function

Using the function ga is convenient if you want to

- Return results directly to the MATLAB workspace
- Run the genetic algorithm multiple times with different options, by calling ga from an M-file

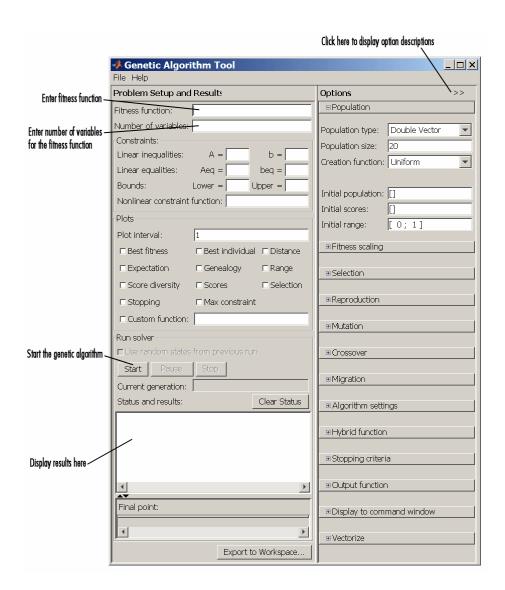
"Using the Genetic Algorithm from the Command Line" on page 6-23 provides a detailed description of using the function ga and creating the options structure.

Using the Genetic Algorithm Tool

The Genetic Algorithm Tool is a graphical user interface that enables you to use the genetic algorithm without working at the command line. To open it, enter

gatool

at the MATLAB command prompt. The tool opens as shown here.



To use the Genetic Algorithm Tool, you must first enter the following information:

• **Fitness function** — The objective function you want to minimize. Enter the fitness function in the form @fitnessfun, where fitnessfun.m is an

M-file that computes the fitness function. "Writing M-Files for Functions You Want to Optimize" on page 1-3 explains how write this M-file. The @ sign creates a function handle to fitnessfun.

• Number of variables — The length of the input vector to the fitness function. For the function my_fun described in "Writing M-Files for Functions You Want to Optimize" on page 1-3, you would enter 2.

You can enter constraints or a nonlinear constraint function for the problem in the **Constraints** pane. If the problem is unconstrained, leave these fields blank.

To run the genetic algorithm, click the **Start** button. The tool displays the results of the optimization in the **Status and results** pane.

You can change the options for the genetic algorithm in the **Options** pane. To view the options in one of the categories listed in the pane, click the + sign next to it.

For more information,

- See "Overview of the Genetic Algorithm Tool" on page 6-2 for a detailed description of the tool.
- See "Example: Rastrigin's Function" on page 3-7 for an example of using the tool.

Example: Rastrigin's Function

In this section...

"Rastrigin's Function" on page 3-7

"Finding the Minimum of Rastrigin's Function" on page 3-9

"Finding the Minimum from the Command Line" on page 3-11

"Displaying Plots" on page 3-12

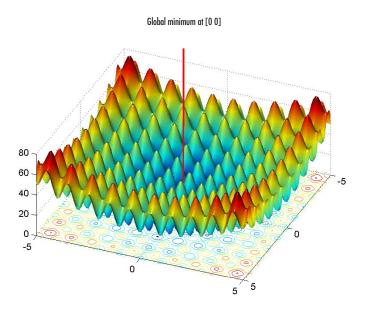
Rastrigin's Function

This section presents an example that shows how to find the minimum of Rastrigin's function, a function that is often used to test the genetic algorithm.

For two independent variables, Rastrigin's function is defined as

$$Ras(x) = 20 + x_1^2 + x_2^2 - 10(\cos 2\pi x_1 + \cos 2\pi x_2)$$

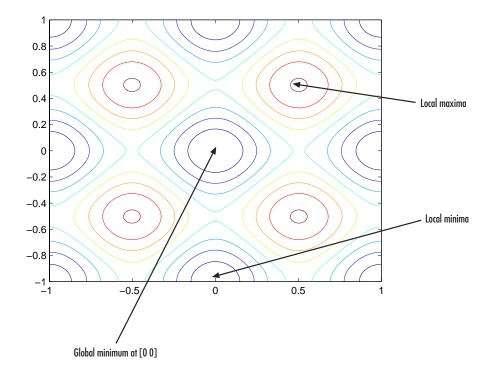
The toolbox contains an M-file, rastriginsfcn.m, that computes the values of Rastrigin's function. The following figure shows a plot of Rastrigin's function.



As the plot shows, Rastrigin's function has many local minima—the "valleys" in the plot. However, the function has just one global minimum, which occurs at the point $[0\ 0]$ in the x-y plane, as indicated by the vertical line in the plot, where the value of the function is 0. At any local minimum other than $[0\ 0]$, the value of Rastrigin's function is greater than 0. The farther the local minimum is from the origin, the larger the value of the function is at that point.

Rastrigin's function is often used to test the genetic algorithm, because its many local minima make it difficult for standard, gradient-based methods to find the global minimum.

The following contour plot of Rastrigin's function shows the alternating maxima and minima.



Finding the Minimum of Rastrigin's Function

This section explains how to find the minimum of Rastrigin's function using the genetic algorithm.

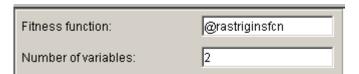
Note Because the genetic algorithm uses random number generators, the algorithm returns slightly different results each time you run it.

To find the minimum, do the following steps:

- f 1 Enter gatool at the command line to open the Genetic Algorithm Tool.
- **2** Enter the following in the Genetic Algorithm Tool:

- In the **Fitness function** field, enter @rastriginsfcn.
- In the **Number of variables** field, enter 2, the number of independent variables for Rastrigin's function.

The **Fitness function** and **Number of variables** fields should appear as shown in the following figure.



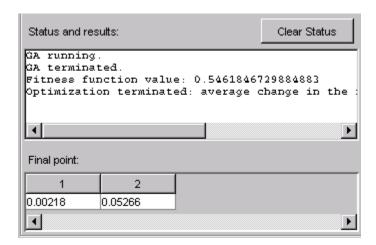
3 Click the **Start** button in the **Run solver** pane, as shown in the following figure.



While the algorithm is running, the **Current generation** field displays the number of the current generation. You can temporarily pause the algorithm by clicking the **Pause** button. When you do so, the button name changes to **Resume**. To resume the algorithm from the point at which you paused it, click **Resume**.

When the algorithm is finished, the **Status and results** pane appears as shown in the following figure.

The **Status and results** pane displays the following information:



• The final value of the fitness function when the algorithm terminated:

Function value: 0.5461846729884883

Note that the value shown is very close to the actual minimum value of Rastrigin's function, which is 0. "Genetic Algorithm Examples" on page 6-32 describes some ways to get a result that is closer to the actual minimum.

• The reason the algorithm terminated.

Optimization terminated: average change in the fitness value less than options. TolFun.

• The final point, which in this example is [0.00218 0.05266].

Finding the Minimum from the Command Line

To find the minimum of Rastrigin's function from the command line, enter

```
[x fval exitflag] = ga(@rastriginsfcn, 2)
```

This returns

Optimization terminated: average change in the fitness value less than options. TolFun.

```
x =
    0.0229
               0.0106
fval =
    0.1258
exitflag =
1
```

where

- x is the final point returned by the algorithm.
- fval is the fitness function value at the final point.
- exitflag is integer value corresponding to the reason that the algorithm terminated.

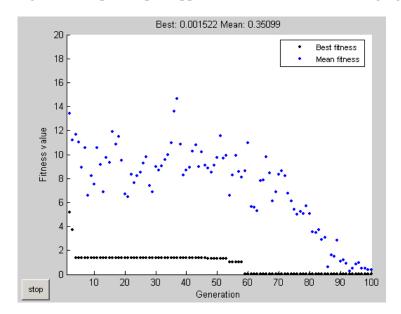
Note Because the genetic algorithm uses random number generators, the algorithm returns slightly different results each time you run it.

Displaying Plots

The **Plots** pane enables you to display various plots that provide information about the genetic algorithm while it is running. This information can help you change options to improve the performance of the algorithm. For example, to plot the best and mean values of the fitness function at each generation, select the box next to **Best fitness**, as shown in the following figure.

-Plots-		
Plot interval: 1		
✓ Best fitness	☐ Best individual	Distance
☐ Expectation	☐ Genealogy	Range
Score diversity	☐ Scores	☐ Selection
☐ Stopping	Max constraint	
Custom function:		

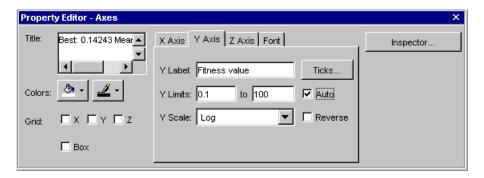
When you click **Start**, the Genetic Algorithm Tool displays a plot of the best and mean values of the fitness function at each generation. When the algorithm stops, the plot appears as shown in the following figure.



The points at the bottom of the plot denote the best fitness values, while the points above them denote the averages of the fitness values in each generation. The plot also displays the best and mean values in the current generation numerically at the top.

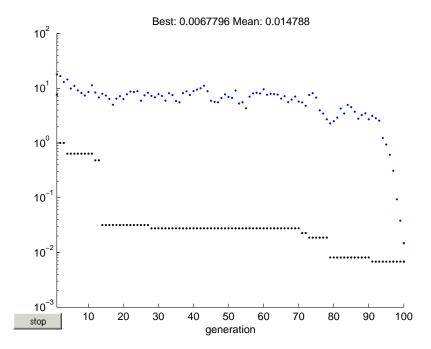
To get a better picture of how much the best fitness values are decreasing, you can change the scaling of the *y*-axis in the plot to logarithmic scaling. To do so,

1 Select **Axes Properties** from the **Edit** menu in the plot window to open the Property Editor attached to your figure window as shown below.



- 2 Click the Y tab.
- 3 In the Scale pane, select Log.

The plot now appears as shown in the following figure.



Typically, the best fitness value improves rapidly in the early generations, when the individuals are farther from the optimum. The best fitness value improves more slowly in later generations, whose populations are closer to the optimal point.

Some Genetic Algorithm Terminology

In this section...

"Fitness Functions" on page 3-16

"Individuals" on page 3-16

"Populations and Generations" on page 3-17

"Diversity" on page 3-17

"Fitness Values and Best Fitness Values" on page 3-17

"Parents and Children" on page 3-18

Fitness Functions

The *fitness function* is the function you want to optimize. For standard optimization algorithms, this is known as the objective function. The toolbox tries to find the minimum of the fitness function.

You can write the fitness function as an M-file and pass it as a function handle input argument to the main genetic algorithm function.

Individuals

An *individual* is any point to which you can apply the fitness function. The value of the fitness function for an individual is its score. For example, if the fitness function is

$$f(x_1, x_2, x_3) = (2x_1 + 1)^2 + (3x_2 + 4)^2 + (x_3 - 2)^2$$

the vector (2, -3, 1), whose length is the number of variables in the problem, is an individual. The score of the individual (2, -3, 1) is f(2, -3, 1) = 51.

An individual is sometimes referred to as a *genome* and the vector entries of an individual as *genes*.

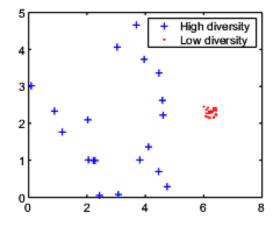
Populations and Generations

A *population* is an array of individuals. For example, if the size of the population is 100 and the number of variables in the fitness function is 3, you represent the population by a 100-by-3 matrix. The same individual can appear more than once in the population. For example, the individual (2, -3, 1) can appear in more than one row of the array.

At each iteration, the genetic algorithm performs a series of computations on the current population to produce a new population. Each successive population is called a new *generation*.

Diversity

Diversity refers to the average distance between individuals in a population. A population has high diversity if the average distance is large; otherwise it has low diversity. In the following figure, the population on the left has high diversity, while the population on the right has low diversity.



Diversity is essential to the genetic algorithm because it enables the algorithm to search a larger region of the space.

Fitness Values and Best Fitness Values

The *fitness value* of an individual is the value of the fitness function for that individual. Because the toolbox finds the minimum of the fitness function,

the *best* fitness value for a population is the smallest fitness value for any individual in the population.

Parents and Children

To create the next generation, the genetic algorithm selects certain individuals in the current population, called *parents*, and uses them to create individuals in the next generation, called *children*. Typically, the algorithm is more likely to select parents that have better fitness values.

How the Genetic Algorithm Works

In this section...

"Outline of the Algorithm" on page 3-19

"Initial Population" on page 3-20

"Creating the Next Generation" on page 3-21

"Plots of Later Generations" on page 3-23

"Stopping Conditions for the Algorithm" on page 3-23

Outline of the Algorithm

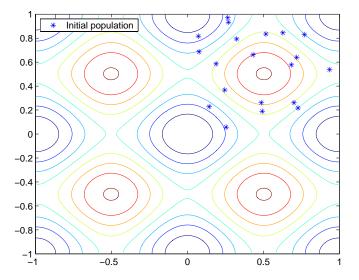
The following outline summarizes how the genetic algorithm works:

- **1** The algorithm begins by creating a random initial population.
- **2** The algorithm then creates a sequence of new populations. At each step, the algorithm uses the individuals in the current generation to create the next population. To create the new population, the algorithm performs the following steps:
 - a Scores each member of the current population by computing its fitness value.
 - **b** Scales the raw fitness scores to convert them into a more usable range of values.
 - c Selects members, called parents, based on their fitness.
 - **d** Some of the individuals in the current population that have lower fitness are chosen as *elite*. These elite individuals are passed to the next population.
 - **e** Produces children from the parents. Children are produced either by making random changes to a single parent—*mutation*—or by combining the vector entries of a pair of parents—*crossover*.
 - **f** Replaces the current population with the children to form the next generation.

3 The algorithm stops when one of the stopping criteria is met. See "Stopping Conditions for the Algorithm" on page 3-23.

Initial Population

The algorithm begins by creating a random initial population, as shown in the following figure.



In this example, the initial population contains 20 individuals, which is the default value of **Population size** in the **Population** options. Note that all the individuals in the initial population lie in the upper-right quadrant of the picture, that is, their coordinates lie between 0 and 1, because the default value of **Initial range** in the **Population** options is [0;1].

If you know approximately where the minimal point for a function lies, you should set **Initial range** so that the point lies near the middle of that range. For example, if you believe that the minimal point for Rastrigin's function is near the point [0 0], you could set **Initial range** to be [-1;1]. However, as this example shows, the genetic algorithm can find the minimum even with a less than optimal choice for **Initial range**.

Creating the Next Generation

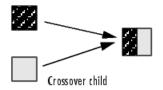
At each step, the genetic algorithm uses the current population to create the children that make up the next generation. The algorithm selects a group of individuals in the current population, called *parents*, who contribute their *genes*—the entries of their vectors—to their children. The algorithm usually selects individuals that have better fitness values as parents. You can specify the function that the algorithm uses to select the parents in the **Selection function** field in the **Selection** options.

The genetic algorithm creates three types of children for the next generation:

- *Elite children* are the individuals in the current generation with the best fitness values. These individuals automatically survive to the next generation.
- *Crossover children* are created by combining the vectors of a pair of parents.
- *Mutation children* are created by introducing random changes, or mutations, to a single parent.

The following schematic diagram illustrates the three types of children.







"Mutation and Crossover" on page 6-41 explains how to specify the number of children of each type that the algorithm generates and the functions it uses to perform crossover and mutation.

The following sections explain how the algorithm creates crossover and mutation children.

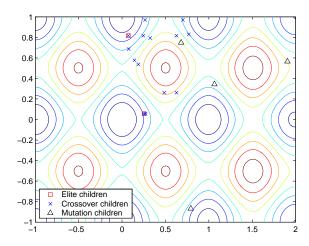
Crossover Children

The algorithm creates crossover children by combining pairs of parents in the current population. At each coordinate of the child vector, the default crossover function randomly selects an entry, or *gene*, at the same coordinate from one of the two parents and assigns it to the child.

Mutation Children

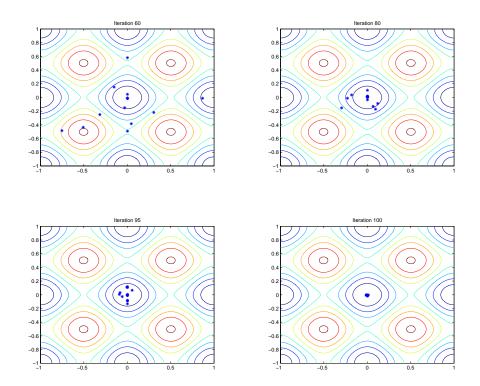
The algorithm creates mutation children by randomly changing the genes of individual parents. By default, the algorithm adds a random vector from a Gaussian distribution to the parent.

The following figure shows the children of the initial population, that is, the population at the second generation, and indicates whether they are elite, crossover, or mutation children.



Plots of Later Generations

The following figure shows the populations at iterations 60, 80, 95, and 100.



As the number of generations increases, the individuals in the population get closer together and approach the minimum point [0 0].

Stopping Conditions for the Algorithm

The genetic algorithm uses the following conditions to determine when to stop:

• **Generations** — The algorithm stops when the number of generations reaches the value of **Generations**.

- **Time limit** The algorithm stops after running for an amount of time in seconds equal to **Time limit**.
- **Fitness limit** The algorithm stops when the value of the fitness function for the best point in the current population is less than or equal to **Fitness limit**.
- **Stall generations** The algorithm stops when the weighted average change in the fitness function value over **Stall generations** is less than **Function tolerance**.
- **Stall time limit** The algorithm stops if there is no improvement in the objective function during an interval of time in seconds equal to **Stall time limit**.
- **Function Tolerance** The algorithm runs until the weighted average change in the fitness function value over **Stall generations** is less than **Function tolerance**.
- Nonlinear constraint tolerance The Nonlinear constraint tolerance is not used as stopping criterion. It is used to determine the feasibility with respect to nonlinear constraints.

The algorithm stops as soon as any one of these conditions is met. You can specify the values of these criteria in the **Stopping criteria** pane in the Genetic Algorithm Tool. The default values are shown in the figure below.

⊡ Stopping criteria	
Generations:	100
Time limit:	Inf
Fitness limit:	-Inf
Stall generations:	50
Stall time limit:	20
Function tolerance:	1e-006
Nonlinear constraint tolerance:	1e-006

When you run the genetic algorithm, the **Status and results** panel displays the criterion that caused the algorithm to stop.

The options **Stall time limit** and **Time limit** prevent the algorithm from running too long. If the algorithm stops due to one of these conditions, you might improve your results by increasing the values of **Stall time limit** and **Time limit**.

Description of the Nonlinear Constraint Solver

The genetic algorithm uses the Augmented Lagrangian Genetic Algorithm (ALGA) to solve nonlinear constraint problems. The optimization problem solved by the ALGA algorithm is

$$\min_{x} f(x)$$

such that

$$\begin{split} &C_i(x) \leq 0, i = 1...m \\ &C_i(x) = 0, \, i = m+1...mt \\ &Ax \leq b \\ &A_{eq}x = beq \\ &LB \leq x \leq UB \end{split}$$

where C(x) represents the nonlinear inequality and equality constraints, m is the number of nonlinear inequality constraints, and mt is the total number of nonlinear constraints.

The Augmented Lagrangian Genetic Algorithm (ALGA) attempts to solve a nonlinear optimization problem with nonlinear constraints, linear constraints, and bounds. In this approach, bounds and linear constraints are handled separately from nonlinear constraints. A subproblem is formulated by combining the fitness function and nonlinear constraint function using the Lagrangian and the penalty parameters. A sequence of such optimization problems are approximately minimized using the genetic algorithm such that the linear constraints and bounds are satisfied.

A subproblem formulation is defined as

$$\Theta(x, \lambda, s, \rho) = f(x) - \sum_{i=1}^{m} \lambda_i s_i \log(s_i - c_i(x)) + \sum_{i=m+1}^{mt} \lambda_i c_i(x) + \frac{\rho}{2} \sum_{i=m+1}^{mt} c_i(x)^2$$

where the components λ_i of the vector λ are nonnegative and are known as Lagrange multiplier estimates. The elements s_i of the vector s are nonnegative

shifts, and ρ is the positive penalty parameter. The algorithm begins by using an initial value for the penalty parameter (InitialPenalty).

The genetic algorithm minimizes a sequence of the subproblem, which is an approximation of the original problem. When the subproblem is minimized to a required accuracy and satisfies feasibility conditions, the Lagrangian estimates are updated. Otherwise, the penalty parameter is increased by a penalty factor (PenaltyFactor). This results in a new subproblem formulation and minimization problem. These steps are repeated until the stopping criteria are met. For a complete description of the algorithm, see the following references:

- Conn, A. R., N. I. M. Gould, and Ph. L. Toint. "A Globally Convergent Augmented Lagrangian Algorithm for Optimization with General Constraints and Simple Bounds," SIAM Journal on Numerical Analysis, Volume 28, Number 2, pages 545–572, 1991.
- Conn, A. R., N. I. M. Gould, and Ph. L. Toint. "A Globally Convergent Augmented Lagrangian Barrier Algorithm for Optimization with General Inequality Constraints and Simple Bounds," *Mathematics of Computation*, Volume 66, Number 217, pages 261–288, 1997.

Getting Started with Simulated Annealing and Threshold Acceptance

What Are Simulated Annealing and Threshold Acceptance? (p. 4-2)

Calling the Simulated Annealing and Threshold Acceptance Solvers (p. 4-3)

Example: Minimizing De Jong's Fifth Function (p. 4-4)

Some Simulated Annealing and Threshold Acceptance Terminology (p. 4-6)

How Simulated Annealing and Threshold Acceptance Work (p. 4-8) Introduces simulated annealing and threshold acceptance.

Explains how to use simulated annealing and threshold acceptance.

Presents an example of solving an optimization problem using simulated annealing.

Explains some basic terminology for simulated annealing and threshold acceptance.

Presents an overview of how the simulated annealing algorithm works.

What Are Simulated Annealing and Threshold Acceptance?

Simulated annealing is a method for solving unconstrained and bound-constrained optimization problems. The method models the physical process of heating a material and then slowly lowering the temperature to decrease defects, thus minimizing the system energy.

At each iteration of the simulated annealing algorithm, a new point is randomly generated. The distance of the new point from the current point, or the extent of the search, is based on a probability distribution with a scale proportional to the temperature. The algorithm accepts all new points that lower the objective, but also, with a certain probability, points that raise the objective. By accepting points that raise the objective, the algorithm avoids being trapped in local minima, and is able to explore globally for more possible solutions. An annealing schedule is selected to systematically decrease the temperature as the algorithm proceeds. As the temperature decreases, the algorithm reduces the extent of its search to converge to a minimum.

Threshold acceptance uses a similar approach, but instead of accepting new points that raise the objective with a certain probability, it accepts all new points below a fixed threshold. The threshold is then systematically lowered, just as the temperature is lowered in an annealing schedule. Because threshold acceptance avoids the probabilistic acceptance calculations of simulated annealing, it may locate an optimizer faster than simulated annealing.

Calling the Simulated Annealing and Threshold Acceptance Solvers

This section provides a brief introduction to using the simulated annealing and threshold acceptance at the command line. To simplify the presentation, this section uses only the simulated annealing function simulannealbnd. The threshold acceptance function threshacceptbnd has the same syntax.

To call the simulated annealing function at the command line, use the syntax

```
[x fval] = simulannealbnd(@objfun, x0, lb, ub, options)
```

where

- @objfun is a function handle to the objective function.
- x0 is an initial guess for the optimizer.
- 1b and ub are lower and upper bound constraints, respectively, on x.
- options is a structure containing options for the algorithm. If you do not pass in this argument, simulannealbnd uses its default options.

The results are given by:

- x Final point returned by the solver
- fval Value of the objective function at x

The command-line function simulannealbnd is convenient if you want to

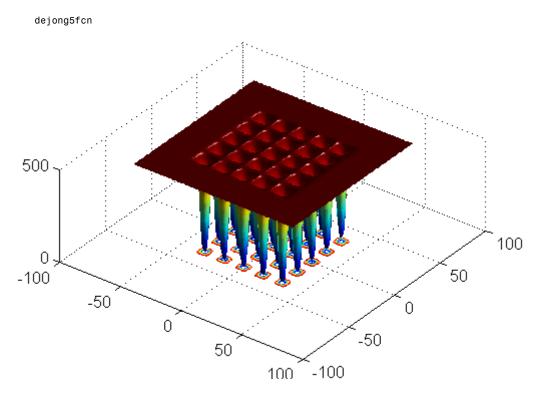
- Return results directly to the MATLAB workspace.
- Run the simulated annealing algorithm multiple times with different options by calling simulannealbnd from an M-file.

"Using the Simulated Annealing and Threshold Acceptance Algorithms from the Command Line" on page 7-2 provides a detailed description of using the function simulannealbnd and creating the options structure.

Example: Minimizing De Jong's Fifth Function

This section presents an example that shows how to find the minimum of the function using simulated annealing.

De Jong's fifth function is a two-dimensional function with many (25) local minima:



Many standard optimization algorithms get stuck in local minima. Because the simulated annealing algorithm performs a wide random search, the chance of being trapped in local minima is decreased.

To run the simulated annealing algorithm without constraints, call simulannealbnd at the command line using the objective function in dejong5fcn.m, referenced by anonymous function pointer:

```
fun = @dejong5fcn;
  [x fval] = simulannealbnd(fun, [0 0])
This returns
  x =
    -31.9779 -31.9595
  fval =
```

where

0.9980

- x is the final point returned by the algorithm.
- fval is the objective function value at the final point.

Note Because simulated annealing and threshold acceptance both use random number generators, each time you run these algorithms you may get different results. See "Reproducing Your Results" on page 7-5 for more information.

Some Simulated Annealing and Threshold Acceptance Terminology

In this section...

"Objective Function" on page 4-6

"Temperature" on page 4-6

"Annealing Schedule" on page 4-6

"Reannealing" on page 4-6

Objective Function

The *objective function* is the function you want to optimize. The algorithms in the toolbox attempt to find the minimum of the objective function. Write the objective function as an M-file and pass it to the solver as a function handle.

Temperature

The *temperature* is the control parameter in simulated annealing that is decreased gradually as the algorithm proceeds. It determines the probability of accepting a worse solution at any step and is used to limit the extent of the search in a given dimension. You can specify the initial temperature as an integer in the InitialTemperature option, and the annealing schedule as a function to the TemperatureFcn option.

Annealing Schedule

The *annealing schedule* is the rate by which the temperature is decreased as the algorithm proceeds. The slower the rate of decrease, the better the chances are of finding an optimal solution, but the longer the run time. You can specify the temperature schedule as a function handle with the TemperatureFcn option.

Reannealing

Annealing is the technique of closely controlling the temperature when cooling a material to ensure that it is brought to an optimal state. *Reannealing* raises the temperature after a certain number of new points have been accepted,

and starts the search again at the higher temperature. Reannealing avoids getting caught at local minima. You specify the reannealing schedule with the ReannealInterval option.

How Simulated Annealing and Threshold Acceptance Work

In this section...

"Outline of the Algorithm" on page 4-8

"Stopping Conditions for the Algorithm" on page 4-9

Outline of the Algorithm

The following is an outline of the steps performed for both the simulated annealing and threshold acceptance algorithms:

- 1 The algorithm begins by randomly generating a new point. The distance of the new point from the current point, or the extent of the search, is determined by a probability distribution with a scale proportional to the current temperature.
- **2** The algorithm determines whether the new point is better or worse than the current point. If the new point is better than the current point, it becomes the next point. If the new point is worse than the current point, the algorithm may still make it the next point. Simulated annealing accepts a worse point based on an acceptance probability. Threshold acceptance accepts a worse point if the objective function is raised by less than a fixed threshold.
- **3** The algorithm systematically lowers the temperature and (for threshold acceptance) the threshold, storing the best point found so far.
- 4 Reannealing is performed after a certain number of points (ReannealInterval) are accepted by the solver. Reannealing raises the temperature in each dimension, depending on sensitivity information. The search is resumed with the new temperature values.
- **5** The algorithm stops when the average change in the objective function is very small, or when any other stopping criteria are met. See "Stopping Conditions for the Algorithm" on page 4-9.

Stopping Conditions for the Algorithm

The simulated annealing and threshold acceptance algorithms use the following conditions to determine when to stop:

- TolFun The algorithm runs until the average change in value of the objective function in StallIterLim iterations is less than TolFun. The default value is 1e-6.
- MaxIter The algorithm stops if the number of iterations exceeds this maximum number of iterations. You can specify the maximum number of iterations as a positive integer or Inf. Inf is the default.
- MaxFunEval specifies the maximum number of evaluations of the objective function. The algorithm stops if the number of function evaluations exceeds the maximum number of function evaluations. The allowed maximum is 3000*numberofvariables.
- TimeLimit specifies the maximum time in seconds the algorithm runs before stopping.
- ObjectiveLimit The algorithm stops if the best objective function value is less than or equal to the value of ObjectiveLimit.

Using Direct Search

Overview of the Pattern Search Tool (GUI) (p. 5-2)

Performing a Pattern Search from the Command Line (p. 5-19)

Pattern Search Examples: Setting Options (p. 5-25)

Parameterizing Functions Called by patternsearch (p. 5-52)

Provides an overview of the Pattern Search Tool.

Explains how to perform a pattern search from the command line.

Explains how to set options for a pattern search.

Explains how to write functions with additional parameters.

Overview of the Pattern Search Tool (GUI)

In this section...

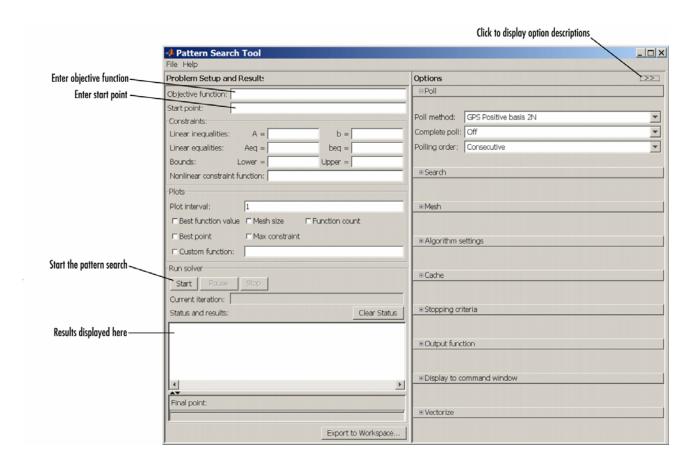
- "Opening the Pattern Search Tool" on page 5-2
- "Defining a Problem in the Pattern Search Tool" on page 5-3
- "Running a Pattern Search" on page 5-4
- "Example A Linearly Constrained Problem" on page 5-5
- "Pausing and Stopping the Algorithm" on page 5-8
- "Displaying Plots" on page 5-8
- "Example Working with a Custom Plot Function" on page 5-10
- "Setting Options in the Pattern Search Tool" on page 5-14
- "Importing and Exporting Options and Problems" on page 5-15
- "Generating an M-File" on page 5-18

Opening the Pattern Search Tool

To open the tool, enter

psearchtool

at the MATLAB prompt. This opens the Pattern Search Tool, as shown here.

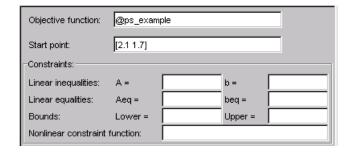


Defining a Problem in the Pattern Search Tool

You can define the problem you want to solve using the following fields:

- **Objective function** The function you want to minimize. Enter a handle to an M-file function that computes the objective function. "Writing M-Files for Functions You Want to Optimize" on page 1-3 describes how to write the M-file.
- **Start point** The starting point for the pattern search algorithm.

The following figure shows these fields for the example described in "Example: Finding the Minimum of a Function Using the GPS Algorithm" on page 2-6.



Constrained Problems

You can enter any constraints for the problem in the following fields in the **Constraints** pane:

- Linear inequalities Enter the following for inequality constraints of the form *Ax* ≤ *b*:
 - Enter the matrix A in the A = field.
 - Enter the vector b in the b = field.
- **Linear equalities** Enter the following for equality constraints of the form $Aeq \ x = beq$:
 - Enter the matrix Aeq in the Aeq = field.
 - Enter the vector beq in the **beq** = field.
- **Bounds** Enter the following information for bounds constraints of the form $lb \le x$ and $x \le ub$:
 - Enter the vector 1b for the lower bound in the **Lower** = field.
 - Enter the vector ub in the **Upper** = field.

Leave the fields that correspond to constraints, such as the **Nonlinear constraint function** field which does not appear in the problem, empty.

Running a Pattern Search

To run a pattern search, click Start in the Run solver pane. When you do so,

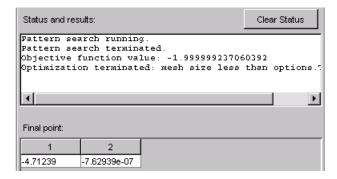
• The **Current iteration** field displays the number of the current iteration.

• The **Status and results** pane displays the message Pattern search running.

When the pattern search terminates, the **Status and results** pane displays

- The message Pattern search terminated.
- The objective function value at the final point
- The reason the pattern search terminated
- The **Final Point** field displays coordinates of the final point.

The following figure shows this information displayed when you run the example in "Example: Finding the Minimum of a Function Using the GPS Algorithm" on page 2-6.



Example — A Linearly Constrained Problem

This section presents an example of performing a pattern search on a constrained minimization problem. The example minimizes the function

$$F(x) = \frac{1}{2}x^T H x + f^T x$$

where

$$H = \begin{bmatrix} 36 & 17 & 19 & 12 & 8 & 15 \\ 17 & 33 & 18 & 11 & 7 & 14 \\ 19 & 18 & 43 & 13 & 8 & 16 \\ 12 & 11 & 13 & 18 & 6 & 11 \\ 8 & 7 & 8 & 6 & 9 & 8 \\ 15 & 14 & 16 & 11 & 8 & 29 \end{bmatrix}$$

$$f = \begin{bmatrix} 20 & 15 & 21 & 18 & 29 & 24 \end{bmatrix}$$

subject to the constraints

$$A \cdot x \le b$$

$$Aeq \cdot x = beq$$

where

$$A = \begin{bmatrix} -8 & 7 & 3 & -4 & 9 & 0 \end{bmatrix}$$

$$b = \begin{bmatrix} 7 \\ 1 & 8 & 3 & 3 & 3 \end{bmatrix}$$

$$5 & 0 & 5 & 1 & 5 & 8 \\ 2 & 6 & 7 & 1 & 1 & 8 \\ 1 & 0 & 0 & 0 & 0 \end{bmatrix}$$

$$beq = \begin{bmatrix} 84 & 62 & 65 & 1 \end{bmatrix}$$

Performing a Pattern Search on the Example

To perform a pattern search on the example, first enter

psearchtool

to open the Pattern Search Tool. Then type the following function in the Objective function field:

@lincontest7

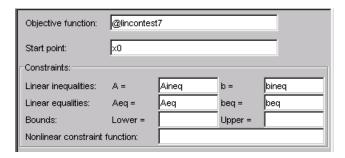
This is an M-file included in the toolbox that computes the objective function for the example. Because the matrices and vectors defining the starting point and constraints are large, it is more convenient to set their values as variables in the MATLAB workspace first and then enter the variable names in the Pattern Search Tool. To do so, enter

```
x0 = [2 1 0 9 1 0];
Aineq = [-8 7 3 -4 9 0];
bineq = [7];
Aeq = [7 1 8 3 3 3; 5 0 5 1 5 8; 2 6 7 1 1 8; 1 0 0 0 0 0];
beq = [84 62 65 1];
```

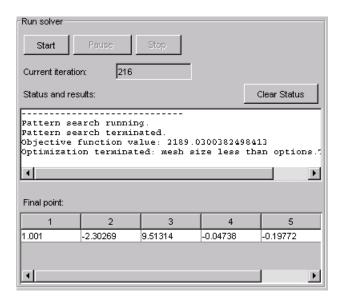
Then, enter the following in the Pattern Search Tool:

- Set **Initial point** to x0.
- Set the following **Linear inequalities**:
 - Set \mathbf{A} = to Aineq.
 - Set \mathbf{b} = to bineq.
 - Set Aeq = to Aeq.
 - Set **beq** = to beq.

The following figure shows these settings in the Pattern Search Tool.



Then click **Start** to run the pattern search. When the search is finished, the results are displayed in **Status and results** pane, as shown in the following figure.



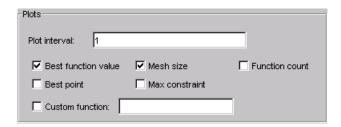
Pausing and Stopping the Algorithm

While pattern search is running, you can

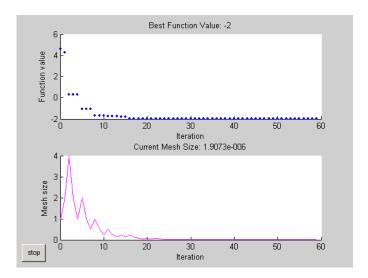
- Click **Pause** to temporarily suspend the algorithm. To resume the algorithm from the point at which you paused, click **Resume**.
- Click **Stop** to stop the algorithm. The **Status and results** pane displays the objective function value of the current point at the moment you clicked Stop.

Displaying Plots

The Plots pane, shown in the following figure, enables you to display various plots of the results of a pattern search.



Select the check boxes next to the plots you want to display. For example, if you select **Best function value** and **Mesh size**, and run the example described in "Example: Finding the Minimum of a Function Using the GPS Algorithm" on page 2-6, the tool displays the plots shown in the following figure.



The upper plot displays the objective function value at each iteration. The lower plot displays the mesh size at each iteration.

Note When you display more than one plot, clicking on any plot while the pattern search is running or after the solver has completed opens a larger version of the plot in a separate window.

"Plot Options" on page 8-24 describes the types of plots you can create.

Example — Working with a Custom Plot Function

To use a plot function other than those included with the toolbox, you can write your own custom plot function that is called at each iteration of the pattern search to create the plot. This example shows how to create a plot function that displays the logarithmic change in the best objective function value from the previous iteration to the current iteration.

This section covers the following topics:

- "Creating the Custom Plot Function" on page 5-10
- "Using the Custom Plot Function" on page 5-11
- "How the Plot Function Works" on page 5-12

Creating the Custom Plot Function

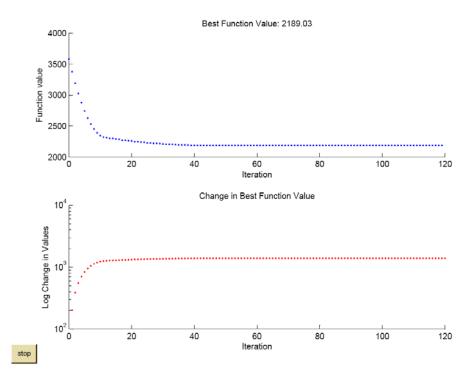
To create the plot function for this example, copy and paste the following code into a new M-file in the MATLAB Editor.

```
function stop = psplotchange(optimvalues, flag)
% PSPLOTCHANGE Plots the change in the best objective function
% value from the previous iteration.
% Best objective function value in the previous iteration
persistent last best
stop = false;
if(strcmp(flag, 'init'))
        set(gca, 'Yscale', 'log'); %Set up the plot
        hold on;
        xlabel('Iteration');
        ylabel('Log Change in Values');
        title(['Change in Best Function Value']);
% Best objective function value in the current iteration
best = min(optimvalues.fval);
```

Then save the M-file as psplotchange.m in a directory on the MATLAB path.

Using the Custom Plot Function

To use the custom plot function, select **Custom function** in the **Plots** pane and enter <code>@psplotchange</code> in the field to the right. To compare the custom plot with the best function value plot, also select **Best function value**. Now, when you run the example described in "Example — A Linearly Constrained Problem" on page 5-5, the pattern search tool displays the plots shown in the following figure.



Note that because the scale of the *y*-axis in the lower custom plot is logarithmic, the plot will only show changes that are greater than 0. The logarithmic scale shows small changes in the objective function that the upper plot does not reveal.

How the Plot Function Works

The plot function uses information contained in the following structures, which the Pattern Search Tool passes to the function as input arguments:

- optimvalues Structure containing the current state of the solver
- flag String indicating the current status of the algorithm

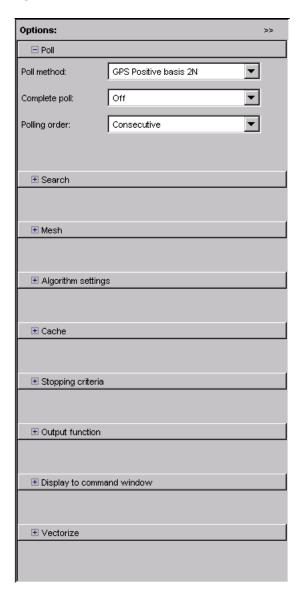
The most important statements of the custom plot function, psplotchange.m, are summarized in the following table.

Custom Plot Function Statements

M-File Statement	Description
persistent last_best	Creates the persistent variable last_best, the best objective function value in the previous generation. Persistent variables are preserved over multiple calls to the plot function.
<pre>set(gca,'Yscale','log')</pre>	Sets up the plot before the algorithm starts.
<pre>best = min(optimvalues.fval)</pre>	Sets best equal to the minimum objective function value. The field optimvalues.fval contains the objective function value in the current iteration. The variable best is the minimum objective function value. For a complete description of the fields of the structure optimvalues, see "Structure of the Plot Functions" on page 8-4.
<pre>change = last_best - best</pre>	Sets the variable change to the best objective function value at the previous iteration minus the best objective function value in the current iteration.
<pre>plot(optimvalues.iteration, change, '.r')</pre>	Plots the variable change at the current objective function value, for the current iteration contained in optimvalues.iteration.

Setting Options in the Pattern Search Tool

You can set options for a pattern search in the Options pane, shown in the figure below.



For a detailed description of the available options, see "Pattern Search Options" on page 8-2.

Setting Options as Variables in the MATLAB Workspace

You can set numerical options either directly, by typing their values in the corresponding edit box, or by entering the name of a variable in the MATLAB workspace that contains the option values. For options whose values are large matrices or vectors, it is often more convenient to define their values as variables in the MATLAB workspace.

Importing and Exporting Options and Problems

You can export options and problem structures from the Pattern Search Tool to the MATLAB workspace, and later import them in a subsequent session of the tool. This provides an easy way to save your work for future sessions of the Pattern Search Tool. The following sections describe how to import and export options and problem structures.

Exporting Options, Problems, and Results

After working on a problem using the Pattern Search Tool, you can export the following information to the MATLAB workspace:

- The problem definition, including
 - The objective function
 - The start point
 - Constraints on the problem
- The current options
- The results of the algorithm

To do so, click the **Export to Workspace** button or select **Export to Workspace** from the **File** menu. This opens the dialog box shown in the following figure.



The dialog box provides the following options:

• To save the objective function and options in a MATLAB structure, select Export problem and options to a MATLAB structure named and enter a name for the structure.

If you have run a pattern search in the current session and you select **Include information needed to resume this run**, the final point from the last search is saved in place of **Start point**. Use this option if you want to run the pattern search at a later time from the final point of the last search.

See "Importing a Problem" on page 5-18.

- To save only the options, select Export options to a MATLAB structure **named** and enter a name for the options structure.
- To save the results of the last run of the algorithm, select Export results to a MATLAB structure named and enter a name for the results structure.

Example — Running patternsearch on an Exported Problem

To export the problem described in "Example — A Linearly Constrained Problem" on page 5-5 and perform a pattern search on it using the function patternsearch at the command line, do the following steps:

- 1 Click Export to Workspace.
- **2** In the Export to Workspace dialog box, enter a name for the problem structure, such as my_psproblem, in the Export problems and options to a MATLAB structure named field.

3 Call the function patternsearch with my_psproblem as the input argument.

```
[x fval] = patternsearch(my_psproblem)
```

This returns

```
x =
   1.0010 -2.3027 9.5131 -0.0474 -0.1977 1.3083

fval =
   2.1890e+003
```

See "Performing a Pattern Search from the Command Line" on page 5-19 for more information.

Importing Options

To import an options structure for a pattern search from the MATLAB workspace, select **Import Options** from the **File** menu. This opens a dialog box that displays a list of the valid pattern search options structures in the MATLAB workspace. When you select an options structure and click **Import**, the Pattern Search Tool resets its options to the values in the imported structure.

Note You cannot import options structures that contain any invalid option fields. Structures with invalid fields are not displayed in the Import Pattern Search Options dialog box.

You can create an options structure in either of the following ways:

- Calling psoptimset with options as the output
- By saving the current options from the Export to Workspace dialog box in the Pattern Search Tool

Importing a Problem

To import a problem that you previously exported from the Pattern Search Tool, select **Import Problem** from the **File** menu. This opens the dialog box that displays a list of the pattern search problem structures in the MATLAB workspace. When you select a problem structure and click **OK**, the Pattern Search Tool resets the problem definition and the options to the values in the imported structure. In addition, if you selected **Include information needed to resume this run** when you created the problem structure, the tool resets **Start point** to the final point of the last run prior to exporting the structure.

See "Exporting Options, Problems, and Results" on page 5-15.

Generating an M-File

To create an M-file that runs a pattern search using the objective function and options you specify in the Pattern Search Tool, select Generate M-File from the **File** menu and save the M-file in a directory on the MATLAB path. Calling this M-file at the command line returns the same results as the Pattern Search Tool, using the objective function and options settings that were in place when you generated the M-file.

Performing a Pattern Search from the Command Line

In this section...

"Calling patternsearch with the Default Options" on page 5-19

"Setting Options for patternsearch at the Command Line" on page 5-21

"Using Options and Problems from the Pattern Search Tool" on page 5-23

Calling patternsearch with the Default Options

This section describes how to perform a pattern search with the default options.

Pattern Search on Unconstrained Problems

For an unconstrained problem, call patternsearch with the syntax

```
[x fval] = patternsearch(@objectfun, x0)
```

The output arguments are

- x The final point
- fval The value of the objective function at x

The required input arguments are

- @objectfun A function handle to the objective function objectfun, which you can write as an M-file. See "Writing M-Files for Functions You Want to Optimize" on page 1-3 to learn how to do this.
- ullet x0 The initial point for the pattern search algorithm.

As an example, you can run the example described in "Example: Finding the Minimum of a Function Using the GPS Algorithm" on page 2-6 from the command line by entering

```
[x fval] = patternsearch(@ps example, [2.1 1.7])
```

This returns

Optimization terminated: mesh size less than options. TolMesh.

```
x =
   -4.7124
              -0.0000
fval =
   -2,0000
```

Pattern Search on Constrained Problems

If your problem has constraints, use the syntax

```
[x fval] = patternsearch(@objfun,x0,A,b,Aeq,beq,lb,ub,nonlcon)
```

where

- A is a matrix and b is vector that represent inequality constraints of the form $Ax \leq b$.
- Aeq is a matrix and beq is a vector that represent equality constraints of the form Aeq x = beq
- 1b and ub are vectors representing bound constraints of the form $lb \le x$ and $x \le ub$, respectively.
- nonlcon is a function that returns the nonlinear equality and inequality vectors, C and Ceq, respectively. The function is minimized such that $C(x) \le 0$ and Ceq(x)=0.

You only need to pass in the constraints that are part of the problem. For example, if there are no bound constraints or a nonlinear constraint function, use the syntax

```
[x fval] = patternsearch(@objfun, x0, A, b Aeq, beq)
```

Use empty brackets [] for constraint arguments that are not needed for the problem. For example, if there are no inequality constraints or a nonlinear constraint function, use the syntax

```
[x \text{ fval}] = \text{patternsearch}(@objfun, x0, [], [], Aeq, beq, lb, ub)
```

Additional Output Arguments

To get more information about the performance of the pattern search, you can call patternsearch with the syntax

```
[x fval exitflag output] = patternsearch(@objfun, x0)
```

Besides x and fval, this returns the following additional output arguments:

- exitflag Integer indicating whether the algorithm was successful
- output Structure containing information about the performance of the solver

See the reference page for patternsearch for more information about these arguments.

Setting Options for patternsearch at the Command Line

You can specify any of the options that are available in the Pattern Search Tool by passing an options structure as an input argument to patternsearch using the syntax

Pass in empty brackets [] for any constraints that do not appear in the problem.

You create the options structure using the function psoptimset.

```
options = psoptimset
```

This returns the options structure with the default values for its fields.

```
options =
```

TolMesh: 1.0000e-006 TolCon: 1.0000e-006

```
TolX: 1.0000e-006
         TolFun: 1.0000e-006
        TolBind: 1.0000e-003
        MaxIter: '100*numberofvariables'
    MaxFunEvals: '2000*numberofvariables'
      TimeLimit: Inf
MeshContraction: 0.5000
  MeshExpansion: 2
MeshAccelerator: 'off'
     MeshRotate: 'on'
InitialMeshSize: 1
      ScaleMesh: 'on'
    MaxMeshSize: Inf
 InitialPenalty: 10
  PenaltyFactor: 100
     PollMethod: 'gpspositivebasis2n'
   CompletePoll: 'off'
   PollingOrder: 'consecutive'
   SearchMethod: []
CompleteSearch: 'off'
        Display: 'final'
     OutputFcns: []
       PlotFcns: []
   PlotInterval: 1
          Cache: 'off'
      CacheSize: 10000
       CacheTol: 2.2204e-016
     Vectorized: 'off'
```

The function patternsearch uses these default values if you do not pass in options as an input argument.

The value of each option is stored in a field of the options structure, such as options. MeshExpansion. You can display any of these values by entering options followed by the name of the field. For example, to display the mesh expansion factor for the pattern search, enter

```
options.MeshExpansion
ans =
   2
```

To create an options structure with a field value that is different from the default, use the function psoptimset. For example, to change the mesh expansion factor to 3 instead of its default value 2, enter

```
options = psoptimset('MeshExpansion', 3)
```

This creates the options structure with all values set to their defaults except for MeshExpansion, which is set to 3.

If you now call patternsearch with the argument options, the pattern search uses a mesh expansion factor of 3.

If you subsequently decide to change another field in the options structure, such as setting PlotFcns to @psplotmeshsize, which plots the mesh size at each iteration, call psoptimset with the syntax

```
options = psoptimset(options, 'PlotFcns', @psplotmeshsize)
```

This preserves the current values of all fields of options except for PlotFcns, which is changed to @plotmeshsize. Note that if you omit the options input argument, psoptimset resets MeshExpansion to its default value, which is 2.

You can also set both MeshExpansion and PlotFcns with the single command

```
options = psoptimset('MeshExpansion',3,'PlotFcns',@plotmeshsize)
```

Using Options and Problems from the Pattern Search Tool

As an alternative to creating the options structure using psoptimset, you can set the values of options in the Pattern Search Tool and then export the options to a structure in the MATLAB workspace, as described in "Exporting Options, Problems, and Results" on page 5-15. If you export the default options in the Pattern Search Tool, the resulting options structure has the same settings as the default structure returned by the command

options = psoptimset

except for the default value of 'Display', which is 'final' when created by psoptimset, but 'none' when created in the Pattern Search Tool.

You can also export an entire problem from the Pattern Search Tool and run it from the command line. See "Example — Running patternsearch on an Exported Problem" on page 5-16 for an example.

Pattern Search Examples: Setting Options

In this section...

"Poll Method" on page 5-25

"Complete Poll" on page 5-27

"Using a Search Method" on page 5-32

"Mesh Expansion and Contraction" on page 5-35

"Mesh Accelerator" on page 5-40

"Using Cache" on page 5-41

"Setting Tolerances for the Solver" on page 5-43

"Constrained Minimization Using patternsearch" on page 5-48

Note All examples use the generalized pattern search (GPS) algorithm, but can be applied to the MADS algorithm as well.

Poll Method

At each iteration, the pattern search polls the points in the current mesh—that is, it computes the objective function at the mesh points to see if there is one whose function value is less than the function value at the current point. "How Pattern Search Works" on page 2-13 provides an example of polling. You can specify the pattern that defines the mesh by the **Poll method** option. The default pattern, GPS Positive basis 2N, consists of the following 2N directions, where N is the number of independent variables for the objective function.

```
[100...0]
[010...0]
   ...
[000...1]
[-1 \ 00...0]
[0 - 10...0]
[0\ 00...-1]
```

For example, if objective function has three independent variables, the GPS Positive basis 2N, consists of the following six vectors.

 $\begin{bmatrix} 1 & 0 & 0 \end{bmatrix}$ [0 1 0] $\begin{bmatrix} 0 & 0 & 1 \end{bmatrix}$ $\begin{bmatrix} -1 & 0 & 0 \end{bmatrix}$ $\begin{bmatrix} 0 & -1 & 0 \end{bmatrix}$ $[0 \ 0 \ -1]$

Alternatively, you can set **Poll method** to GPS Positive basis NP1, the pattern consisting of the following N + 1 directions.

```
[100...0]
[010...0]
   ...
[000...1]
[-1 -1 -1 ... -1]
```

For example, if objective function has three independent variables, the GPS Positive basis Np1, consists of the following four vectors.

A pattern search will sometimes run faster using GPS Positive basis Np1 rather than the GPS Positive basis 2N as the **Poll method**, because the algorithm searches fewer points at each iteration. Although not being addressed in this example, the same is true when using the MADS Positive basis Np1 over the MADS Positive basis 2N. For example, if you run a pattern search on the example described in "Example — A Linearly Constrained Problem" on page 5-5, the algorithm performs 2080 function evaluations with GPS Positive basis 2N, the default **Poll method**, but only 1413 function evaluations using GPS Positive basis Np1.

However, if the objective function has many local minima, using GPS Positive basis 2N as the **Poll method** might avoid finding a local minimum that is not the global minimum, because the search explores more points around the current point at each iteration.

Complete Poll

By default, if the pattern search finds a mesh point that improves the value of the objective function, it stops the poll and sets that point as the current point for the next iteration. When this occurs, some mesh points might not get polled. Some of these unpolled points might have an objective function value that is even lower than the first one the pattern search finds.

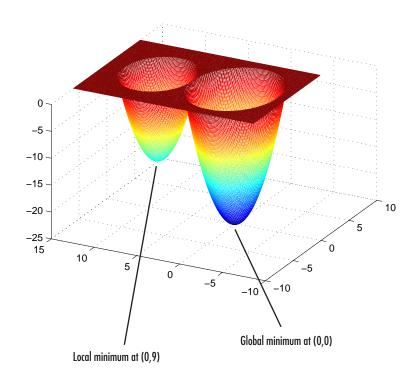
For problems in which there are several local minima, it is sometimes preferable to make the pattern search poll *all* the mesh points at each iteration and choose the one with the best objective function value. This enables the pattern search to explore more points at each iteration and thereby potentially avoid a local minimum that is not the global minimum. You can make the pattern search poll the entire mesh setting **Complete poll** to On in **Poll** options.

Example — Using a Complete Poll in a Generalized Pattern Search

As an example, consider the following function.

$$f(x_1, x_2) = \begin{cases} x_1^2 + x_2^2 - 25 & \text{for } x_1^2 + x_2^2 \le 25 \\ x_1^2 + (x_2 - 9)^2 - 16 & \text{for } x_1^2 + (x_2 - 9)^2 \le 16 \\ 0 & \text{otherwise} \end{cases}$$

The following figure shows a plot of the function.



The global minimum of the function occurs at (0, 0), where its value is -25. However, the function also has a local minimum at (0, 9), where its value is -16.

To create an M-file that computes the function, copy and paste the following code into a new M-file in the MATLAB Editor.

```
function z = poll_example(x)

if x(1)^2 + x(2)^2 <= 25

z = x(1)^2 + x(2)^2 - 25;

elseif x(1)^2 + (x(2) - 9)^2 <= 16

z = x(1)^2 + (x(2) - 9)^2 - 16;

else z = 0;

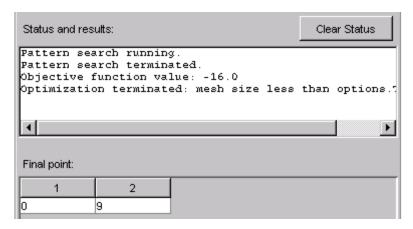
end
```

Then save the file as poll example.m in a directory on the MATLAB path.

To run a pattern search on the function, enter the following in the Pattern Search Tool:

- Set **Objective function** to @poll example.
- Set Start point to [0 5].
- Set Level of display to Iterative in the Display to command window options.

Click **Start** to run the pattern search with **Complete poll** set to Off, its default value. The Pattern Search Tool displays the results in the **Status and results** pane, as shown in the following figure.



The pattern search returns the local minimum at (0, 9). At the initial point, (0, 5), the objective function value is 0. At the first iteration, the search polls the following mesh points.

$$f((0, 5) + (1, 0)) = f(1, 5) = 0$$

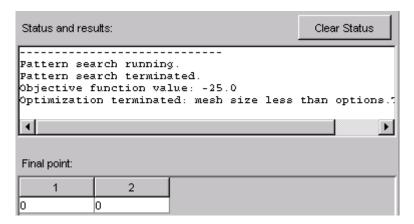
$$f((0, 5) + (0, 1)) = f(0, 6) = -7$$

As soon as the search polls the mesh point (0, 6), at which the objective function value is less than at the initial point, it stops polling the current mesh and sets the current point at the next iteration to (0, 6). Consequently, the search moves toward the local minimum at (0, 9) at the first iteration. You see this by looking at the first two lines of the command line display.

Iter	f-count	MeshSize	f(x)	Method
0	1	1	0	Start iterations
1	3	2	- 7	Successful Poll

Note that the pattern search performs only two evaluations of the objective function at the first iteration, increasing the total function count from 1 to 3.

Next, set **Complete poll** to 0n and click **Start**. The **Status and results** pane displays the following results.



This time, the pattern search finds the global minimum at (0, 0). The difference between this run and the previous one is that with **Complete poll** set to 0n, at the first iteration the pattern search polls all four mesh points.

$$f((0, 5) + (1, 0)) = f(1, 5) = 0$$

$$f((0, 5) + (0, 1)) = f(0, 6) = -6$$

$$f((0, 5) + (-1, 0)) = f(-1, 5) = 0$$

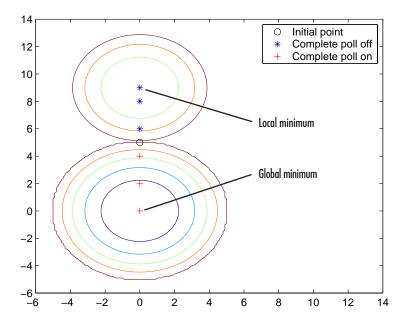
$$f((0, 5) + (0, -1)) = f(0, 4) = -9$$

Because the last mesh point has the lowest objective function value, the pattern search selects it as the current point at the next iteration. The first two lines of the command-line display show this.

Iter	f-count	MeshSize	f(x)	Method
0	1	1	0	Start iterations
1	5	2	- 9	Successful Poll

In this case, the objective function is evaluated four times at the first iteration. As a result, the pattern search moves toward the global minimum at (0, 0).

The following figure compares the sequence of points returned when **Complete poll** is set to 0ff with the sequence when **Complete poll** is 0n.



Using a Search Method

In addition to polling the mesh points, the pattern search algorithm can perform an optional step at every iteration, called *search*. At each iteration, the search step applies another optimization method to the current point. If this search does not improve the current point, the poll step is performed.

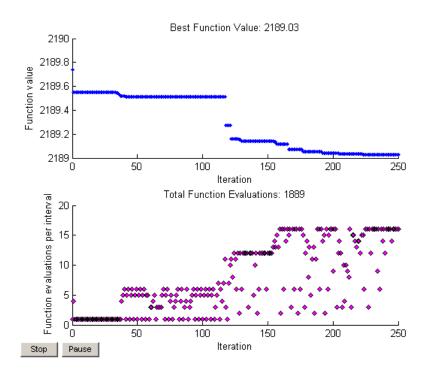
The following example illustrates the use of a search method on the problem described in "Example — A Linearly Constrained Problem" on page 5-5. To set up the example, enter the following commands at the MATLAB prompt to define the initial point and constraints.

```
x0 = [2 1 0 9 1 0];
Aineq = [-8 7 3 -4 9 0 ];
bineq = [7];
Aeq = [7 1 8 3 3 3; 5 0 5 1 5 8; 2 6 7 1 1 8; 1 0 0 0 0 0];
beq = [84 62 65 1];
```

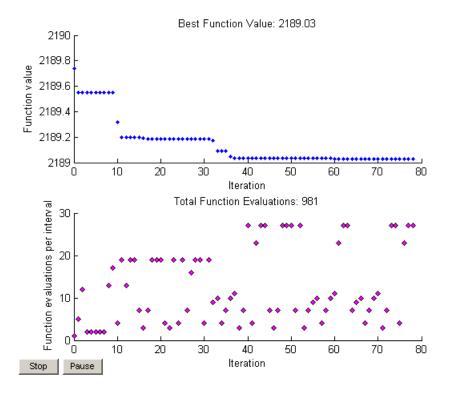
Then enter the settings shown in the following figure in the Pattern Search Tool.

Objective function: ali	incontest7	
Start point: x0		
Constraints:		
Linear inequalities:	A = Aineq	b = bineq
Linear equalities:	Aeq = Aeq	beq = beq
Bounds: L	ower =	Upper =
Nonlinear constraint fu	unction:	
Plots		
Plot interval:	1	
☑ Best function value	□ Mesh size	
□ Best point	□ Max constraint	
□ Custom function:		

For comparison, click **Start** to run the example without a search method. This displays the plots shown in the following figure.



To see the effect of using a search method, select GPS Positive Basis Np1 in the **Search method** field in **Search** options. This sets the search method to be a pattern search using the pattern for GPS Positive basis Np1. Then click **Start** to run the genetic algorithm. This displays the following plots.

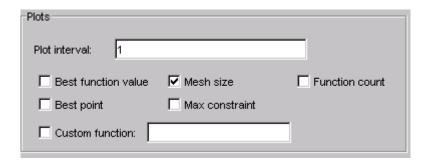


Note that using the search method reduces the total function evaluations by almost 50 percent—from 1889 to 981—and reduces the number of iterations from 250 to 78.

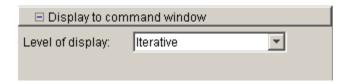
Mesh Expansion and Contraction

The **Expansion factor** and **Contraction factor** options, in **Mesh** options, control how much the mesh size is expanded or contracted at each iteration. With the default **Expansion factor** value of 2, the pattern search multiplies the mesh size by 2 after each successful poll. With the default **Contraction factor** value of 0.5, the pattern search multiplies the mesh size by 0.5 after each unsuccessful poll.

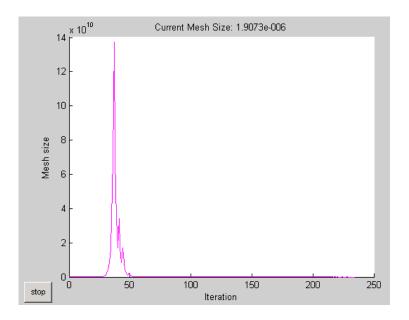
You can view the expansion and contraction of the mesh size during the pattern search by selecting **Mesh size** in the **Plots** pane.



To also display the values of the mesh size and objective function at the command line, set Level of display to Iterative in the Display to command window options.



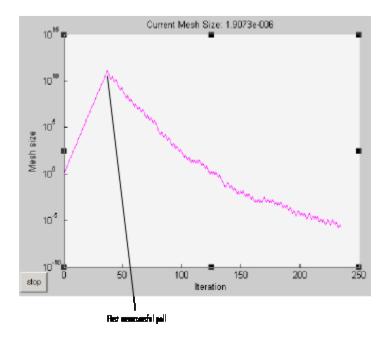
When you run the example described in "Example — A Linearly Constrained Problem" on page 5-5, the Pattern Search Tool displays the following plot.



To see the changes in mesh size more clearly, change the y-axis to logarithmic scaling as follows:

- 1 Select Axes Properties from the Edit menu in the plot window.
- $\boldsymbol{2}$ In the Properties Editor, select the \boldsymbol{Y} tab.
- 3 Set Scale to Log.

Updating these settings in the MATLAB Property Editor will show the plot in the following figure.



The first 37 iterations result in successful polls, so the mesh sizes increase steadily during this time. You can see that the first unsuccessful poll occurs at iteration 38 by looking at the command-line display for that iteration.

36	39	6.872e+010	3486	Successful Poll
37	40	1.374e+011	3486	Successful Poll
38	43	6.872e+010	3486	Refine Mesh

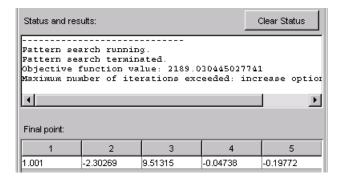
Note that at iteration 37, which is successful, the mesh size doubles for the next iteration. But at iteration 38, which is unsuccessful, the mesh size is multiplied 0.5.

To see how **Expansion factor** and **Contraction factor** affect the pattern search, make the following changes:

- Set **Expansion factor** to 3.0.
- Set Contraction factor to 0.75.

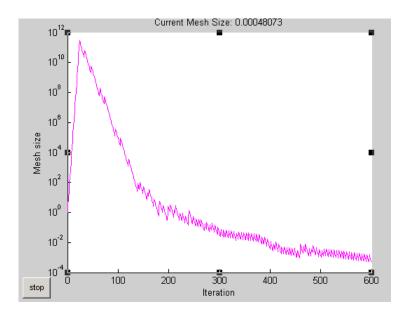
⊟ Mesh	
Initial size:	1
Max size:	Inf
Accelerator:	Off
Rotate:	On 🔻
Scale:	On 🔻
Expansion factor:	3.0
Contraction factor:	0.75

Then click **Start**. The **Status and results** pane shows that the final point is approximately the same as with the default settings of **Expansion factor** and **Contraction factor**, but that the pattern search takes longer to reach that point.



The algorithm halts because it exceeds the maximum number of iterations, whose value you can set in the **Max iteration** field in the **Stopping criteria** options. The default value is 100 times the number of variables for the objective function, which is 6 in this example.

When you change the scaling of the *y*-axis to logarithmic, the mesh size plot appears as shown in the following figure.



Note that the mesh size increases faster with **Expansion factor** set to 3.0, as compared with the default value of 2.0, and decreases more slowly with **Contraction factor** set to 0.75, as compared with the default value of 0.5.

Mesh Accelerator

The mesh accelerator can make a pattern search converge faster to an optimal point by reducing the number of iterations required to reach the mesh tolerance. When the mesh size is below a certain value, the pattern search contracts the mesh size by a factor smaller than the **Contraction factor** factor.

Note It is recommended to only use the mesh accelerator for problems in which the objective function is not too steep near the optimal point, or you might lose some accuracy. For differentiable problems, this means that the absolute value of the derivative is not too large near the solution.

To use the mesh accelerator, set **Accelerator** to 0n in the **Mesh** options. When you run the example described in "Example — A Linearly Constrained

Problem" on page 5-5, the number of iterations required to reach the mesh tolerance is 246, as compared with 270 when **Accelerator** is set to 0ff.

You can see the effect of the mesh accelerator by setting **Level of display** to Iterative in **Display to command window**. Run the example with **Accelerator** set to 0n, and then run it again with **Accelerator** set to 0ff. The mesh sizes are the same until iteration 226, but differ at iteration 227. The MATLAB Command Window displays the following lines for iterations 226 and 227 with **Accelerator** set to 0ff.

Iter	f-count	MeshSize	f(x)	Method
226	1501	6.104e-005	2189	Refine Mesh
227	1516	3.052e-005	2189	Refine Mesh

Note that the mesh size is multiplied by 0.5, the default value of **Contraction** factor.

For comparison, the Command Window displays the following lines for the same iteration numbers with **Accelerator** set to On.

Iter	f-count	MeshSize	f(x)	Method
226	1501	6.104e-005	2189	Refine Mesh
227	1516	1.526e-005	2189	Refine Mesh

In this case the mesh size is multiplied by 0.25.

Using Cache

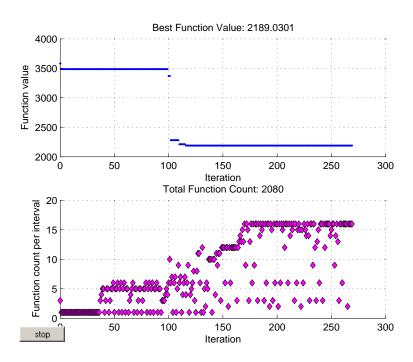
Typically, at any given iteration of a pattern search, some of the mesh points might coincide with mesh points at previous iterations. By default, the pattern search recomputes the objective function at these mesh points even though it has already computed their values and found that they are not optimal. If computing the objective function takes a long time—say, several minutes—this can make the pattern search run significantly longer.

You can eliminate these redundant computations by using a cache, that is, by storing a history of the points that the pattern search has already visited. To do so, set **Cache** to 0n in **Cache** options. At each poll, the pattern search checks to see whether the current mesh point is within a specified tolerance, **Tolerance**, of a point in the cache. If so, the search does not compute the

objective function for that point, but uses the cached function value and moves on to the next point.

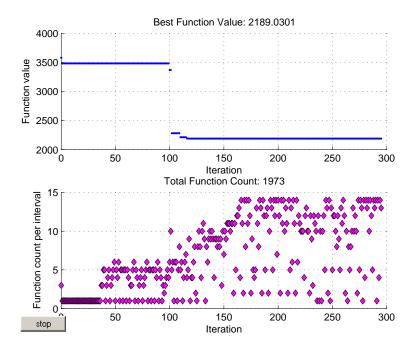
Note When **Cache** is set to 0n, the pattern search might fail to identify a point in the current mesh that improves the objective function because it is within the specified tolerance of a point in the cache. As a result, the pattern search might run for more iterations with **Cache** set to 0n than with **Cache** set to 0ff. It is generally a good idea to keep the value of **Tolerance** very small, especially for highly nonlinear objective functions.

To illustrate this, select **Best function value** and **Function count** in the **Plots** pane and run the example described in "Example — A Linearly Constrained Problem" on page 5-5 with **Cache** set to Off. After the pattern search finishes, the plots appear as shown in the following figure.



Note that the total function count is 2080.

Now, set **Cache** to 0n and run the example again. This time, the plots appear as shown in the following figure.



This time, the total function count is reduced to 1973.

Setting Tolerances for the Solver

Tolerance refers to how small a parameter, such a mesh size, can become before the search is halted or changed in some way. You can specify the value of the following tolerances:

• **Mesh tolerance** — When the current mesh size is less than the value of **Mesh tolerance**, the algorithm halts.

- **X tolerance** After a successful poll, if the distance from the previous best point to the current best point is less than the value of **X tolerance**, the algorithm halts.
- **Function tolerance** After a successful poll, if the difference between the function value at the previous best point and function value at the current best point is less than the value of **Function tolerance**, the algorithm halts.
- **Nonlinear constraint tolerance** The algorithm treats a point to be feasible if constraint violation is less than TolCon.
- **Bind tolerance** Bind tolerance applies to constrained problems and specifies how close a point must get to the boundary of the feasible region before a linear constraint is considered to be active. When a linear constraint is active, the pattern search polls points in directions parallel to the linear constraint boundary as well as the mesh points.

Usually, you should set **Bind tolerance** to be at least as large as the maximum of **Mesh tolerance**, **X tolerance**, and **Function tolerance**.

Example — Setting Bind Tolerance

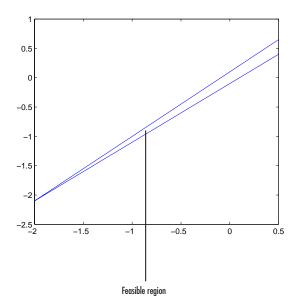
The following example illustrates of how **Bind tolerance** affects a pattern search. The example finds the minimum of

$$f(x_1, x_2) = \sqrt{x_1^2 + x_2^2}$$

subject to the constraints

$$-11x_1 + 10x_2 \le 10$$
$$10x_1 - 10x_2 \le 10$$

Note that you can compute the objective function using the function norm. The feasible region for the problem lies between the two lines in the following figure.



Running a Pattern Search with the Default Bind Tolerance

To run the example, enter psearchtool to open the Pattern Search Tool and enter the following information:

- Set **Objective function** to @(x) norm(x).
- Set **Start point** to [-1.001 -1.1].
- Select **Mesh size** in the Plots pane.
- Set Level of display to Iterative in the Display to command window options.

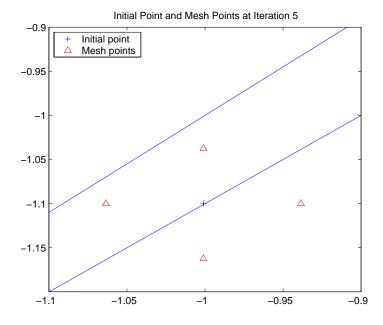
Then click **Start** to run the pattern search.

The display in the MATLAB Command Window shows that the first four polls are unsuccessful, because the mesh points do not lie in the feasible region.

Iter	f-count	MeshSize	f(x)	Method
0	1	1	1.487	Start iterations
1	1	0.5	1.487	Refine Mesh

2	1	0.25	1.487	Refine Mesh
3	1	0.125	1.487	Refine Mesh
4	1	0.0625	1.487	Refine Mesh

The pattern search contracts the mesh at each iteration until one of the mesh points lies in the feasible region. The following figure shows a close-up of the initial point and mesh points at iteration 5.



The top mesh point, which is (-1.001, -1.0375), has a smaller objective function value than the initial point, so the poll is successful.

Because the distance from the initial point to lower boundary line is less than the default value of **Bind tolerance**, which is 0.0001, the pattern search does not consider the linear constraint $10x_1 - 10x_2 \le 10$ to be active, so it does not search points in a direction parallel to the boundary line.

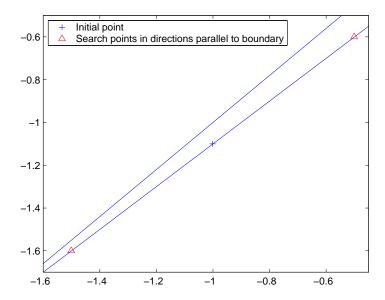
Increasing the Value of Bind Tolerance

To see the effect of bind tolerance, change **Bind tolerance** to 0.01 and run the pattern search again.

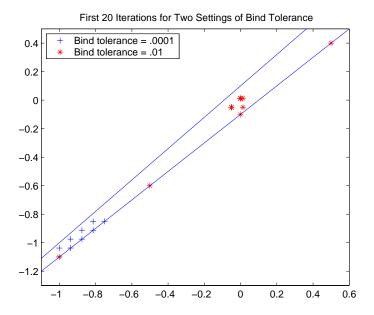
This time, the display in the MATLAB Command Window shows that the first two iterations are successful.

Iter	f-count	MeshSize	f(x)	Method
0	1	1	1.487	Start iterations
1	2	2	0.7817	Successful Poll
2	3	4	0.6395	Successful Poll

Because the distance from the initial point to the boundary is less than **Bind tolerance**, the second linear constraint is active. In this case, the pattern search polls points in directions parallel to the boundary line $10x_1 - 10x_2 = 10$, resulting in successful poll. The following figure shows the initial point with two addition search points in directions parallel to the boundary.



The following figure compares the sequences of points during the first 20 iterations of the pattern search for both settings of **Bind tolerance**.



Note that when **Bind tolerance** is set to .01, the points move toward the optimal point more quickly. The pattern search requires only 90 iterations. When **Bind tolerance** is set to .0001, the search requires 124 iterations. However, when the feasible region does not contain very acute angles, as it does in this example, increasing **Bind tolerance** can increase the number of iterations required, because the pattern search tends to poll more points.

Constrained Minimization Using patternsearch

Suppose you want to minimize the simple objective function of two variables x1 and x2,

$$\min_{x} \ f(x) = (4 - 2.1^* x_1^2 - x_1^{\frac{4}{3}})^* x_1^2 + x_1^* x_2 + (-4 + 4^* x_2^2)^* x_2^2$$

subject to the following nonlinear inequality constraints and bounds

```
\begin{array}{lll} x_1 \cdot x_2 + x_1 \cdot x_2 + 1.5 & \leq 0, \text{ (nonlinear constraint)} \\ 10 \cdot x_1 \cdot x_2 & \leq 0, & \text{ (nonlinear constraint)} \\ 0 \leq x_1 & \leq 1, & \text{ (bound)} \\ 0 \leq x_2 & \leq 13. & \text{ (bound)} \end{array}
```

Begin by creating the objective and constraint functions. First, create an M-file named simple objective.m as follows:

```
function y = simple_objective(x)
y = (4 - 2.1*x(1)^2 + x(1)^4/3)*x(1)^2 + x(1)*x(2) + (-4 + 4*x(2)^2)*x(2)^2;
```

The pattern search solver assumes the objective function will take one input x where x has as many elements as number of variables in the problem. The objective function computes the value of the function and returns that scalar value in its one return argument y.

Then create an M-file named simple_constraint.m containing the constraints:

```
function [c, ceq] = simple_constraint(x)
c = [1.5 + x(1)*x(2) + x(1) - x(2);
-x(1)*x(2) + 10];
ceq = [];
```

The pattern search solver assumes the constraint function will take one input x, where x has as many elements as the number of variables in the problem. The constraint function computes the values of all the inequality and equality constraints and returns two vectors, c and ceq, respectively.

Next, to minimize the objective function using the patternsearch function, you need to pass in a function handle to the objective function as well as specifying a start point as the second argument. Lower and upper bounds are provided as LB and UB respectively. In addition, you also need to pass a function handle to the nonlinear constraint function.

```
ObjectiveFunction = @simple_objective;
X0 = [0 0]; % Starting point
LB = [0 0]; % Lower bound
```

```
UB = [1 13]; % Upper bound
ConstraintFunction = @simple constraint;
[x,fval] = patternsearch(ObjectiveFunction,X0,[],[],[],[],...
                         LB, UB, ConstraintFunction)
Optimization terminated: mesh size less than options.TolMesh
 and constraint violation is less than options.TolCon.
x =
    0.8122
            12.3122
fval =
  9.1324e+004
```

Next, plot the results. Create an options structure using psoptimset that selects two plot functions. The first plot function psplotbestf plots the best objective function value at every iteration. The second plot function psplotmaxconstr plots the maximum constraint violation at every iteration.

Note You can also visualize the progress of the algorithm by displaying information to the Command Window using the 'Display' option.

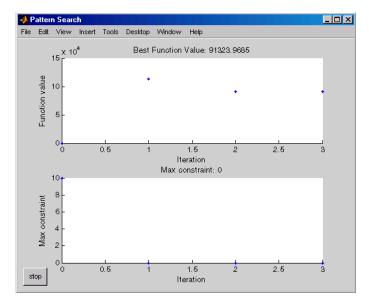
```
options = psoptimset('PlotFcns', {@psplotbestf, @psplotmaxconstr}, 'Display', 'iter');
[x,fval] = patternsearch(ObjectiveFunction,X0,[],[],[],[],LB,UB,ConstraintFunction,options)
```

			max		
Iter	f-count	f(x)	constraint	MeshSize	Method
0	1	0	10	0.8919	
1	5	113580	0	0.001	Increase penalty
2	24	91324.4	0	1e-005	Increase penalty
3	48	91324	0	1e-007	Increase penalty

Optimization terminated: mesh size less than options.TolMesh and constraint violation is less than options.TolCon.

x =
 0.8122 12.3122

fval =
 9.1324e+004



Best Objective Function Value and Maximum Constraint Violation at Each Iteration

Parameterizing Functions Called by patternsearch

In this section...

"Using Additional Parameters" on page 5-52

"Parameterizing Functions Using Anonymous Functions with patternsearch" on page 5-52

"Parameterizing a Function Using a Nested Function with patternsearch" on page 5-54

Using Additional Parameters

Sometimes you might want to write functions that are called by patternsearch that have additional parameters to the independent variable. For example, suppose you want to minimize the following function:

$$f(x) = (a - bx_1^2 + x_1^{4/3})x_1^2 + x_1x_2 + (-c + cx_2^2)x_2^2$$

for different values of a, b, and c. Because patternsearch accepts objective functions that depend only on x, you must provide the additional parameters a, b, and c to the function before calling patternsearch.

The following examples show how to parameterize the objective function, but you can use the same methods to parameterize any user-defined functions called by patternsearch, for example using a custom search method.

Parameterizing Functions Using Anonymous Functions with patternsearch

To parameterize your function, first write an M-file containing the following code:

function y = parameterfun(x,a,b,c)
y =
$$(a - b*x(1)^2 + x(1)^4/3)*x(1)^2 + x(1)*x(2) + ...$$

 $(-c + c*x(2)^2)*x(2)^2;$

Save the M- file as parameterfun.m in a directory on the MATLAB path.

Now, suppose you want to minimize the function for the parameter values a = 4, b = 2.1, and c = 4. To do so, define a function handle to an anonymous function by entering the following commands at the MATLAB prompt:

```
a = 4; b = 2.1; c = 4; % Define parameter values objfun = @(x) parameterfun(x,a,b,c); x0 = [0.5 \ 0.5];
```

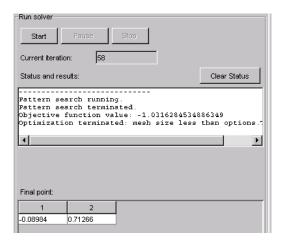
If you are using the Pattern Search Tool,

- Set **Objective function** to objfun.
- Set **Start point** to x0.

The following figure shows these settings in the Pattern Search Tool.



Next, click **Start** to run the optimization. The **Status and results** pane displays the final answer.



If you subsequently decide to change the values of a, b, and c, you must recreate the anonymous function. For example,

```
a = 3.6; b = 2.4; c = 5;
                           % Define parameter values
objfun = @(x) parameterfun(x,a,b,c);
```

Parameterizing a Function Using a Nested Function with patternsearch

As an alternative to parameterizing the objective function as an anonymous function, you can write a single M-file that

- Accepts a, b, c, and x0 as inputs.
- Contains the objective function as a nested function.
- Calls patternsearch.

The following shows the code for the M-file.

```
function [x \text{ fval}] = \text{runps}(a,b,c,x0)
[x, fval] = patternsearch(@nestedfun,x0);
% Nested function that computes the objective function
    function y = nestedfun(x)
        y = (a - b*x(1)^2 + x(1)^4/3)*x(1)^2 + x(1)*x(2) + ...
         (-c + c*x(2)^2)*x(2)^2;
    end
end
```

Note that the objective function is computed in the nested function nestedfun, which has access to the variables a, b, and c. To run the optimization, enter

```
[x fval] = runps(a,b,c,x0)
```

This returns

Optimization terminated: mesh size less than options. TolMesh.

```
x =
   -0.0898
               0.7127
fval =
   -1.0316
```

Using the Genetic Algorithm

Overview of the Genetic Algorithm Tool (p. 6-2)

Using the Genetic Algorithm from the Command Line (p. 6-23)

Genetic Algorithm Examples (p. 6-32)

Parameterizing Functions Called by ga (p. 6-65)

Provides an overview of the Genetic Algorithm Tool.

Describes how to use the genetic algorithm at the command line.

Explains how to set options for the genetic algorithm.

Explains how to write functions with additional parameters.

Overview of the Genetic Algorithm Tool

In this section...

- "Opening the Genetic Algorithm Tool" on page 6-2
- "Defining an Unconstrained Problem in the Genetic Algorithm Tool" on page 6-3
- "Running the Genetic Algorithm" on page 6-4
- "Pausing and Stopping the Algorithm" on page 6-5
- "Displaying Plots" on page 6-7
- "Example Creating a Custom Plot Function" on page 6-9
- "Reproducing Your Results" on page 6-12
- "Setting Options in the Genetic Algorithm Tool" on page 6-13
- "Importing and Exporting Options and Problems" on page 6-14
- "Example Resuming the Genetic Algorithm from the Final Population" on page 6-18
- "Generating an M-File" on page 6-22

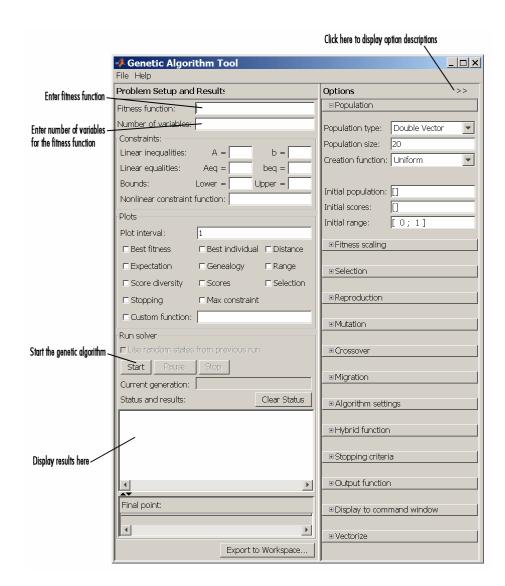
Opening the Genetic Algorithm Tool

To open the tool, enter

gatool

at the MATLAB prompt.

This opens the Genetic Algorithm Tool, as shown in the following figure.



Defining an Unconstrained Problem in the Genetic Algorithm Tool

You can define the problem you want to solve in the following two fields:

- **Fitness function** The function you want to minimize. Enter a handle to an M-file function that computes the fitness function. "Writing M-Files for Functions You Want to Optimize" on page 1-3 describes how to write the M-file.
- Number of variables The number of independent variables for the fitness function.

The following figure shows these fields for the example described in "Example: Rastrigin's Function" on page 3-7.

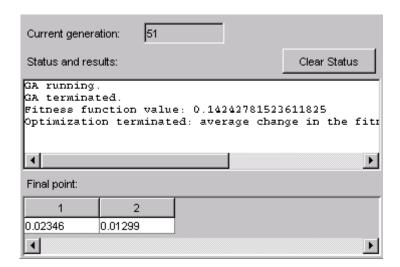


Running the Genetic Algorithm

To run the genetic algorithm, click **Start** in the **Run solver** pane. When you do so,

- The **Current generation** field displays the number of the current generation.
- The **Status and results** pane displays the message GA running.

The following figure shows the Current generation field and Status and results pane.



When the algorithm terminates, the **Status and results** pane displays

- The message GA terminated.
- The fitness function value of the best individual in the final generation
- The reason the algorithm terminated
- The coordinates of the final point

You can change many of the settings in the Genetic Algorithm Tool while the algorithm is running. Your changes are applied at the next generation. Until your changes are applied, which occurs at the start of the next generation, the **Status and results** pane displays the message Changes pending. At the start of the next generation, the pane displays the message Changes applied.

Pausing and Stopping the Algorithm

While the genetic algorithm is running, you can

 Click Pause to temporarily suspend the algorithm. To resume the algorithm using the current population at the time you paused, click Resume.

Click **Stop** to stop the algorithm. The **Status and results** pane displays the fitness function value of the best point in the current generation at the moment you clicked **Stop**.

Note If you click **Stop** and then run the genetic algorithm again by clicking **Start**, the algorithm begins with a new random initial population or with the population you specify in the **Initial population** field. If you want to restart the algorithm where it left off, use the **Pause** and **Resume** buttons.

"Example — Resuming the Genetic Algorithm from the Final Population" on page 6-18 explains what to do if you click **Stop** and later decide to resume the genetic algorithm from the final population of the last run.

Setting Stopping Criteria

The genetic algorithm uses several criteria, listed in the **Stopping criteria** options, to decide when to stop, in case you do not stop it manually by clicking **Stop.** The algorithm stops if any one of the following conditions occur:

- **Generations** The algorithm reaches the specified number of generations.
- **Time limit** The algorithm runs for the specified amount of time in seconds.
- **Fitness limit** The best fitness value in the current generation is less than or equal to the specified value.
- Stall generations The algorithm computes the specified number of generations with no improvement in the fitness function.
- Stall time limit The algorithm runs for the specified amount of time in seconds with no improvement in the fitness function.
- **Function tolerance** The algorithm runs until the cumulative change in the fitness function value over **Stall generations** is less than **Function** Tolerance.

The **Nonlinear constraint tolerance** is not used as stopping criterion. It is used to determine the feasibility with respect to nonlinear constraints.

If you want the genetic algorithm to continue running until you click **Pause** or **Stop**, you should change the default values of the following five options as follows:

- Set **Generations** to Inf.
- Set **Time limit** to Inf.
- Set **Fitness limit** to -Inf.
- Set **Stall generations** to Inf.
- Set Stall time limit to Inf.

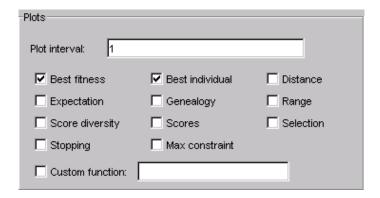
The following figure shows these settings.

⊡ Stopping criteria	
Generations:	Inf
Time limit:	Inf
Fitness limit:	-Inf
Stall generations:	Inf
Stall time limit:	Inf
Function tolerance:	1e-006
Nonlinear constraint tolerance:	1e-006

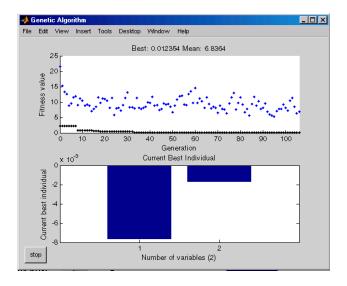
Note Do not use these settings when calling the genetic algorithm function ga at the command line. The function will not terminate until you press **Ctrl** + **C**. Instead, set **Generations** or **Time limit** to a finite number.

Displaying Plots

The **Plots** pane, shown in the following figure, enables you to display various plots of the results of the genetic algorithm.



Select the check boxes next to the plots you want to display. For example, if you select Best fitness and Best individual, and run the example described in "Example: Rastrigin's Function" on page 3-7, the tool displays plots similar to those shown in the following figure.



The upper plot displays the best and mean fitness values in each generation. The lower plot displays the coordinates of the point with the best fitness value in the current generation.

Note When you display more than one plot, clicking on any plot while the genetic algorithm is running or after the solver has completed opens a larger version of the plot in a separate window.

"Plot Options" on page 8-24 describes the types of plots you can create.

Example – Creating a Custom Plot Function

If none of the plot functions that come with the toolbox is suitable for the output you want to plot, you can write your own custom plot function, which the genetic algorithm calls at each generation to create the plot. This example shows how to create a plot function that displays the change in the best fitness value from the previous generation to the current generation.

This section covers the following topics:

- "Creating the Custom Plot Function" on page 6-9
- "Using the Plot Function" on page 6-10
- "How the Plot Function Works" on page 6-11

Creating the Custom Plot Function

To create the plot function for this example, copy and paste the following code into a new M-file in the MATLAB Editor.

```
function state = gaplotchange(options, state, flag)
% GAPLOTCHANGE Plots the logarithmic change in the best score from the
% previous generation.
%
persistent last_best % Best score in the previous generation

if(strcmp(flag,'init')) % Set up the plot
    set(gca,'xlim',[1,options.Generations],'Yscale','log');
    hold on;
    xlabel Generation
    title('Change in Best Fitness Value')
end
```

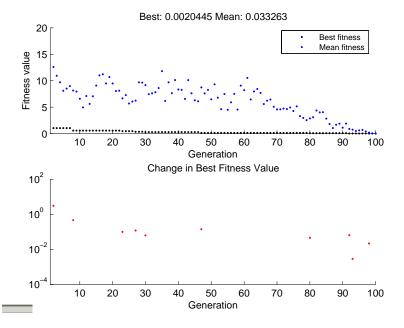
```
best = min(state.Score); % Best score in the current generation
if state.Generation == 0 % Set last best to best.
    last_best = best;
else
 change = last best - best; % Change in best score
 last best=best;
 plot(state.Generation, change, '.r');
 title(['Change in Best Fitness Value'])
end
```

Then save the M-file as gaplotchange. m in a directory on the MATLAB path.

Using the Plot Function

To use the custom plot function, select **Custom** in the **Plots** pane and enter @gaplotchange in the field to the right. To compare the custom plot with the best fitness value plot, also select **Best fitness**. Now, if you run the example described in "Example: Rastrigin's Function" on page 3-7, the tool displays plots similar to those shown in the following figure.





Note that because the scale of the *y*-axis in the lower custom plot is logarithmic, the plot only shows changes that are greater then 0. The logarithmic scale enables you to see small changes in the fitness function that the upper plot does not reveal.

How the Plot Function Works

The plot function uses information contained in the following structures, which the genetic algorithm passes to the function as input arguments:

- options The current options settings
- state Information about the current generation
- $\bullet\,$ flag String indicating the current status of the algorithm

The most important lines of the plot function are the following:

• persistent last best

Creates the persistent variable last best—the best score in the previous generation. Persistent variables are preserved over multiple calls to the plot function.

- set(gca, 'xlim',[1,options.Generations], 'Yscale', 'log'); Sets up the plot before the algorithm starts. options. Generations is the maximum number of generations.
- best = min(state.Score)

The field state. Score contains the scores of all individuals in the current population. The variable best is the minimum score. For a complete description of the fields of the structure state, see "Structure of the Plot Functions" on page 8-26.

- change = last best best The variable change is the best score at the previous generation minus the best score in the current generation.
- plot(state.Generation, change, '.r') Plots the change at the current generation, whose number is contained in state.Generation.

The code for gaplotchange contains many of the same elements as the code for gaplotbestf, the function that creates the best fitness plot.

Reproducing Your Results

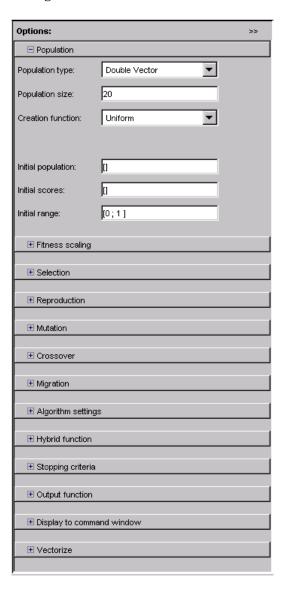
To reproduce the results of the last run of the genetic algorithm, select the **Use random states from previous run** check box. This resets the states of the random number generators used by the algorithm to their previous values. If you do not change any other settings in the Genetic Algorithm Tool, the next time you run the genetic algorithm, it returns the same results as the previous run.

Normally, you should leave Use random states from previous run unselected to get the benefit of randomness in the genetic algorithm. Select the **Use random states from previous run** check box if you want to analyze the results of that particular run or show the exact results to others. After the algorithm has run, you can clear your results using the Clear Status button in the **Run solver** settings.



Setting Options in the Genetic Algorithm Tool

You can set options for the genetic algorithm in the **Options** pane, shown in the figure below.



"Genetic Algorithm Examples" on page 6-32 describes how options settings affect the performance of the genetic algorithm. For a detailed description of all the available options, see "Genetic Algorithm Options" on page 8-23.

Setting Options as Variables in the MATLAB Workspace

You can set numerical options either directly, by typing their values in the corresponding edit box, or by entering the name of a variable in the MATLAB workspace that contains the option values. For example, you can set the **Population size** to 50 in either of the following ways:

- Enter 50 in the **Population size** field.
- Enter

```
popsize = 50
```

at the MATLAB prompt and then enter popsize in the **Population size** field.

For options whose values are large matrices or vectors, it is often more convenient to define their values as variables in the MATLAB workspace. This way, it is easy to change the entries of the matrix or vector if necessary.

Importing and Exporting Options and Problems

You can export options and problem structures from the Genetic Algorithm Tool to the MATLAB workspace, and then import them back into the tool at a later time. This enables you to save the current settings for a problem and restore them later. You can also export the options structure and use it with the genetic algorithm function ga at the command line.

You can import and export the following information:

- The problem definition, including Fitness function, Number of variables, Linear inequalities, Linear equalities, Bounds, and a **Nonlinear constraint function**
- The currently specified options
- The results of the algorithm

The following sections explain how to import and export this information:

- "Exporting Options and Problems" on page 6-15
- "Example Running ga on an Exported Problem" on page 6-16
- "Importing Options" on page 6-17
- "Importing Problems" on page 6-18
- "Resetting the Problem Fields" on page 6-18

Exporting Options and Problems

You can export options and problems to the MATLAB workspace so that you can use them at a future time in the Genetic Algorithm Tool. You can also apply the function ga using these options or problems at the command line—see "Using Options and Problems from the Genetic Algorithm Tool" on page 6-27.

To export options or problems, click the **Export to Workspace** button or select **Export to Workspace** from the **File** menu. This opens the dialog box shown in the following figure.



The dialog box provides the following options:

• To save both the problem definition and the current options settings, select **Export problem and options to a MATLAB structure named** and enter a name for the structure. Clicking **OK** saves this information to a structure in the MATLAB workspace. If you later import this structure into the Genetic Algorithm Tool, the settings for **Fitness function**, **Number of variables**, and all options settings are restored to the values they had when you exported the structure.

Note If you select Use random states from previous run in the Run **solver** pane before exporting a problem, the Genetic Algorithm Tool also saves the states of rand and randn at the beginning of the last run when you export. Then, when you import the problem and run the genetic algorithm with Use random states from previous run selected, the results of the run just before you exported the problem are reproduced exactly.

 If you want the genetic algorithm to resume from the final population of the last run before you exported the problem, select **Include information needed to resume this run**. Then, when you import the problem structure and click **Start**, the algorithm resumes from the final population of the previous run.

To restore the genetic algorithm's default behavior of generating a random initial population, delete the population in the **Initial population** field and replace it with empty brackets, [].

Note If you select Include information needed to resume this run, then selecting **Use random states from previous run** has no effect on the initial population created when you import the problem and run the genetic algorithm on it. The latter option is only intended to reproduce results from the beginning of a new run, not from a resumed run.

- To save only the options, select Export options to a MATLAB structure **named** and enter a name for the options structure.
- To save the results of the last run of the algorithm, select Export results to **a MATLAB structure named** and enter a name for the results structure.

Example — Running ga on an Exported Problem

To export the problem described in "Example: Rastrigin's Function" on page 3-7 and run the genetic algorithm function ga on it at the command line, do the following steps:

1 Click Export to Workspace.

- 2 In the Export to Workspace dialog box, enter a name for the problem structure, such as my_problem, in the Export problems and options to a MATLAB structure named field.
- **3** At the MATLAB prompt, call the function ga with my_problem as the input argument:

See "Using the Genetic Algorithm from the Command Line" on page 6-23 for more information.

Importing Options

To import an options structure from the MATLAB workspace, select **Import Options** from the **File** menu. This opens a dialog box that displays a list of the genetic algorithm options structures in the MATLAB workspace. When you select an options structure and click **Import**, the options fields in the Genetic Algorithm Tool are updated to display the values of the imported options.

You can create an options structure in either of the following ways:

- Calling gaoptimset with options as an output argument
- By exporting the current options from the Export to Workspace dialog box in the Genetic Algorithm Tool

Importing Problems

To import a problem that you previously exported from the Genetic Algorithm Tool, select **Import Problem** from the **File** menu. This opens the dialog box that displays a list of the genetic algorithm problem structures in the MATLAB workspace. When you select a problem structure and click **OK**, the following fields are updated in the Genetic Algorithm Tool:

- Fitness function
- Number of variables
- Linear inequalities
- Linear equalities
- Bounds
- Nonlinear constraint function
- The fields specified in the **Options** panel

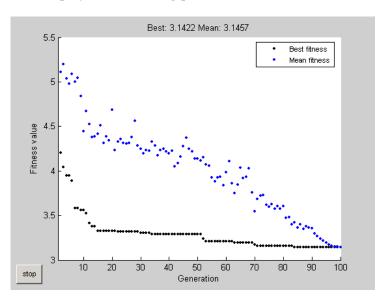
Resetting the Problem Fields

To reset or clear a problem you previously ran in the Genetic Algorithm Tool, select **New Problem** from the **File** menu. This sets all the fields in the Genetic Algorithm Tool to the default options.

Example — Resuming the Genetic Algorithm from the Final Population

The following example shows how export a problem so that when you import it and click Start, the genetic algorithm resumes from the final population saved with the exported problem. To run the example, enter the following information in the Genetic Algorithm Tool:

- Set Fitness function to @ackleyfon, which computes Ackley's function, a test function provided with the toolbox.
- Set Number of variables to 10.
- Select **Best fitness** in the **Plots** pane.
- · Click Start.



This displays the following plot.

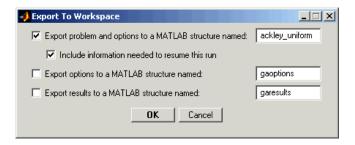
Suppose you want to experiment by running the genetic algorithm with other options settings, and then later restart this run from its final population with its current options settings. You can do this using the following steps:

1 Click Export to Workspace.

- **2** In the dialog box that appears,
 - Select Export problem and options to a MATLAB structure named.
 - Enter a name for the problem and options, such as ackley_uniform, in the text field.
 - Select Include information needed to resume this run.

The dialog box should now appear as in the following figure.





3 Click OK.

This exports the problem and options to a structure in the MATLAB workspace. You can view the structure in the MATLAB Command Window by entering

```
ackley uniform
ackley uniform =
      fitnessfcn: @ackleyfcn
           nvars: 10
      LB: []
      UB: []
           Aineq: []
           bineq: []
     Aeq: []
     beq: []
         nonlcon: []
         options: [1x1 struct]
```

After running the genetic algorithm with different options settings or even a different fitness function, you can restore the problem as follows:

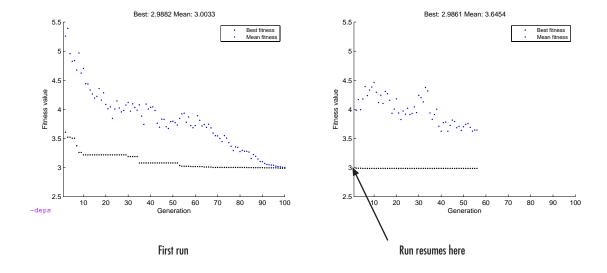
1 Select **Import Problem** from the **File** menu. This opens the dialog box shown in the following figure.



2 Select ackley_uniform.

3 Click Import.

This sets the **Initial population** and **Initial scores** fields in the **Population** panel to the final population of the run before you exported the problem. All other options are restored to their setting during that run. When you click **Start**, the genetic algorithm resumes from the saved final population. The following figure shows the best fitness plots from the original run and the restarted run.



Note If, after running the genetic algorithm with the imported problem, you want to restore the genetic algorithm's default behavior of generating a random initial population, delete the population in the **Initial population** field.

Generating an M-File

To create an M-file that runs the genetic algorithm, using the fitness function and options you specify in the Genetic Algorithm Tool, select Generate M-File from the File menu and save the M-file in a directory on the MATLAB path. Calling this M-file at the command line returns the same results as the Genetic Algorithm Tool, using the fitness function and options settings that were in place when you generated the M-file.

Using the Genetic Algorithm from the Command Line

In this section...

- "Running ga with the Default Options" on page 6-23
- "Setting Options for ga at the Command Line" on page 6-24
- "Using Options and Problems from the Genetic Algorithm Tool" on page 6-27
- "Reproducing Your Results" on page 6-27
- "Resuming ga from the Final Population of a Previous Run" on page 6-29
- "Running ga from an M-File" on page 6-29

Running ga with the Default Options

To run the genetic algorithm with the default options, call ga with the syntax

```
[x fval] = ga(@fitnessfun, nvars)
```

The input arguments to ga are

- @fitnessfun A function handle to the M-file that computes the fitness function. "Writing M-Files for Functions You Want to Optimize" on page 1-3 explains how to write this M-file.
- nvars The number of independent variables for the fitness function.

The output arguments are

- x The final point
- fval The value of the fitness function at x

For a description of additional input and output arguments, see the reference page for ga.

You can run the example described in "Example: Rastrigin's Function" on page 3-7 from the command line by entering

```
[x \text{ fval}] = ga(@rastriginsfcn, 2)
```

This returns

```
x =
    0.0027
              -0.0052
fval =
    0,0068
```

Additional Output Arguments

To get more information about the performance of the genetic algorithm, you can call ga with the syntax

```
[x fval exitflag output population scores] = ga(@fitnessfcn, nvars)
```

Besides x and fval, this function returns the following additional output arguments:

- exitflag Integer value corresponding to the reason the algorithm terminated
- output Structure containing information about the performance of the algorithm at each generation
- population Final population
- scores Final scores

See the ga reference page for more information about these arguments.

Setting Options for ga at the Command Line

You can specify any of the options that are available in the Genetic Algorithm Tool by passing an options structure as an input argument to ga using the syntax

```
[x \text{ fval}] = ga(@fitnessfun, nvars, [],[],[],[],[],[],[],options)
```

This syntax does not specify any linear equality, linear inequality, or nonlinear constraints.

You create the options structure using the function gaoptimset.

```
options = gaoptimset
```

This returns the structure options with the default values for its fields.

```
options =
        PopulationType: 'doubleVector'
          PopInitRange: [2x1 double]
        PopulationSize: 20
            EliteCount: 2
     CrossoverFraction: 0.8000
    MigrationDirection: 'forward'
     MigrationInterval: 20
     MigrationFraction: 0.2000
           Generations: 100
             TimeLimit: Inf
          FitnessLimit: -Inf
         StallGenLimit: 50
        StallTimeLimit: 20
                TolFun: 1.0000e-006
                TolCon: 1.0000e-006
     InitialPopulation: []
         InitialScores: []
        InitialPenalty: 10
         PenaltyFactor: 100
          PlotInterval: 1
           CreationFcn: @gacreationuniform
     FitnessScalingFcn: @fitscalingrank
          SelectionFcn: @selectionstochunif
          CrossoverFcn: @crossoverscattered
           MutationFcn: @mutationgaussian
             HybridFcn: []
               Display: 'final'
              PlotFcns: []
            OutputFcns: []
            Vectorized: 'off'
```

The function ga uses these default values if you do not pass in options as an input argument.

The value of each option is stored in a field of the options structure, such as options. PopulationSize. You can display any of these values by entering options followed by the name of the field. For example, to display the size of the population for the genetic algorithm, enter

```
options.PopulationSize
ans =
    20
```

To create an options structure with a field value that is different from the default — for example to set PopulationSize to 100 instead of its default value 20 — enter

```
options = gaoptimset('PopulationSize', 100)
```

This creates the options structure with all values set to their defaults except for PopulationSize, which is set to 100.

If you now enter,

```
ga(@fitnessfun,nvars,[],[],[],[],[],[],[],options)
```

ga runs the genetic algorithm with a population size of 100.

If you subsequently decide to change another field in the options structure, such as setting PlotFons to @gaplotbestf, which plots the best fitness function value at each generation, call gaoptimset with the syntax

```
options = gaoptimset(options, 'PlotFcns', @plotbestf)
```

This preserves the current values of all fields of options except for PlotFcns, which is changed to @plotbestf. Note that if you omit the input argument options, gaoptimset resets PopulationSize to its default value 20.

You can also set both PopulationSize and PlotFcns with the single command

```
options = gaoptimset('PopulationSize',100,'PlotFcns',@plotbestf)
```

Using Options and Problems from the Genetic Algorithm Tool

As an alternative to creating an options structure using gaoptimset, you can set the values of options in the Genetic Algorithm Tool and then export the options to a structure in the MATLAB workspace, as described in "Exporting Options and Problems" on page 6-15. If you export the default options in the Genetic Algorithm Tool, the resulting structure options has the same settings as the default structure returned by the command

```
options = gaoptimset
```

If you export a problem structure, ga_problem, from the Genetic Algorithm Tool, you can apply ga to it using the syntax

```
[x fval] = ga(ga problem)
```

The problem structure contains the following fields:

- fitnessfcn Fitness function
- nvars Number of variables for the problem
- Aineq Matrix for inequality constraints
- Bineq Vector for inequality constraints
- ullet Aeq Matrix for equality constraints
- ullet Beq Vector for equality constraints
- LB Lower bound on x
- \bullet UB Upper bound on x
- nonlcon Nonlinear constraint function
- options Options structure

Reproducing Your Results

Because the genetic algorithm is stochastic—that is, it makes random choices—you get slightly different results each time you run the genetic algorithm. The algorithm uses the MATLAB uniform and normal random number generators, rand and randn, to makes random choices at each iteration. Each time ga calls rand and randn, their states are changed, so that

the next time they are called, they return different random numbers. This is why the output of ga differs each time you run it.

If you need to reproduce your results exactly, you can call ga with an output argument that contains the current states of rand and randn and then reset the states to these values before running ga again. For example, to reproduce the output of ga applied to Rastrigin's function, call ga with the syntax

```
[x fval exitflag output] = ga(@rastriginsfcn, 2);
```

Suppose the results are

```
x =
              -0.0052
    0.0027
fval =
    0.0068
```

The states of rand and randn are stored in the first two fields of output.

```
output =
      randstate: [35x1 double]
     randnstate: [2x1 double]
    generations: 100
      funccount: 2000
        message: [1x64 char]
```

Then, reset the states, by entering

```
rand('twister', output.randstate);
randn('state', output.randnstate);
```

If you now run ga a second time, you get the same results.

Note If you do not need to reproduce your results, it is better not to set the states of rand and randn, so that you get the benefit of the randomness in the genetic algorithm.



Resuming ga from the Final Population of a Previous Run

By default, ga creates a new initial population each time you run it. However, you might get better results by using the final population from a previous run as the initial population for a new run. To do so, you must have saved the final population from the previous run by calling ga with the syntax

```
[x, fval, exitflag, output, final pop] = ga(@fitnessfcn, nvars);
```

The last output argument is the final population. To run ga using final_pop as the initial population, enter

```
options = gaoptimset('InitialPop', final_pop);
[x, fval, exitflag, output, final_pop2] = ...
ga(@fitnessfcn, nvars,[],[],[],[],[],[],[],options);
```

You can then use final_pop2, the final population from the second run, as the initial population for a third run.

Running ga from an M-File

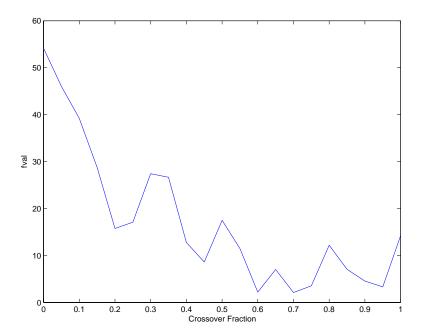
The command-line interface enables you to run the genetic algorithm many times, with different options settings, using an M-file. For example, you can run the genetic algorithm with different settings for **Crossover fraction** to see which one gives the best results. The following code runs the function ga 21 times, varying options. CrossoverFraction from 0 to 1 in increments of 0.05, and records the results.

```
options = gaoptimset('Generations',300);
rand('twister', 71); % These two commands are only included to
randn('state', 59); % make the results reproducible.
record=[];
for n=0:.05:1
  options = gaoptimset(options,'CrossoverFraction', n);
  [x fval]=ga(@rastriginsfcn, 10,[],[],[],[],[],[],[],options);
  record = [record; fval];
end
```

You can plot the values of fval against the crossover fraction with the following commands:

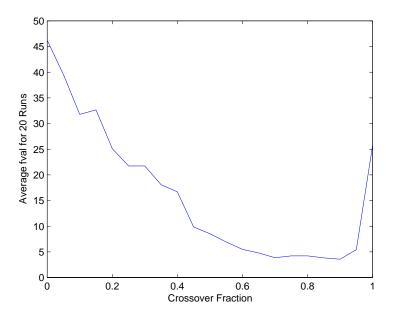
```
plot(0:.05:1, record);
xlabel('Crossover Fraction');
ylabel('fval')
```

The following plot appears.



The plot indicates that you get the best results by setting options. Crossover Fraction to a value somewhere between 0.6 and 0.95.

You can get a smoother plot of fval as a function of the crossover fraction by running ga 20 times and averaging the values of fval for each crossover fraction. The following figure shows the resulting plot.



The plot narrows the range of best choices for options.CrossoverFraction to values between 0.7 and 0.9.



Genetic Algorithm Examples

In this section...

- "Improving Your Results" on page 6-32
- "Population Diversity" on page 6-32
- "Fitness Scaling" on page 6-37
- "Selection" on page 6-40
- "Reproduction Options" on page 6-41
- "Mutation and Crossover" on page 6-41
- "Setting the Amount of Mutation" on page 6-42
- "Setting the Crossover Fraction" on page 6-44
- "Comparing Results for Varying Crossover Fractions" on page 6-48
- "Global vs. Local Minima" on page 6-50
- "Using a Hybrid Function" on page 6-54
- "Setting the Maximum Number of Generations" on page 6-57
- "Vectorizing the Fitness Function" on page 6-58
- "Constrained Minimization Using ga" on page 6-59

Improving Your Results

To get the best results from the genetic algorithm, you usually need to experiment with different options. Selecting the best options for a problem involves trial and error. This section describes some ways you can change options to improve results. For a complete description of the available options, see "Importing and Exporting Options and Problems" on page 5-15.

Population Diversity

One of the most important factors that determines the performance of the genetic algorithm performs is the *diversity* of the population. If the average distance between individuals is large, the diversity is high; if the average distance is small, the diversity is low. Getting the right amount of diversity is a matter of trial and error. If the diversity is too high or too low, the genetic algorithm might not perform well.

This section explains how to control diversity by setting the **Initial range** of the population. "Setting the Amount of Mutation" on page 6-42 describes how the amount of mutation affects diversity.

This section also explains how to set the population size.

Example — Setting the Initial Range

By default, the Genetic Algorithm Tool creates a random initial population using the creation function. You can specify the range of the vectors in the initial population in the **Initial range** field in **Population** options.

Note The initial range only restricts the range of the points in the initial population by specifying the lower and upper bounds. Subsequent generations can contain points whose entries do not lie in the initial range. Additionally, the upper and lower bounds can be adjusted by setting the **Bounds** fields in the **Constraints** panel.

If you know approximately where the solution to a problem lies, you should specify the initial range so that it contains your guess for the solution. However, the genetic algorithm can find the solution even if it does not lie in the initial range, provided that the populations have enough diversity.

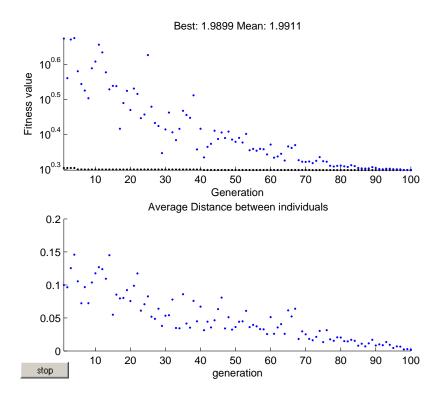
The following example shows how the initial range affects the performance of the genetic algorithm. The example uses Rastrigin's function, described in "Example: Rastrigin's Function" on page 3-7. The minimum value of the function is 0, which occurs at the origin.

To run the example, make the following settings in the Genetic Algorithm Tool:

- Set **Fitness function** to @rastriginsfcn.
- Set Number of variables to 2.
- Select **Best fitness** in the **Plots** pane.
- Select **Distance** in the **Plots** pane.

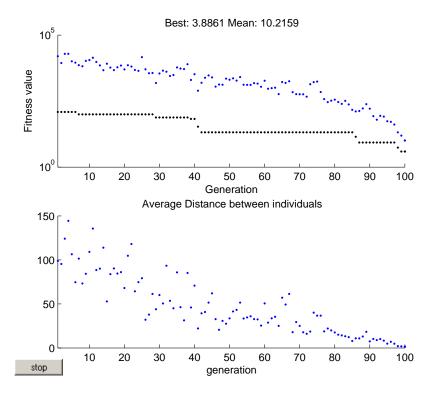
• Set **Initial range** to [1; 1.1].

Then click **Start**. The genetic algorithm returns the best fitness function value of approximately 2 and displays the plots in the following figure.



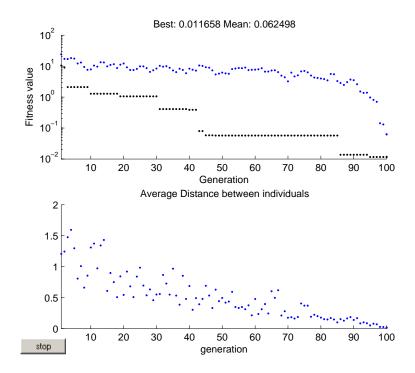
The upper plot, which displays the best fitness at each generation, shows little progress in lowering the fitness value. The lower plot shows the average distance between individuals at each generation, which is a good measure of the diversity of a population. For this setting of initial range, there is too little diversity for the algorithm to make progress.

Next, try setting **Initial range** to [1; 100] and running the algorithm. The genetic algorithm returns the best fitness value of approximately 3.9 and displays the following plots.



This time, the genetic algorithm makes progress, but because the average distance between individuals is so large, the best individuals are far from the optimal solution.

Finally, set $Initial\ range\ to\ [1;\ 2]$ and run the genetic algorithm. This returns the best fitness value of approximately .012 and displays the following plots.



The diversity in this case is better suited to the problem, so the genetic algorithm returns a much better result than in the previous two cases.

Setting the Population Size

The Population size field in Population options determines the size of the population at each generation. Increasing the population size enables the genetic algorithm to search more points and thereby obtain a better result. However, the larger the population size, the longer the genetic algorithm takes to compute each generation.

Note You should set **Population size** to be at least the value of **Number** of variables, so that the individuals in each population span the space being searched.

You can experiment with different settings for **Population size** that return good results without taking a prohibitive amount of time to run.

Fitness Scaling

Fitness scaling converts the raw fitness scores that are returned by the fitness function to values in a range that is suitable for the selection function. The selection function uses the scaled fitness values to select the parents of the next generation. The selection function assigns a higher probability of selection to individuals with higher scaled values.

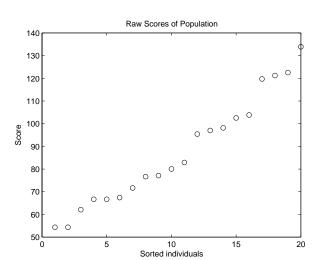
The range of the scaled values affects the performance of the genetic algorithm. If the scaled values vary too widely, the individuals with the highest scaled values reproduce too rapidly, taking over the population gene pool too quickly, and preventing the genetic algorithm from searching other areas of the solution space. On the other hand, if the scaled values vary only a little, all individuals have approximately the same chance of reproduction and the search will progress very slowly.

The default fitness scaling option, Rank, scales the raw scores based on the rank of each individual instead of its score. The rank of an individual is its position in the sorted scores: the rank of the most fit individual is 1, the next most fit is 2, and so on. The rank scaling function assigns scaled values so that

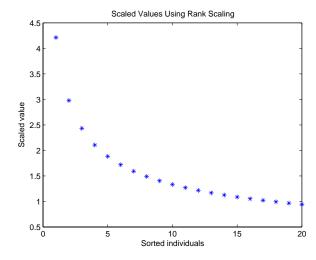
- The scaled value of an individual with rank n is proportional to $1/(\sqrt{n})$.
- The sum of the scaled values over the entire population equals the number of parents needed to create the next generation.

Rank fitness scaling removes the effect of the spread of the raw scores.

The following plot shows the raw scores of a typical population of 20 individuals, sorted in increasing order.



The following plot shows the scaled values of the raw scores using rank scaling.



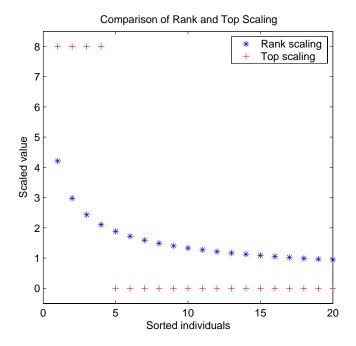
Because the algorithm minimizes the fitness function, lower raw scores have higher scaled values. Also, because rank scaling assigns values that depend

only on an individual's rank, the scaled values shown would be the same for any population of size 20 and number of parents equal to 32.

Comparing Rank and Top Scaling

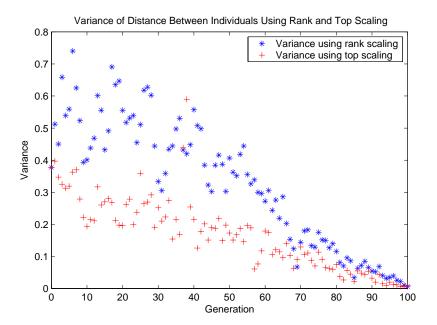
To see the effect of scaling, you can compare the results of the genetic algorithm using rank scaling with one of the other scaling options, such as Top. By default, top scaling assigns 40 percent of the fittest individuals to the same scaled value and assigns the rest of the individuals to value 0. Using the default selection function, only 40 percent of the fittest individuals can be selected as parents.

The following figure compares the scaled values of a population of size 20 with number of parents equal to 32 using rank and top scaling.



Because top scaling restricts parents to the fittest individuals, it creates less diverse populations than rank scaling. The following plot compares the

variances of distances between individuals at each generation using rank and top scaling.



Selection

The selection function chooses parents for the next generation based on their scaled values from the fitness scaling function. An individual can be selected more than once as a parent, in which case it contributes its genes to more than one child. The default selection option, Stochastic uniform, lays out a line in which each parent corresponds to a section of the line of length proportional to its scaled value. The algorithm moves along the line in steps of equal size. At each step, the algorithm allocates a parent from the section it lands on.

A more deterministic selection option is Remainder, which performs two steps:

 In the first step, the function selects parents deterministically according to the integer part of the scaled value for each individual. For example, if an individual's scaled value is 2.3, the function selects that individual twice as a parent.

• In the second step, the selection function selects additional parents using the fractional parts of the scaled values, as in stochastic uniform selection. The function lays out a line in sections, whose lengths are proportional to the fractional part of the scaled value of the individuals, and moves along the line in equal steps to select the parents.

Note that if the fractional parts of the scaled values all equal 0, as can occur using Top scaling, the selection is entirely deterministic.

Reproduction Options

Reproduction options control how the genetic algorithm creates the next generation. The options are

• **Elite count** — The number of individuals with the best fitness values in the current generation that are guaranteed to survive to the next generation. These individuals are called *elite children*. The default value of **Elite count** is 2.

When **Elite count** is at least 1, the best fitness value can only decrease from one generation to the next. This is what you want to happen, since the genetic algorithm minimizes the fitness function. Setting **Elite count** to a high value causes the fittest individuals to dominate the population, which can make the search less effective.

• **Crossover fraction** — The fraction of individuals in the next generation, other than elite children, that are created by crossover. "Setting the Crossover Fraction" on page 6-44 describes how the value of **Crossover fraction** affects the performance of the genetic algorithm.

Mutation and Crossover

The genetic algorithm uses the individuals in the current generation to create the children that make up the next generation. Besides elite children, which correspond to the individuals in the current generation with the best fitness values, the algorithm creates

- Crossover children by selecting vector entries, or genes, from a pair of individuals in the current generation and combines them to form a child
- Mutation children by applying random changes to a single individual in the current generation to create a child

Both processes are essential to the genetic algorithm. Crossover enables the algorithm to extract the best genes from different individuals and recombine them into potentially superior children. Mutation adds to the diversity of a population and thereby increases the likelihood that the algorithm will generate individuals with better fitness values.

See "Creating the Next Generation" on page 3-21 for an example of how the genetic algorithm applies mutation and crossover.

You can specify how many of each type of children the algorithm creates as follows:

- Elite count, in Reproduction options, specifies the number of elite
- Crossover fraction, in Reproduction options, specifies the fraction of the population, other than elite children, that are crossover children.

For example, if the **Population size** is 20, the **Elite count** is 2, and the Crossover fraction is 0.8, the numbers of each type of children in the next generation are as follows:

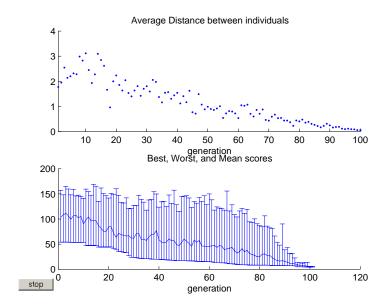
- There are two elite children.
- There are 18 individuals other than elite children, so the algorithm rounds 0.8*18 = 14.4 to 14 to get the number of crossover children.
- The remaining four individuals, other than elite children, are mutation children.

Setting the Amount of Mutation

The genetic algorithm applies mutations using the option that you specify on the Mutation function pane. The default mutation option, Gaussian, adds a random number, or *mutation*, chosen from a Gaussian distribution, to each entry of the parent vector. Typically, the amount of mutation, which is proportional to the standard deviation of the distribution, decreases at each new generation. You can control the average amount of mutation that the algorithm applies to a parent in each generation through the **Scale** and **Shrink** options:

- **Scale** controls the standard deviation of the mutation at the first generation, which is **Scale** multiplied by the range of the initial population, which you specify by the **Initial range** option.
- **Shrink** controls the rate at which the average amount of mutation decreases. The standard deviation decreases linearly so that its final value equals 1 **Shrink** times its initial value at the first generation. For example, if **Shrink** has the default value of 1, then the amount of mutation decreases to 0 at the final step.

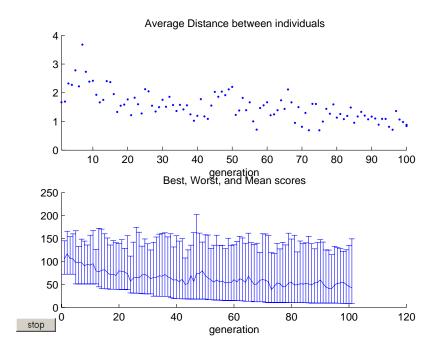
You can see the effect of mutation by selecting the plot options **Distance** and **Range**, and then running the genetic algorithm on a problem such as the one described in "Example: Rastrigin's Function" on page 3-7. The following figure shows the plot.



The upper plot displays the average distance between points in each generation. As the amount of mutation decreases, so does the average distance between individuals, which is approximately 0 at the final generation. The lower plot displays a vertical line at each generation, showing the range from the smallest to the largest fitness value, as well as mean fitness value. As the amount of mutation decreases, so does the range. These plots show

that reducing the amount of mutation decreases the diversity of subsequent generations.

For comparison, the following figure shows the plots for **Distance** and **Range** when you set Shrink to 0.5.



With **Shrink** set to 0.5, the average amount of mutation decreases by a factor of 1/2 by the final generation. As a result, the average distance between individuals decreases by approximately the same factor.

Setting the Crossover Fraction

The Crossover fraction field, in the Reproduction options, specifies the fraction of each population, other than elite children, that are made up of crossover children. A crossover fraction of 1 means that all children other than elite individuals are crossover children, while a crossover fraction of 0 means that all children are mutation children. The following example show that neither of these extremes is an effective strategy for optimizing a function.

The example uses the fitness function whose value at a point is the sum of the absolute values of the coordinates at the points. That is,

$$f(x_1, x_2, ..., x_n) = |x_1| + |x_2| + ... + |x_n|$$

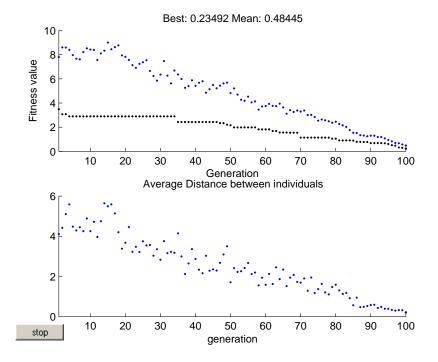
You can define this function as an anonymous function by setting **Fitness** function to

```
@(x) sum(abs(x))
```

To run the example,

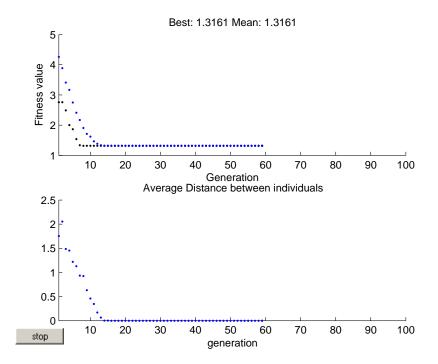
- Set **Fitness function** to @(x) sum(abs(x)).
- Set Number of variables to 10.
- Set Initial range to [-1; 1].
- Select Best fitness and Distance in the Plots pane.

Run the example with the default value of 0.8 for **Crossover fraction**. This returns the best fitness value of approximately 0.2 and displays the following plots.



Crossover Without Mutation

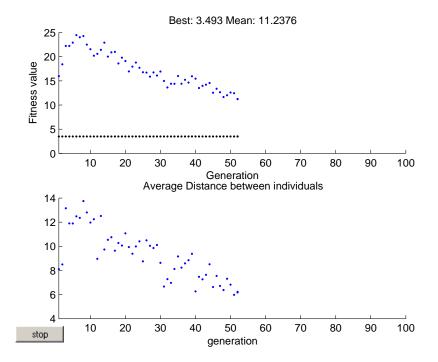
To see how the genetic algorithm performs when there is no mutation, set Crossover fraction to 1.0 and click Start. This returns the best fitness value of approximately 1.3 and displays the following plots.



In this case, the algorithm selects genes from the individuals in the initial population and recombines them. The algorithm cannot create any new genes because there is no mutation. The algorithm generates the best individual that it can using these genes at generation number 8, where the best fitness plot becomes level. After this, it creates new copies of the best individual, which are then are selected for the next generation. By generation number 17, all individuals in the population are the same, namely, the best individual. When this occurs, the average distance between individuals is 0. Since the algorithm cannot improve the best fitness value after generation 8, it stalls after 50 more generations, because **Stall generations** is set to 50.

Mutation Without Crossover

To see how the genetic algorithm performs when there is no crossover, set **Crossover fraction** to 0 and click **Start**. This returns the best fitness value of approximately 3.5 and displays the following plots.



In this case, the random changes that the algorithm applies never improve the fitness value of the best individual at the first generation. While it improves the individual genes of other individuals, as you can see in the upper plot by the decrease in the mean value of the fitness function, these improved genes are never combined with the genes of the best individual because there is no crossover. As a result, the best fitness plot is level and the algorithm stalls at generation number 50.

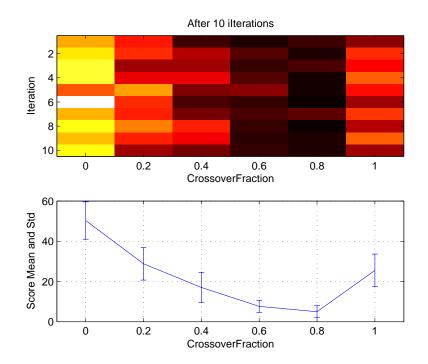
Comparing Results for Varying Crossover Fractions

The demo deterministicstudy.m, which is included in the toolbox, compares the results of applying the genetic algorithm to Rastrigin's function with Crossover fraction set to 0, .2, .4, .6, .8, and 1. The demo runs for 10 generations. At each generation, the demo plots the means and standard deviations of the best fitness values in all the preceding generations, for each value of the **Crossover fraction**.

To run the demo, enter

deterministicstudy

at the MATLAB prompt. When the demo is finished, the plots appear as in the following figure.



The lower plot shows the means and standard deviations of the best fitness values over 10 generations, for each of the values of the crossover fraction. The upper plot shows a color-coded display of the best fitness values in each generation.

For this fitness function, setting **Crossover fraction** to 0.8 yields the best result. However, for another fitness function, a different setting for **Crossover fraction** might yield the best result.

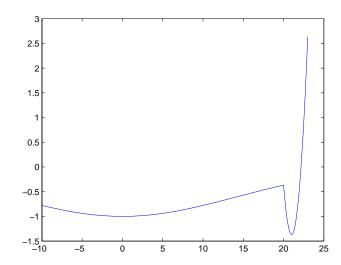
Global vs. Local Minima

Sometimes the goal of an optimization is to find the global minimum or maximum of a function—a point where the function value is smaller or larger at any other point in the search space. However, optimization algorithms sometimes return a local minimum—a point where the function value is smaller than at nearby points, but possibly greater than at a distant point in the search space. The genetic algorithm can sometimes overcome this deficiency with the right settings.

As an example, consider the following function

$$f(x) = \begin{cases} -\exp(-\left(\frac{x}{20}\right)^2) & \text{for } x \le 20\\ -\exp(-1) + (x - 20)(x - 22) & \text{for } x > 20 \end{cases}$$

The following figure shows a plot of the function.



The function has two local minima, one at x = 0, where the function value is -1, and the other at x = 21, where the function value is -1 - 1/e. Since the latter value is smaller, the global minimum occurs at x = 21.

Running the Genetic Algorithm on the Example

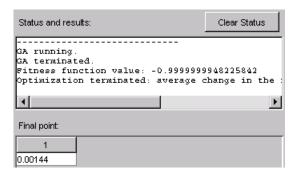
To run the genetic algorithm on this example,

1 Copy and paste the following code into a new M-file in the MATLAB Editor.

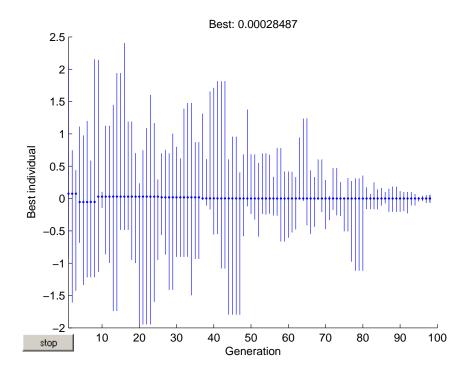
```
function y = two_min(x)
if x<=20
    y = -exp(-(x/20).^2);
else
    y = -exp(-1)+(x-20)*(x-22);
end</pre>
```

- **2** Save the file as two min.m in a directory on the MATLAB path.
- **3** In the Genetic Algorithm Tool,
 - Set **Fitness function** to @two min.
 - Set Number of variables to 1.
 - · Click Start.

The genetic algorithm returns a point very close to the local minimum at x = 0.

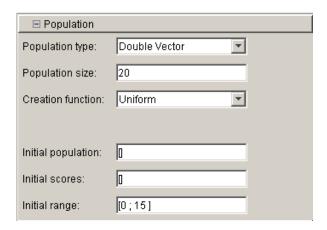


The following custom plot shows why the algorithm finds the local minimum rather than the global minimum. The plot shows the range of individuals in each generation and the best individual.

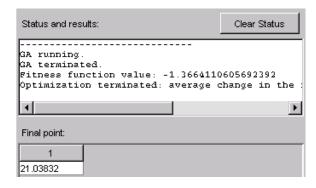


Note that all individuals are between -2 and 2.5. While this range is larger than the default **Initial range** of [0;1], due to mutation, it is not large enough to explore points near the global minimum at x = 21.

One way to make the genetic algorithm explore a wider range of points—that is, to increase the diversity of the populations—is to increase the Initial range. The Initial range does not have to include the point x = 21, but it must be large enough so that the algorithm generates individuals near x = 21. Set **Initial range** to [0;15] as shown in the following figure.



Then click **Start**. The genetic algorithm returns a point very close to 21.



This time, the custom plot shows a much wider range of individuals. By the second generation there are individuals greater than 21, and by generation 12, the algorithm finds a best individual that is approximately equal to 21.

Using a Hybrid Function

20

30

40

50

Generation

-60

stop

10

A hybrid function is an optimization function that runs after the genetic algorithm terminates in order to improve the value of the fitness function. The hybrid function uses the final point from the genetic algorithm as its initial point. You can specify a hybrid function in **Hybrid function** options.

60

70

80

90

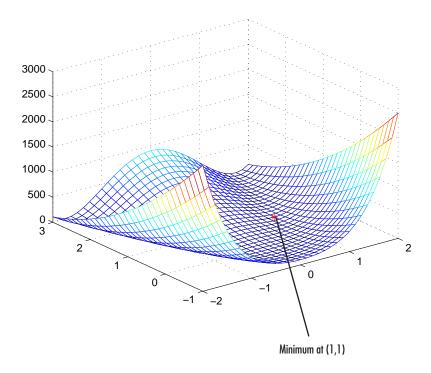
100

This example uses the function fminunc, an unconstrained minimization function in the Optimization Toolbox. The example first runs the genetic algorithm to find a point close to the optimal point and then uses that point as the initial point for fminunc.

The example finds the minimum of Rosenbrock's function, which is defined by

$$f(x_1, x_2) = 100(x_2 - x_1^2)^2 + (1 - x_1)^2$$

The following figure shows a plot of Rosenbrock's function.



The toolbox provides an M-file, dejong2fcn.m, that computes the function. To see a demo of this example, enter

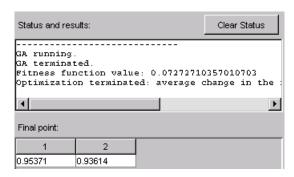
hybriddemo

at the MATLAB prompt.

To explore the example, first enter gatool to open the Genetic Algorithm Tool and enter the following settings:

- Set Fitness function to @dejong2fcn.
- Set Number of variables to 2.
- Set **Population size** to 10.

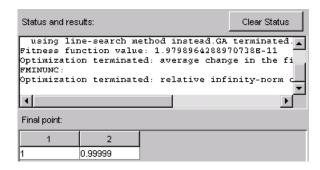
Before adding a hybrid function, try running the genetic algorithm by itself, by clicking **Start**. The genetic algorithm displays the following results in the Status and results pane.



The final point is close to the true minimum at (1, 1). You can improve this result by setting **Hybrid function** to fminunc in the **Hybrid function** options.



The function fminunc uses the final point of one run, or step, of the genetic algorithm as the initial point of the next step to return a more accurate result when the genetic algorithm terminates, as shown in the Status and results pane.



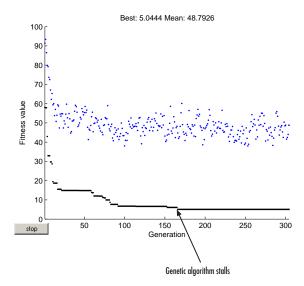
Setting the Maximum Number of Generations

The **Generations** option in **Stopping criteria** determines the maximum number of generations the genetic algorithm runs for—see "Stopping Conditions for the Algorithm" on page 3-23. Increasing the **Generations** option often improves the final result.

As an example, change the settings in the Genetic Algorithm Tool as follows:

- Set **Fitness function** to @rastriginsfcn.
- Set Number of variables to 10.
- Select **Best fitness** in the **Plots** pane.
- Set **Generations** to Inf.
- Set Stall generations to Inf.
- Set Stall time to Inf.

Then run the genetic algorithm for approximately 300 generations and click **Stop**. The following figure shows the resulting best fitness plot after 300 generations.



Note that the algorithm *stalls* at approximately generation number 170—that is, there is no immediate improvement in the fitness function after generation 170. If you restore **Stall generations** to its default value of 50, the algorithm would terminate at approximately generation number 230. If the genetic algorithm stalls repeatedly with the current setting for **Generations**, you can try increasing both the **Generations** and **Stall generations** options to improve your results. However, changing other options might be more effective.

Note When **Mutation function** is set to Gaussian, increasing the value of **Generations** might actually worsen the final result. This can occur because the Gaussian mutation function decreases the average amount of mutation in each generation by a factor that depends on the value specified in **Generations**. Consequently, the setting for **Generations** affects the behavior of the algorithm.

Vectorizing the Fitness Function

The genetic algorithm usually runs faster if you *vectorize* the fitness function. This means that the genetic algorithm only calls the fitness function once, but expects the fitness function to compute the fitness for all individuals in the current population at once. To vectorize the fitness function,

 Write the M-file that computes the function so that it accepts a matrix with arbitrarily many rows, corresponding to the individuals in the population.
 For example, to vectorize the function

$$f(x_1, x_2) = x_1^2 - 2x_1x_2 + 6x_1 + x_2^2 - 6x_2$$

write the M-file using the following code:

```
z = x(:,1).^2 - 2*x(:,1).*x(:,2) + 6*x(:,1) + x(:,2).^2 - 6*x(:,2);
```

The colon in the first entry of x indicates all the rows of x, so that x(:, 1) is a vector. The .^ and .* operators perform element-wise operations on the vectors.

• In the **Vectorize** pane, set the **Fitness function is vectorized** option to On.

Note The fitness function must accept an arbitrary number of rows to use the **Vectorize** option.

The following comparison, run at the command line, shows the improvement in speed with **Vectorize** set to On.

```
tic;ga(@rastriginsfcn,20);toc
elapsed_time =
    4.3660
options=gaoptimset('Vectorize','on');
tic;ga(@rastriginsfcn,20,[],[],[],[],[],[],[],options);toc
elapsed_time =
    0.5810
```

Constrained Minimization Using ga

Suppose you want to minimize the simple fitness function of two variables x_1 and x_2 ,

$$\min_{x} f(x) = 100 \left(x_1^2 - x_2 \right)^2 + (1 - x_1)^2$$

subject to the following nonlinear inequality constraints and bounds

```
\begin{aligned} x_1 \cdot x_2 + x_1 - x_2 + 1.5 &\leq 0 \quad \text{(nonlinear constraint)} \\ 10 - x_1 \cdot x_2 &\leq 0 \quad \text{(nonlinear constraint)} \\ 0 &\leq x_1 &\leq 1 \quad \text{(bound)} \\ 0 &\leq x_2 &\leq 13 \quad \text{(bound)} \end{aligned}
```

Begin by creating the fitness and constraint functions. First, create an M-file named simple_fitness.m as follows:

```
function y = simple_fitness(x)
y = 100 * (x(1)^2 - x(2))^2 + (1 - x(1))^2;
```

The genetic algorithm function, ga, assumes the fitness function will take one input x, where x has as many elements as the number of variables in the problem. The fitness function computes the value of the function and returns that scalar value in its one return argument, y.

Then create an M-file, simple constraint.m, containing the constraints

```
function [c, ceq] = simple_constraint(x)
c = [1.5 + x(1)*x(2) + x(1) - x(2);...
-x(1)*x(2) + 10;
ceq = [];
```

The ga function assumes the constraint function will take one input x, where x has as many elements as the number of variables in the problem. The constraint function computes the values of all the inequality and equality constraints and returns two vectors, c and ceg, respectively.

To minimize the fitness function, you need to pass a function handle to the fitness function as the first argument to the ga function, as well as specifying the number of variables as the second argument. Lower and upper bounds are provided as LB and UB respectively. In addition, you also need to pass a function handle to the nonlinear constraint function.

```
ObjectiveFunction = @simple fitness;
              % Number of variables
nvars = 2;
LB = [0 \ 0]; % Lower bound
UB = [1 13]; % Upper bound
ConstraintFunction = @simple constraint;
[x,fval] = ga(ObjectiveFunction,nvars,[],[],[],[],LB,UB,ConstraintFunction)
Warning: 'mutationgaussian' mutation function
is for unconstrained minimization only;
using @mutationadaptfeasible mutation function.
Set @mutationadaptfeasible as MutationFcn options
using GAOPTIMSET.
Optimization terminated: current tolerance on f(x) 1e-007
is less than options. TolFun and constraint violation is
less than options.TolCon.
```

```
x =
     0.8122     12.3122

fval =
     1.3578e+004
```

Note For the constrained minimization problem, the ga function changed the mutation function to @mutationadaptfeasible. The default mutation function, @mutationgaussian, is only appropriate for unconstrained minimization problems.

The genetic algorithm solver handles linear constraints and bounds differently from nonlinear constraints. All the linear constraints and bounds are satisfied throughout the optimization. However, ga may not satisfy all the nonlinear constraints at every generation. If ga converges to a solution, the nonlinear constraints will be satisfied at that solution.

ga uses the mutation and crossover functions to produce new individuals at every generation. ga satisfies linear and bound constraints by using mutation and crossover functions that only generate feasible points. For example, in the previous call to ga, the default mutation function mutationguassian will not satisfy the linear constraints and so the mutationadaptfeasible is used instead. If you provide a custom mutation function, this custom function must only generate points that are feasible with respect to the linear and bound constraints. All the crossover functions in the toolbox generate points that satisfy the linear constraints and bounds except the crossoverheuristic function.

Specify mutationadaptfeasible as the mutation function for the minimization problem by using the gaoptimset function.

```
options = gaoptimset('MutationFcn',@mutationadaptfeasible);
```

Next run the ga solver.

```
[x,fval] = ga(ObjectiveFunction,nvars,[],[],[],LB,UB,ConstraintFunction,options)
```

```
Optimization terminated: current tolerance on f(x) 1e-007 is less than options.TolFun
and constraint violation is less than options.TolCon.
x =
   0.8122 12.3122
fval =
  1.3578e+004
```

Now, use the gaoptimset function to create an options structure that will select two plot functions. The first plot function is gaplotbestf, which plots the best and mean score of the population at every generation. The second plot function is gaplotmaxconstr, which plots the maximum constraint violation of nonlinear constraints at every generation. You can also visualize the progress of the algorithm by displaying information to the command window using the 'Display' option.

```
options = gaoptimset(options, 'PlotFcns', {@gaplotbestf,@gaplotmaxconstr}, 'Display', 'iter');
```

Rerun the ga solver.

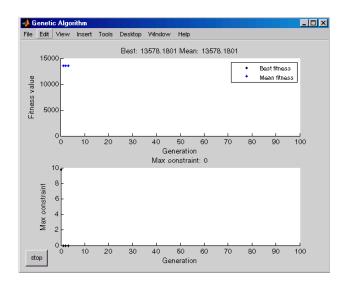
[x,fval] = ga(ObjectiveFunction,nvars,[],[],[],[],... LB, UB, ConstraintFunction, options)

		Best	max	Stall
Generation	f-count	f(x)	constraint	Generations
1	849	14915.8	0	0
2	1567	13578.3	0	0
3	2334	13578.3	0	1
4	3043	13578.3	0	2
5	3752	13578.3	0	3

Optimization terminated: current tolerance on f(x) 1e-009 is less than options. TolFun and constraint violation is less than options.TolCon.

```
x =
     0.8122     12.3123

fval =
     1.3578e+004
```



You can provide a start point for the minimization to the ga function by specifying the InitialPopulation option. The ga function will use the first individual from InitialPopulation as a start point for a constrained minimization.

```
X0 = [0.5 0.5]; % Start point (row vector)
options = gaoptimset(options, 'InitialPopulation', X0);
```

Now, rerun the ga solver.

 $[x,fval] = ga(ObjectiveFunction,nvars,[],[],[],[],\dots \\ LB,UB,ConstraintFunction,options)$

		Best	max	Stall
Generation	f-count	f(x)	constraint	Generations
1	965	13579.6	0	0
2	1728	13578.2	1.776e-015	0
3	2422	13578.2	0	0

Optimization terminated: current tolerance on f(x) 1e-007 is less than options.TolFun and constraint violation is less than options.TolCon.

x =

0.8122 12.3122

fval =

1.3578e+004

Parameterizing Functions Called by ga

In this section...

"Using Additional Parameters" on page 6-65

"Parameterizing Functions Using Anonymous Functions with ga" on page 6-65

"Parameterizing a Function Using a Nested Function with ga" on page 6-66

Using Additional Parameters

Sometimes you might want to write functions that are called by ga that have additional parameters to the independent variable. For example, suppose you want to minimize the following function:

$$f(x) = (a - bx_1^2 + x_1^{4/3})x_1^2 + x_1x_2 + (-c + cx_2^2)x_2^2$$

for different values of a, b, and c. Because ga accepts a fitness function that depends only on x, you must provide the additional parameters a, b, and c to the function before calling ga.

The following examples show how to parameterize the objective function, but you can use the same methods to parameterize any user-defined functions called by ga, patternsearch, simulannealbnd, or threshacceptbnd.

Parameterizing Functions Using Anonymous Functions with ga

To parameterize your function, first write an M-file containing the following code:

function y = parameterfun(x,a,b,c)
y =
$$(a - b*x(1)^2 + x(1)^4/3)*x(1)^2 + x(1)*x(2) + ...$$

 $(-c + c*x(2)^2)*x(2)^2;$

Save the M- file as parameterfun.m in a directory on the MATLAB path.

Now, suppose you want to minimize the function for the parameter values a = 4, b = 2.1, and c = 4. To do so, define a function handle to an anonymous function by entering the following commands at the MATLAB prompt:

```
a = 4; b = 2.1; c = 4;
                         % Define parameter values
fitfun = @(x) parameterfun(x,a,b,c);
NVARS = 3;
```

If you are using the Genetic Algorithm Tool,

- Set **Fitness function** to fitfun.
- Set **Number of variables** to NVARS.

```
a = 3.6; b = 2.4; c = 5;
                            % Define parameter values
fitfun = @(x) parameterfun(x,a,b,c);
```

Parameterizing a Function Using a Nested Function with ga

As an alternative to parameterizing the objective function as an anonymous function, you can write a single M-file that

- Accepts a, b, c and NVARS as inputs.
- Contains the fitness function as a nested function.
- Calls ga.

The following shows the code for the M-file.

```
function [x \text{ fval}] = \text{runga}(a,b,c,NVARS)
[x, fval] = ga(@nestedfun,NVARS);
% Nested function that computes the fitness function
    function y = nestedfun(x)
        y = (a - b*x(1)^2 + x(1)^4/3)*x(1)^2 + x(1)*x(2) + ...
          (-c + c*x(2)^2)*x(2)^2;
    end
end
```

Note that the fitness function is computed in the nested function nestedfun, which has access to the variables a, b, and c. To run the optimization, enter

```
[x fval] = runga(a,b,c,NVARS)
```

This returns

χ =

-0.1302 0.7170 0.2272

fval =

-1.0254

Using the Simulated Annealing and Threshold Acceptance Algorithms

Using the Simulated Annealing and Threshold Acceptance Algorithms from the Command Line (p. 7-2)

Simulated Annealing and Threshold Acceptance Examples (p. 7-7)

Explains how to use the simulated annealing and threshold acceptance algorithms at the command line.

Links to examples of using the simulated annealing and threshold acceptance algorithms.

Using the Simulated Annealing and Threshold Acceptance Algorithms from the Command Line

In this section...

"Running simulannealbnd and threshacceptbnd with the Default Options" on page 7-2

"Setting Options for simulannealbnd and threshacceptbnd at the Command Line" on page 7-3

"Reproducing Your Results" on page 7-5

Running simulannealbnd and threshacceptbnd with the Default Options

To run either the simulated annealing or threshold acceptance algorithms with the default options, call the corresponding function with the syntax

```
[x, fval] = simulannealbnd(@objfun, x0)
[x, fval] = threshacceptbnd(@objfun, x0)
```

The input arguments to simulannealbnd and threshacceptbnd are

- @objfun A function handle to the M-file that computes the objective function. "Writing M-Files for Functions You Want to Optimize" on page 1-3 explains how to write this M-file.
- x0 The initial guess of the optimal argument to the objective function.

The output arguments are

- x The final point.
- fval The value of the objective function at x.

For a description of additional input and output arguments, see the reference pages for simulannealbnd and threshacceptbnd.

You can run the example described in "Example: Minimizing De Jong's Fifth Function" on page 4-4 from the command line with the simulated annealing algorithm by entering

```
[x, fval] = simulannealbnd(@dejong5fcn, [0 0])
```

This returns

```
x =
-31.9564 -15.9755
fval =
5.9288
```

Additional Output Arguments

To get more information about the performance of the algorithm, you can call simulannealbnd or threshacceptbnd with the syntax

```
[x, fval, exitflag, output] = simulannealbnd(@objfun, x0)
```

Besides x and fval, this function returns the following additional output arguments:

- exitflag Flag indicating the reason the algorithm terminated
- output Structure containing information about the performance of the algorithm

See the simulannealbnd and threshacceptbnd reference pages for more information about these arguments.

Setting Options for simulannealbnd and threshacceptbnd at the Command Line

You can specify options by passing an options structure as an input argument to either simulannealbnd and threshacceptbnd using the syntax

```
[x, fval] = simulannealbnd(@objfun, x0, [], [], options)
```

This syntax does not specify any lower or upper bound constraints.

You create the options structure using the function saoptimset:

```
options = saoptimset('simulannealbnd')
```

This returns the structure options with the default values for its fields:

```
options =
          AnnealingFcn: @annealingfast
        TemperatureFcn: @temperatureexp
         AcceptanceFcn: @acceptancesa
                TolFun: 1.0000e-006
        StallIterLimit: '500*numberofvariables'
           MaxFunEvals: '3000*numberofvariables'
             TimeLimit: Inf
               MaxIter: Inf
        ObjectiveLimit: -Inf
               Display: 'final'
       DisplayInterval: 10
             HybridFcn: []
        HybridInterval: 'end'
              PlotFcns: []
          PlotInterval: 1
            OutputFcns: []
    InitialTemperature: 100
      ReannealInterval: 100
              DataType: 'double'
```

These are the default values for simulannealbnd. To see the default values for threshacceptbnd, run

```
options = saoptimset('threshacceptbnd')
```

The value of each option is stored in a field of the options structure, such as options. ReannealInterval. You can display any of these values by entering options followed by the name of the field. For example, to display the interval for reannealing used for the simulated annealing algorithm, enter

```
options.ReannealInterval
ans =
   100
```

To create an options structure with a field value that is different from the default—for example, to set ReannealInterval to 300 instead of its default value 100—enter

```
options = saoptimset('ReannealInterval', 300)
```

This creates the options structure with all values set to their defaults, except for ReannealInterval, which is set to 300.

If you now enter

```
simulannealbnd(@objfun, x0, [], [], options)
```

simulannealbnd runs the simulated annealing algorithm with a reannealing interval of 300.

If you subsequently decide to change another field in the options structure, such as setting PlotFcns to @saplotbestf, which plots the best objective function value at each iteration, call saoptimset with the syntax

```
options = saoptimset(options, 'PlotFcns', @saplotbestf)
```

This preserves the current values of all fields of options except for PlotFcns, which is changed to @saplotbestf. Note that if you omit the input argument options, saoptimset resets ReannealInterval to its default value 100.

You can also set both ReannealInterval and PlotFcns with the single command

Reproducing Your Results

Because the simulated annealing and threshold acceptance algorithms are stochastic—that is, they each makes random choices—you get slightly different results each time you run them. The algorithms use the MATLAB uniform and normal random number generators, rand and randn, when generating subsequent points and also when determining whether or not to accept new points. Each time the algorithms call rand and randn, their states are changed so that the next time they are called, they return different random numbers.

If you need to reproduce your results exactly, call simulannealbnd or threshacceptbnd with an output argument that contains the current states of rand and randn and then reset the states to these values before running the function again. For example, to reproduce the output of simulanneal applied to De Jong's fifth function, call simulannealbnd with the syntax

```
[x,fval,exitflag,output] = simulannealbnd(@dejong5fcn,[0 0]);
```

Suppose the results are

```
x =
  -32.0401
            -16.1223
fval =
    5.9288
```

The states of rand and randn are stored in two fields of output.

```
output =
     iterations: 2041
      funccount: 2058
        message: [1x80 char]
      randstate: [625x1 uint32]
     randnstate: [2x1 double]
    problemtype: 'unconstrained'
    temperature: [2x1 double]
      totaltime: 1.8226
```

Reset the states by entering

```
rand('twister', output.randstate);
randn('state', output.randnstate);
```

If you now run simulannealbnd a second time, you get the same results.

Note If you do not need to reproduce your results, it is better not to set the states of rand and randn, so that you get the benefit of the randomness in these algorithms.

Simulated Annealing and Threshold Acceptance Examples

If you are viewing this documentation in the Help browser, click the following link to see the demo Minimization Using Simulated Annealing And Threshold Acceptance Algorithms. Or, from the command line in MATLAB, type showdemo('saobjective').

Options Reference

Pattern Search Options (p. 8-2)

Describes the options for pattern

search.

Genetic Algorithm Options (p. 8-23)

Describes the options for the genetic

algorithm.

Simulated Annealing and Threshold Acceptance Algorithm Options (p. 8-45)

Describes the options for the simulated annealing and threshold

acceptance algorithms.

Pattern Search Options

In this section...

"Pattern Search Tool vs. Command Line" on page 8-2

"Plot Options" on page 8-3

"Poll Options" on page 8-5

"Search Options" on page 8-8

"Mesh Options" on page 8-12

"Algorithm Settings" on page 8-13

"Cache Options" on page 8-13

"Stopping Criteria" on page 8-14

"Output Function Options" on page 8-15

"Display to Command Window Options" on page 8-17

"Vectorize Option" on page 8-18

"Options Table for Pattern Search Algorithms" on page 8-19

Pattern Search Tool vs. Command Line

There are two ways to specify options for pattern search, depending on whether you are using the Pattern Search Tool or calling the function patternsearch at the command line:

- If you are using the Pattern Search Tool (psearchtool), you specify the options by selecting an option from a drop-down list or by entering the value of the option in the text field, as described in "Setting Options in the Pattern Search Tool" on page 5-14.
- If you are calling patternsearch from the command line, you specify the options by creating an options structure using the function psoptimset, as follows:

```
options = psoptimset('Param1', value1, 'Param2', value2, ...);
```

See "Setting Options for patternsearch at the Command Line" on page 5-21 for examples.

In this section, each option is listed in two ways:

- By its label, as it appears in the Pattern Search Tool
- By its field name in the options structure

For example:

- **Poll method** refers to the label of the option in the Pattern Search Tool.
- PollMethod refers to the corresponding field of the options structure.

Plot Options

Plot options enable you to plot data from the pattern search while it is running. When you select plot functions and run the pattern search, a plot window displays the plots on separate axes. You can stop the algorithm at any time by clicking the **Stop** button on the plot window.

Plot interval (PlotInterval) specifies the number of iterations between consecutive calls to the plot function.

You can select any of the following plots in the **Plots** pane.

- **Best function value** (@psplotbestf) plots the best objective function value.
- Function count (@psplotfuncount) plots the number of function evaluations.
- Mesh size (@psplotmeshsize) plots the mesh size.
- Best point (@psplotbestx) plots the current best point.
- Max constraint (@psplotmaxconstr) plots the maximum nonlinear constraint violation.
- **Custom** enables you to use your own plot function. To specify the plot function using the Pattern Search Tool,
 - Select Custom function.

• Enter @myfun in the text box, where myfun is the name of your function.

"Structure of the Plot Functions" on page 8-4 describes the structure of a plot function.

To display a plot when calling patternsearch from the command line, set the PlotFcns field of options to be a function handle to the plot function. For example, to display the best function value, set options as follows

```
options = psoptimset('PlotFcns', @psplotbestf);
```

To display multiple plots, use the syntax

```
options = psoptimset('PlotFcns', {@plotfun1, @plotfun2, ...});
```

where <code>@plotfun1</code>, <code>@plotfun2</code>, and so on are function handles to the plot functions (listed in parentheses in the preceding list).

Structure of the Plot Functions

The first line of a plot function has the form

```
function stop = plotfun(optimvalues, flag)
```

The input arguments to the function are

- optimvalues Structure containing information about the current state of the solver. The structure contains the following fields:
 - x Current point
 - iteration Iteration number
 - fval Objective function value
 - meshsize Current mesh size
 - function Number of function evaluations
 - method Method used in last iteration
 - TolFun Tolerance on function value in last iteration
 - TolX Tolerance on x value in last iteration

- nonlinineq Nonlinear inequality constraints, displayed only when a nonlinear constraint function is specified
- nonlineq Nonlinear equality constraints, displayed only when a nonlinear constraint function is specified
- flag Current state in which the plot function is called. The possible values for flag are
 - init Initialization state
 - iter Iteration state
 - interrupt Intermediate stage
 - done Final state

"Parameterizing Functions Called by patternsearch" on page 5-52 explains how to provide additional parameters to the function.

The output argument stop provides a way to stop the algorithm at the current iteration. stop can have the following values:

- false The algorithm continues to the next iteration.
- true The algorithm terminates at the current iteration.

Poll Options

Poll options control how the pattern search polls the mesh points at each iteration.

Poll method (PollMethod) specifies the pattern the algorithm uses to create the mesh. There are two patterns for each of the two classes of direct search algorithms: the generalized pattern search (GPS) algorithm and the mesh adaptive direct search (MADS) algorithm.

These patterns are the Positive basis 2N and the Positive basis N+1:

• The default pattern, GPS Positive basis 2N, consists of the following 2N vectors, where N is the number of independent variables for the objective function.

```
[100...0]

[010...0]

...

[000...1]

[-1 00...0]

[0 -10...0]

...

[0 00...-1]
```

For example, if the optimization problem has three independent variables, the pattern consists of the following six vectors.

```
\begin{bmatrix}
1 & 0 & 0 \\
0 & 1 & 0
\end{bmatrix}

\begin{bmatrix}
0 & 0 & 1 \\
-1 & 0 & 0
\end{bmatrix}

\begin{bmatrix}
0 & -1 & 0 \\
0 & 0 & -1
\end{bmatrix}
```

- The pattern, MADS Positive basis 2N, consists of 2N randomly generated vectors, where N is the number of independent variables for the objective function. This is done by randomly generating N vectors which form a linearly independent set, then using this first set and the negative of this set gives 2N vectors. As shown above, the GPS Positive basis 2N pattern is formed using the positive and negative of the linearly independent identity, however, with the MADS Positive basis 2N, the pattern is generated using a random permutation of an N-by-N linearly independent lower triangular matrix that is regenerated at each iteration.
- The GPS Positive basis NP1 pattern consists of the following N+1 vectors.

For example, if the objective function has three independent variables, the pattern consists of the following four vectors.

• The pattern, MADS Positive basis N+1, consists of N randomly generated vectors to form the positive basis, where N is the number of independent variables for the objective function. Then, one more random vector is generated, giving N+1 randomly generated vectors. Each iteration generates a new pattern when the MADS Positive basis N+1 is selected.

Complete poll (CompletePoll) specifies whether all the points in the current mesh must be polled at each iteration. **Complete Poll** can have the values On or Off.

- If you set **Complete poll** to On, the algorithm polls all the points in the mesh at each iteration and chooses the point with the smallest objective function value as the current point at the next iteration.
- If you set **Complete poll** to Off, the default value, the algorithm stops the poll as soon as it finds a point whose objective function value is less than that of the current point. The algorithm then sets that point as the current point at the next iteration.

Polling order (PollingOrder) specifies the order in which the algorithm searches the points in the current mesh. The options are

• Random — The polling order is random.

- Success The first search direction at each iteration is the direction in which the algorithm found the best point at the previous iteration. After the first point, the algorithm polls the mesh points in the same order as **Consecutive**.
- Consecutive The algorithm polls the mesh points in *consecutive* order, that is, the order of the pattern vectors as described in "Poll Method" on page 5-25.

See "Poll Options" on page 8-5 for more information.

Search Options

Search options specify an optional search that the algorithm can perform at each iteration prior to the polling. If the search returns a point that improves the objective function, the algorithm uses that point at the next iteration and omits the polling. Please note, if you have selected the same **Search method** and **Poll method**, only the option selected in the Poll method will be used, although both will be used when the options selected are different.

Complete search (CompleteSearch) applies when you set **Search method** to GPS Positive basis Np1, GPS Positive basis 2N, MADS Positive basis Np1, MADS Positive basis 2N, or Latin hypercube. **Complete** search can have the values On or Off.

For GPS Positive basis Np1, MADS Positive basis Np1, GPS Positive basis 2N, or MADS Positive basis 2N, **Complete search** has the same meaning as the poll option **Complete poll**.

Search method (SearchMethod) specifies the optional search step. The options are

- None ([]) (the default) specifies no search step.
- GPS Positive basis Np1 ('GPSPositiveBasisNp1') performs a search step of a pattern search using the GPS Positive Basis Np1 option.
- GPS Positive basis 2N('GPSPositiveBasis2N') performs a search step of a pattern search using the GPS Positive Basis 2N option.
- MADS Positive basis Np1 ('MADSPositiveBasisNp1') performs a search step of a pattern search using the MADS Positive Basis Np1option.

- MADS Positive basis 2N ('MADSPositiveBasis2N') performs a search step of a pattern search using the MADS Positive Basis 2N option.
- Genetic Algorithm (@searchga) specifies a search using the genetic algorithm. If you select Genetic Algorithm, two other options appear:
 - **Iteration limit** Positive integer specifying the number of iterations of the pattern search for which the genetic algorithm search is performed. The default for **Iteration limit** is 1.
 - Options Options structure for the genetic algorithm, which you can set using gaoptimset.

To change the default values of **Iteration limit** and **Options** at the command line, use the syntax

where iterlim is the value of **Iteration limit** and optionsGA is the genetic algorithm options structure.

- Latin hypercube (@searchlhs) specifies a Latin hypercube search. The way the search is performed depends on the setting for **Complete search**:
 - If you set Complete search to On, the algorithm polls all the points that are randomly generated at each iteration by the Latin hypercube search and chooses the one with the smallest objective function value.
 - If you set **Complete search** to Off (the default), the algorithm stops the poll as soon as it finds one of the randomly generated points whose objective function value is less than that of the current point, and chooses that point for the next iteration.

If you select Latin hypercube, two other options appear:

- **Iteration limit** Positive integer specifying the number of iterations of the pattern search for which the Latin hypercube search is performed. The default for **Iteration limit** is 1.
- **Design level** A positive integer specifying the design level. The number of points searched equals the **Design level** multiplied by the number of independent variables for the objective function. The default for **Design level** is 15.

To change the default values of **Iteration limit** and **Design level** at the command line, use the syntax

```
options=psoptimset('SearchMethod', {@searchlhs,iterlim,level})
```

where iterlim is the value of **Iteration limit** and level is the value of **Design level**.

- Nelder-Mead (@searchneldermead) specifies a search using fminsearch, which uses the Nelder-Mead algorithm. If you select Nelder-Mead, two other options appear:
 - **Iteration limit** Positive integer specifying the number of iterations of the pattern search for which the Nelder-Mead search is performed. The default for **Iteration limit** is 1.
 - Options Options structure for the function fminsearch, which you can create using the function optimset.

To change the default values of **Iteration limit** and **Options** at the command line, use the syntax

where iterlim is the value of **Iteration limit** and optionsNM is the options structure.

- Custom enables you to write your own search function. To specify the search function using the Pattern Search Tool,
 - Set Search function to Custom.
 - Set Function name to @myfun, where myfun is the name of your function.

If you are using patternsearch, set

```
options = psoptimset('SearchMethod', @myfun);
```

To see a template that you can use to write your own search function, enter

```
edit searchfcntemplate
```

The following section describes the structure of the search function.

Structure of the Search Function

Your search function must have the following calling syntax.

```
function [successSearch,xBest,fBest,funccount] =
searchfcntemplate(fun,x,A,b,Aeq,beq,lb,ub, ...
    optimValues,options)
```

The search function has the following input arguments:

- fun Objective function
- x Current point
- A,b Linear inequality constraints
- Aeq, beq Linear equality constraints
- 1b, ub Lower and upper bound constraints
- optimValues Structure that enables you to set search options. The structure contains the following fields:
 - x Current point
 - fval Objective function value at x
 - iteration Current iteration number
 - funccount Counter for user function evaluation
 - scale Scale factor used to scale the design points
 - problemtype Flag passed to the search routines, indicating whether the problem is 'unconstrained', 'boundconstraints', or 'linearconstraints'. This field is a sub-problem type for nonlinear constrained problems.
 - meshsize Current mesh size used in search step
 - method Method used in last iteration
- options Pattern search options structure

The function has the following output arguments:

• successSearch — A Boolean identifier indicating whether the search is successful or not

xBest,fBest — Best point and best function value found by search method

Note If you set **Search method** to Genetic algorithm or Nelder-Mead, we recommend that you leave **Iteration limit** set to the default value 1, because performing these searches more than once is not likely to improve results.

function — Number of user function evaluation in search method

See "Using a Search Method" on page 5-32 for an example.

Mesh Options

Mesh options control the mesh that the pattern search uses. The following options are available.

Initial size (InitialMeshSize) specifies the size of the initial mesh, which is the length of the shortest vector from the initial point to a mesh point. **Initial size** should be a positive scalar. The default is 1.0.

Max size (MaxMeshSize) specifies a maximum size for the mesh. When the maximum size is reached, the mesh size does not increase after a successful iteration. Max size must be a positive scalar, and is only used when the GPS algorithm is selected as the Poll or Search method. The default value is Inf.

Accelerator (MeshAccelerator) specifies whether the **Contraction factor** is multiplied by 0.5 after each unsuccessful iteration. **Accelerator** can have the values 0n or 0ff, the default.

Rotate (MeshRotate) specifies whether the mesh vectors are multiplied by -1 when the mesh size is less than a small value. **Rotate** is only applied when **Poll method** is set to GPS Positive basis Np1.

Note Changing the setting of **Rotate** has no effect on the poll when **Poll** method is set to GPS Positive basis 2N, MADS Positive basis 2N, or MADS Positive basis Np1.

Scale (ScaleMesh) specifies whether the algorithm scales the mesh points by multiplying the pattern vectors by constants. **Scale** can have the values Off or On (the default).

Expansion factor (MeshExpansion) specifies the factor by which the mesh size is increased after a successful poll. The default value is 2.0, which means that the size of the mesh is multiplied by 2.0 after a successful poll. **Expansion factor** must be a positive scalar and is only used when a GPS method is selected as the Poll or Search method.

Contraction factor (MeshContraction) specifies the factor by which the mesh size is decreased after an unsuccessful poll. The default value is 0.5, which means that the size of the mesh is multiplied by 0.5 after an unsuccessful poll. Contraction factor must be a positive scalar and is only used when a GPS method is selected as the Poll or Search method.

See "Mesh Expansion and Contraction" on page 5-35 for more information.

Algorithm Settings

Algorithm settings define algorithmic specific parameters.

Parameters that can be specified for a nonlinear constraint algorithm include

- **Initial penalty** (InitialPenalty) Specifies an initial value of the penalty parameter that is used by the algorithm. **Initial penalty** must be greater than or equal to 1.
- **Penalty factor** (PenaltyFactor) Increases the penalty parameter when the problem is not solved to required accuracy and constraints are not satisfied. **Penalty factor** must be greater than 1.

Cache Options

The pattern search algorithm can keep a record of the points it has already polled, so that it does not have to poll the same point more than once. If the objective function requires a relatively long time to compute, the cache option can speed up the algorithm. The memory allocated for recording the points is called the cache. This option should only be used for deterministic objective functions, but not for stochastic ones.

Cache (Cache) specifies whether a cache is used. The options are On and Off, the default. When you set **Cache** to On, the algorithm does not evaluate the objective function at any mesh points that are within **Tolerance** of a point in the cache.

Tolerance (CacheTo1) specifies how close a mesh point must be to a point in the cache for the algorithm to omit polling it. **Tolerance** must be a positive scalar. The default value is eps.

Size (CacheSize) specifies the size of the cache. **Size** must be a positive scalar. The default value is 1e4.

See "Using Cache" on page 5-41 for more information.

Stopping Criteria

Stopping criteria determine what causes the pattern search algorithm to stop. Pattern search uses the following criteria:

Mesh tolerance (TolMesh) specifies the minimum tolerance for mesh size. The algorithm stops if the mesh size becomes smaller than **Mesh tolerance**. The default value is 1e-6.

Max iteration (MaxIter) specifies the maximum number of iterations the algorithm performs. The algorithm stops if the number of iterations reaches Max iteration. You can select either

- **100*numberofvariables** Maximum number of iterations is 100 times the number of independent variables (the default).
- **Specify** A positive integer for the maximum number of iterations

Max function evaluations (MaxFunEval) specifies the maximum number of evaluations of the objective function. The algorithm stops if the number of function evaluations reaches **Max function evaluations**. You can select either

• **2000*numberofvariables** — Maximum number of function evaluations is 2000 times the number of independent variables.

 Specify — A positive integer for the maximum number of function evaluations

Time limit (TimeLimit) specifies the maximum time in seconds the pattern search algorithm runs before stopping. This also includes any specified pause time for pattern search algorithms.

Bind tolerance (TolBind) specifies the minimum tolerance for the distance from the current point to the boundary of the feasible region. Bind tolerance specifies when a linear constraint is active. It is not a stopping criterion. The default value is 1e-3.

X tolerance (TolX) specifies the minimum distance between the current points at two consecutive iterations. The algorithm stops if the distance between two consecutive points is less than **X tolerance**. The default value is 1e-6.

Function tolerance (TolFun) specifies the minimum tolerance for the objective function. After a successful poll, if the difference between the function value at the previous best point and function value at the current best point is less than the value of Function tolerance, the algorithm halts. The default value is 1e-6.

See "Setting Tolerances for the Solver" on page 5-43 for an example.

Nonlinear constraint tolerance (TolCon) — The **Nonlinear constraint tolerance** is not used as stopping criterion. It is used to determine the feasibility with respect to nonlinear constraints.

Output Function Options

Output functions are functions that the pattern search algorithm calls at each iteration. The following options are available:

- **History to new window** (@psoutputhistory) displays the history of points computed by the algorithm in the MATLAB Command Window at each multiple of **Interval** iterations.
- Custom enables you to write your own output function. To specify the output function using the Pattern Search Tool,

- Select Custom function.
- Enter @myfun in the text box, where myfun is the name of your function.

If you are using patternsearch, set

```
options = psoptimset('OutputFcn', @myfun);
```

To see a template that you can use to write your own output function, enter

```
edit psoutputfcntemplate
```

at the MATLAB command prompt.

The following section describes the structure of the output function.

Structure of the Output Function

Your output function must have the following calling syntax:

```
[stop, options,optchanged] =
psoutputhistory(optimvalues,options,flag,interval)
```

The function has the following input arguments:

- optimvalues Structure containing information about the current state of the solver. The structure contains the following fields:
 - x Current point
 - iteration Iteration number
 - fval Objective function value
 - meshsize Current mesh size
 - funccount Number of function evaluations
 - method Method used in last iteration
 - TolFun Tolerance on function value in last iteration
 - TolX Tolerance on x value in last iteration
 - nonlining Nonlinear inequality constraints, displayed only when a nonlinear constraint function is specified

- nonlineq Nonlinear equality constraints, displayed only when a nonlinear constraint function is specified
- options Options structure
- flag Current state in which the output function is called. The possible values for flag are
 - init Initialization state
 - iter Iteration state
 - interrupt Intermediate stage
 - done Final state
- interval Optional interval argument

"Parameterizing Functions Called by patternsearch" on page 5-52 explains how to provide additional parameters to the output function.

The output function returns the following arguments to ga:

- stop Provides a way to stop the algorithm at the current iteration. stop can have the following values.
 - false The algorithm continues to the next iteration.
 - true The algorithm terminates at the current iteration.
- options Options structure.
- \bullet optchanged Flag indicating changes to options.

Display to Command Window Options

Level of display ('Display') specifies how much information is displayed at the command line while the pattern search is running. The available options are

- Off ('off') No output is displayed.
- Iterative ('iter') Information is displayed for each iteration.
- Diagnose ('diagnose') Information is displayed for each iteration. In addition, the diagnostic lists some problem information and the options that are changed from the defaults.

• Final ('final') — The reason for stopping is displayed.

Both Iterative and Diagnose display the following information:

- Iter Iteration number
- FunEval Cumulative number of function evaluations
- MeshSize Current mesh size
- FunVal Objective function value of the current point
- Method Outcome of the current poll (with no nonlinear constraint function specified). With a nonlinear constraint function, Method displays the update method used after a subproblem is solved.
- Max Constraint Maximum nonlinear constraint violation (displayed only when a nonlinear constraint function has been specified)

The default value of **Level of display** is

- Off in the Pattern Search Tool
- 'final' in an options structure created using psoptimset

Vectorize Option

Objective function is vectorized specifies whether the computation of the objective function is vectorized. When **Objective function is vectorized** is Off, the algorithm calls the objective function on one point at a time as it loops through all of the mesh points. When **Objective function is vectorized** is On, the pattern search algorithm calls the objective function on all the points in the mesh at once, i.e., in a single call to the objective function if either **Complete Poll** or **Complete Search** is On.

Options Table for Pattern Search Algorithms

Option Availability Table for GPS and MADS Algorithms

Option	Description	Algorithm Availability
Cache	With Cache set to 'on', patternsearch keeps a history of the mesh points it polls and does not poll points close to them again at subsequent iterations. Use this option if patternsearch runs slowly because it is taking a long time to compute the objective function. If the objective function is stochastic, it is advised not to use this option.	GPS MADS
CacheSize	Size of the cache.	GPSMADS
CacheTol	Positive scalar specifying how close the current mesh point must be to a point in the cache in order for patternsearch to avoid polling it. Available if 'Cache' option is set to 'on'.	GPSMADS
CompletePoll	Complete poll around current iterate. Evaluate all the points in a poll step.	GPSMADS
CompleteSearch	Complete poll around current iterate. Evaluate all the points in a search step.	GPSMADS
Display	Level of display to Command Window.	GPSMADS

Option Availability Table for GPS and MADS Algorithms (Continued)

Option	Description	Algorithm Availability
InitialMeshSize	Initial mesh size used in pattern search algorithms.	GPSMADS
InitialPenalty	Initial value of the penalty parameter.	GPSMADS
MaxFunEvals	Maximum number of objective function evaluations.	GPSMADS
MaxIter	Maximum number of iterations.	GPSMADS
MaxMeshSize	Maximum mesh size used in a poll/search step.	GPSMADS
MeshAccelerator	Accelerate mesh size contraction.	GPSMADS
MeshContraction	Mesh contraction factor, used when iteration is unsuccessful.	GPS — Default value is 0.5.MADS — Default value is 0.25 if MADS algorithm is selected for either the Poll method or Search method.
MeshExpansion	Mesh expansion factor, expands mesh when iteration is successful.	GPS — Default value is 2.MADS — Default value is 4 if MADS algorithm is selected for either the Poll method or Search method
MeshRotate	Rotate the pattern before declaring a point to be optimum.	GPSMADS

Option Availability Table for GPS and MADS Algorithms (Continued)

Option	Description	Algorithm Availability
OutputFcn	User-specified function that a pattern search calls at each iteration.	GPSMADS
PenaltyFactor	Penalty update parameter.	GPSMADS
PlotFcn	Specifies function to plot at runtime.	GPSMADS
PlotInterval	Specifies that plot functions will be called at every interval.	GPSMADS
PollingOrder	Order in which search directions are polled.	GPS only
PollMethod	Polling strategy used in pattern search.	GPSMADS
ScaleMesh	Automatic scaling of variables.	GPSMADS
SearchMethod	Specifies search method used in pattern search.	GPSMADS
TimeLimit	Total time (in seconds) allowed for optimization. Also includes any specified pause time for pattern search algorithms.	GPSMADS
TolBind	Binding tolerance used to determine if linear constraint is active.	GPSMADS
TolCon	Tolerance on nonlinear constraints.	GPSMADS
TolFun	Tolerance on function value.	GPSMADS
TolMesh	Tolerance on mesh size.	GPSMADS

Option Availability Table for GPS and MADS Algorithms (Continued)

Option	Description	Algorithm Availability
TolX	Tolerance on independent variable.	GPSMADS
Vectorized	Specifies whether functions are vectorized.	GPSMADS

Genetic Algorithm Options

In this section...

- "Genetic Algorithm Tool vs. Command Line" on page 8-23
- "Plot Options" on page 8-24
- "Population Options" on page 8-27
- "Fitness Scaling Options" on page 8-29
- "Selection Options" on page 8-31
- "Reproduction Options" on page 8-32
- "Mutation Options" on page 8-33
- "Crossover Options" on page 8-35
- "Migration Options" on page 8-39
- "Algorithm Settings" on page 8-39
- "Multiobjective Options" on page 8-40
- "Hybrid Function Options" on page 8-40
- "Stopping Criteria Options" on page 8-41
- "Output Function Options" on page 8-41
- "Display to Command Window Options" on page 8-43
- "Vectorize Option" on page 8-44

Genetic Algorithm Tool vs. Command Line

There are two ways to specify options for the genetic algorithm, depending on whether you are using the Genetic Algorithm Tool or calling the functions ga or at the command line:

- If you are using the Genetic Algorithm Tool (gatoo1), select an option from a drop-down list or enter the value of the option in a text field. See "Setting Options in the Genetic Algorithm Tool" on page 6-13.
- If you are calling ga or gamultiobj from the command line, create an options structure using the function gaoptimset, as follows:

```
options = gaoptimset('Param1', value1, 'Param2', value2, ...);
```

See "Setting Options for ga at the Command Line" on page 6-24 for examples.

In this section, each option is listed in two ways:

- By its label, as it appears in the Genetic Algorithm Tool
- By its field name in the options structure

For example:

- **Population type** is the label of the option in the Genetic Algorithm Tool.
- PopulationType is the corresponding field of the options structure.

Plot Options

Plot options enable you to plot data from the genetic algorithm while it is running. When you select plot functions and run the genetic algorithm, a plot window displays the plots on separate axes. Click on any subplot to view a larger version of the plot in a separate figure window. You can stop the algorithm at any time by clicking the **Stop** button on the plot window.

Plot interval (PlotInterval) specifies the number of generations between consecutive calls to the plot function.

You can select any of the following plot functions in the **Plots** pane:

- **Best fitness** (@gaplotbestf) plots the best function value versus generation.
- Expectation (@gaplotexpectation) plots the expected number of children versus the raw scores at each generation.
- Score diversity (@gaplotscorediversity) plots a histogram of the scores at each generation.
- **Stopping** (@plotstopping) plots stopping criteria levels.
- Best individual (@gaplotbestindiv) plots the vector entries of the individual with the best fitness function value in each generation.

- **Genealogy** (@gaplotgenealogy) plots the genealogy of individuals. Lines from one generation to the next are color-coded as follows:
 - Red lines indicate mutation children.
 - Blue lines indicate crossover children.
 - Black lines indicate elite individuals.
- **Scores** (@gaplotscores) plots the scores of the individuals at each generation.
- Max constraint (@gaplotmaxconstr) plots the maximum nonlinear constraint violation at each generation.
- **Distance** (@gaplotdistance) plots the average distance between individuals at each generation.
- **Range** (@gaplotrange) plots the minimum, maximum, and mean fitness function values in each generation.
- **Selection** (@gaplotselection) plots a histogram of the parents.
- **Custom function** enables you to use plot functions of your own. To specify the plot function if you are using the Genetic Algorithm Tool,
 - Select Custom function.
 - Enter @myfun in the text box, where myfun is the name of your function.

See "Structure of the Plot Functions" on page 8-26.

To display a plot when calling ga from the command line, set the PlotFcns field of options to be a function handle to the plot function. For example, to display the best fitness plot, set options as follows

```
options = gaoptimset('PlotFcns', @gaplotbestf);
```

To display multiple plots, use the syntax

```
options =gaoptimset('PlotFcns', {@plotfun1, @plotfun2, ...});
```

where @plotfun1, @plotfun2, and so on are function handles to the plot functions.

Structure of the Plot Functions

The first line of a plot function has the form

```
function state = plotfun(options, state, flag)
```

The input arguments to the function are

- options Structure containing all the current options settings.
- state Structure containing information about the current generation. "The State Structure" on page 8-26 describes the fields of state.
- flag String that tells what stage the algorithm is currently in.

"Parameterizing Functions Called by patternsearch" on page 5-52 explains how to provide additional parameters to the function.

The State Structure

The state structure, which is an input argument to plot, mutation, and output functions, contains the following fields:

- Population Population in the current generation
- Score Scores of the current population
- Generation Current generation number
- StartTime Time when genetic algorithm started
- StopFlag String containing the reason for stopping
- Selection Indices of individuals selected for elite, crossover and mutation
- Expectation Expectation for selection of individuals
- Best Vector containing the best score in each generation
- LastImprovement Generation at which the last improvement in fitness value occurred
- LastImprovementTime Time at which last improvement occurred
- NonlinIneq Nonlinear inequality constraints, displayed only when a nonlinear constraint function is specified

 NonlinEq — Nonlinear equality constraints, displayed only when a nonlinear constraint function is specified

Population Options

Population options enable you to specify the parameters of the population that the genetic algorithm uses.

Population type (PopulationType) specifies the data type of the input to the fitness function. You can set **Population type** to be one of the following:

- Double Vector ('doubleVector') Use this option if the individuals in the population have type double. This is the default.
- Bit string ('bitstring') Use this option if the individuals in the population are bit strings.
- Custom('custom') Use this option to create a population whose data type is neither of the preceding.

If you use a custom population type, you must write your own creation, mutation, and crossover functions that accept inputs of that population type, and specify these functions in the following fields, respectively:

- Creation function (CreationFcn)
- Mutation function (MutationFcn)
- Crossover function (CrossoverFcn)

Population size (PopulationSize) specifies how many individuals there are in each generation. With a large population size, the genetic algorithm searches the solution space more thoroughly, thereby reducing the chance that the algorithm will return a local minimum that is not a global minimum. However, a large population size also causes the algorithm to run more slowly.

If you set **Population size** to a vector, the genetic algorithm creates multiple subpopulations, the number of which is the length of the vector. The size of each subpopulation is the corresponding entry of the vector.

Creation function (CreationFcn) specifies the function that creates the initial population for ga. You can choose from the following functions:

- Uniform (@gacreationuniform) creates a random initial population with a uniform distribution. This is the default.
- Custom enables you to write your own creation function, which must generate data of the type that you specify in **Population type**. To specify the creation function if you are using the Genetic Algorithm Tool,
 - Set Creation function to Custom.
 - Set Function name to @myfun, where myfun is the name of your function.

If you are using ga, set

```
options = gaoptimset('CreationFcn', @myfun);
```

Your creation function must have the following calling syntax.

```
function Population = myfun(GenomeLength, FitnessFcn, options)
```

The input arguments to the function are

- Genomelength Number of independent variables for the fitness function
- FitnessFcn Fitness function
- options Options structure

The function returns Population, the initial population for the genetic algorithm.

"Parameterizing Functions Called by patternsearch" on page 5-52 explains how to provide additional parameters to the function.

Initial population (InitialPopulation) specifies an initial population for the genetic algorithm. The default value is [], in which case ga uses the **Creation function** to create an initial population. If you enter a nonempty array in the **Initial population** field, the array must have **Population size** rows and **Number of variables** columns. In this case, the genetic algorithm does not call the **Creation function**. The initial population can be partial.

Initial scores (InitialScores) specifies initial scores for the initial population. The initial scores can also be partial.

Initial range (PopInitRange) specifies the range of the vectors in the initial population that is generated by the creation function. You can set Initial range to be a matrix with two rows and Number of variables columns, each column of which has the form [1b; ub], where 1b is the lower bound and ub is the upper bound for the entries in that coordinate. If you specify Initial range to be a 2-by-1 vector, each entry is expanded to a constant row of length Number of variables.

See "Example — Setting the Initial Range" on page 6-33 for an example.

Fitness Scaling Options

Fitness scaling converts the raw fitness scores that are returned by the fitness function to values in a range that is suitable for the selection function. You can specify options for fitness scaling in the **Fitness scaling** pane.

Scaling function (FitnessScalingFcn) specifies the function that performs the scaling. The options are

- Rank (@fitscalingrank) The default fitness scaling function, Rank, scales the raw scores based on the rank of each individual instead of its score. The rank of an individual is its position in the sorted scores. The rank of the most fit individual is 1, the next most fit is 2, and so on. Rank fitness scaling removes the effect of the spread of the raw scores.
- Proportional (@fitscalingprop) Proportional scaling makes the scaled value of an individual proportional to its raw fitness score.
- Top (@fitscalingtop) Top scaling scales the top individuals equally. Selecting Top displays an additional field, **Quantity**, which specifies the number of individuals that are assigned positive scaled values. **Quantity** can be an integer between 1 and the population size or a fraction between 0 and 1 specifying a fraction of the population size. The default value is 0.4. Each of the individuals that produce offspring is assigned an equal scaled value, while the rest are assigned the value 0. The scaled values have the form [0 1/n 1/n 0 0 1/n 0 0 1/n ...].

To change the default value for **Quantity** at the command line, use the following syntax

```
options = gaoptimset('FitnessScalingFcn', {@fitscalingtop,
    quantity})
```

where quantity is the value of **Quantity**.

• Shift linear (@fitscalingshiftlinear) — Shift linear scaling scales the raw scores so that the expectation of the fittest individual is equal to a constant multiplied by the average score. You specify the constant in the **Max survival rate** field, which is displayed when you select Shift linear. The default value is 2.

To change the default value of **Max survival rate** at the command line, use the following syntax

```
options = gaoptimset('FitnessScalingFcn',
{@fitscalingshiftlinear, rate})
```

where rate is the value of Max survival rate.

- Custom enables you to write your own scaling function. To specify the scaling function using the Genetic Algorithm Tool,
 - Set Scaling function to Custom.
 - Set **Function name** to @myfun, where myfun is the name of your function.

If you are using ga at the command line, set

```
options = gaoptimset('FitnessScalingFcn', @myfun);
```

Your scaling function must have the following calling syntax:

```
function expection = myfun(scores, nParents)
```

The input arguments to the function are

- scores A vector of scalars, one for each member of the population
- nParents The number of parents needed from this population

The function returns expectation, a row vector of scalars of the same length as scores, giving the scaled values of each member of the population. The sum of the entries of expectation must equal nParents.

"Parameterizing Functions Called by patternsearch" on page 5-52 explains how to provide additional parameters to the function.

See "Fitness Scaling" on page 6-37 for more information.

Selection Options

Selection options specify how the genetic algorithm chooses parents for the next generation. You can specify the function the algorithm uses in the **Selection function** (SelectionFcn) field in the **Selection** options pane. The options are

- Stochastic uniform (@selectionstochunif) The default selection function, Stochastic uniform, lays out a line in which each parent corresponds to a section of the line of length proportional to its scaled value. The algorithm moves along the line in steps of equal size. At each step, the algorithm allocates a parent from the section it lands on. The first step is a uniform random number less than the step size.
- Remainder (@selectionremainder) Remainder selection assigns parents deterministically from the integer part of each individual's scaled value and then uses roulette selection on the remaining fractional part. For example, if the scaled value of an individual is 2.3, that individual is listed twice as a parent because the integer part is 2. After parents have been assigned according to the integer parts of the scaled values, the rest of the parents are chosen stochastically. The probability that a parent is chosen in this step is proportional to the fractional part of its scaled value.
- Uniform (@selectionuniform) Uniform selection chooses parents using the expectations and number of parents. Uniform selection is useful for debugging and testing, but is not a very effective search strategy.
- Roulette (@selectionroulette) Roulette selection chooses parents
 by simulating a roulette wheel, in which the area of the section of the
 wheel corresponding to an individual is proportional to the individual's
 expectation. The algorithm uses a random number to select one of the
 sections with a probability equal to its area.
- Tournament (@selectiontournament) Tournament selection chooses each parent by choosing **Tournament size** players at random and then choosing the best individual out of that set to be a parent. **Tournament size** must be at least 2. The default value of **Tournament size** is 4.

To change the default value of **Tournament size** at the command line, use the syntax

```
options = gaoptimset('SelectionFcn',...
                     {@selecttournament, size})
```

where size is the value of **Tournament size**.

- Custom enables you to write your own selection function. To specify the selection function using the Genetic Algorithm Tool,
 - Set Selection function to Custom.
 - Set **Function name** to @myfun, where myfun is the name of your function.

If you are using ga at the command line, set

```
options = gaoptimset('SelectionFcn', @myfun);
```

Your selection function must have the following calling syntax:

```
function parents = myfun(expectation, nParents, options)
```

The input arguments to the function are

- expectation Expected number of children for each member of the population
- nParents Number of parents to select
- options Genetic algorithm options structure

The function returns parents, a row vector of length nParents containing the indices of the parents that you select.

"Parameterizing Functions Called by patternsearch" on page 5-52 explains how to provide additional parameters to the function.

See "Selection" on page 6-40 for more information.

Reproduction Options

Reproduction options specify how the genetic algorithm creates children for the next generation.

Elite count (EliteCount) specifies the number of individuals that are guaranteed to survive to the next generation. Set **Elite count** to be a positive integer less than or equal to the population size. The default value is 2.

Crossover fraction (CrossoverFraction) specifies the fraction of the next generation, other than elite children, that are produced by crossover. Set **Crossover fraction** to be a fraction between 0 and 1, either by entering the fraction in the text box or moving the slider. The default value is 0.8.

See "Setting the Crossover Fraction" on page 6-44 for an example.

Mutation Options

Mutation options specify how the genetic algorithm makes small random changes in the individuals in the population to create mutation children. Mutation provides genetic diversity and enable the genetic algorithm to search a broader space. You can specify the mutation function in the **Mutation function** (MutationFcn) field in the **Mutation** options pane. You can choose from the following functions:

- Gaussian (mutationgaussian) The default mutation function, Gaussian, adds a random number taken from a Gaussian distribution with mean 0 to each entry of the parent vector. The variance of this distribution is determined by the parameters Scale and Shrink, which are displayed when you select Gaussian, and by the Initial range setting in the Population options.
 - The **Scale** parameter determines the variance at the first generation. If you set **Initial range** to be a 2-by-1 vector v, the initial variance is the same at all coordinates of the parent vector, and is given by **Scale***(v(2) v(1)).
 - If you set **Initial range** to be a vector v with two rows and **Number of variables** columns, the initial variance at coordinate i of the parent vector is given by **Scale***(v(i,2) v(i,1)).
 - The Shrink parameter controls how the variance shrinks as generations go by. If you set Initial range to be a 2-by-1 vector, the variance at the kth generation, var_k, is the same at all coordinates of the parent vector, and is given by the recursive formula

$$var_k = var_{k-1} \left(1 - \text{Shrink} \cdot \frac{k}{\text{Generations}} \right)$$

If you set **Initial range** to be a vector with two rows and **Number of variables** columns, the variance at coordinate i of the parent vector at the k^{th} generation, $var_{i,b}$, is given by the recursive formula

$$var_{i,k} = var_{i,k-1} \left(1 - \text{Shrink} \cdot \frac{k}{\text{Generations}} \right)$$

If you set **Shrink** to 1, the algorithm shrinks the variance in each coordinate linearly until it reaches 0 at the last generation is reached. A negative value of **Shrink** causes the variance to grow.

The default values of **Scale** and **Shrink** are 0.5 and 0.75, respectively. To change these default values at the command line, use the syntax

```
options = gaoptimset('MutationFcn', ...
{@mutationgaussian, scale, shrink})
```

where scale and shrink are the values of Scale and Shrink, respectively.

Uniform (mutationuniform) — Uniform mutation is a two-step process.
 First, the algorithm selects a fraction of the vector entries of an individual
 for mutation, where each entry has a probability **Rate** of being mutated.
 The default value of **Rate** is 0.01. In the second step, the algorithm
 replaces each selected entry by a random number selected uniformly from
 the range for that entry.

To change the default value of **Rate** at the command line, use the syntax

```
options = gaoptimset('MutationFcn', {@mutationuniform, rate})
```

where rate is the value of **Rate**.

- Adaptive Feasible (mutationadaptfeasible) randomly generates directions that are adaptive with respect to the last successful or unsuccessful generation. The feasible region is bounded by the constraints and inequality constraints. A step length is chosen along each direction so that linear constraints and bounds are satisfied.
- Custom enables you to write your own mutation function. To specify the mutation function using the Genetic Algorithm Tool,

- Set Mutation function to Custom.
- Set Function name to @myfun, where myfun is the name of your function.

If you are using ga, set

```
options = gaoptimset('MutationFcn', @myfun);
```

Your mutation function must have this calling syntax:

```
function mutationChildren = myfun(parents, options, nvars,
FitnessFcn, state, thisScore, thisPopulation)
```

The arguments to the function are

- parents Row vector of parents chosen by the selection function
- options Options structure
- nvars Number of variables
- FitnessFcn Fitness function
- state Structure containing information about the current generation.
 "The State Structure" on page 8-26 describes the fields of state.
- thisScore Vector of scores of the current population
- thisPopulation Matrix of individuals in the current population

The function returns mutationChildren—the mutated offspring—as a matrix whose rows correspond to the children. The number of columns of the matrix is **Number of variables**.

"Parameterizing Functions Called by patternsearch" on page 5-52 explains how to provide additional parameters to the function.

Crossover Options

Crossover options specify how the genetic algorithm combines two individuals, or parents, to form a crossover child for the next generation.

Crossover function (CrossoverFcn) specifies the function that performs the crossover. You can choose from the following functions:

• Scattered (@crossoverscattered), the default crossover function, creates a random binary vector and selects the genes where the vector is a 1 from the first parent, and the genes where the vector is a 0 from the second parent, and combines the genes to form the child. For example, if p1 and p2 are the parents

```
p1 = [a b c d e f g h]

p2 = [1 2 3 4 5 6 7 8]
```

and the binary vector is $[1\ 1\ 0\ 0\ 1\ 0\ 0]$, the function returns the following child:

```
child1 = [a b 3 4 e 6 7 8]
```

- Single point (@crossoversinglepoint) chooses a random integer n between 1 and **Number of variables** and then
 - Selects vector entries numbered less than or equal to n from the first parent.
 - Selects vector entries numbered greater than n from the second parent.
 - Concatenates these entries to form a child vector.

For example, if p1 and p2 are the parents

```
p1 = [a b c d e f g h]

p2 = [1 2 3 4 5 6 7 8]
```

and the crossover point is 3, the function returns the following child.

```
child = [a b c 4 5 6 7 8]
```

- Two point (@crossovertwopoint) selects two random integers m and n between 1 and Number of variables. The function selects
 - Vector entries numbered less than or equal to m from the first parent
 - Vector entries numbered from m+1 to n, inclusive, from the second parent
 - Vector entries numbered greater than n from the first parent.

The algorithm then concatenates these genes to form a single gene. For example, if p1 and p2 are the parents

```
p1 = [a b c d e f g h]

p2 = [1 2 3 4 5 6 7 8]
```

and the crossover points are 3 and 6, the function returns the following child.

```
child = [a b c 4 5 6 g h]
```

• Intermediate (@crossoverintermediate) creates children by taking a weighted average of the parents. You can specify the weights by a single parameter, **Ratio**, which can be a scalar or a row vector of length **Number of variables**. The default is a vector of all 1's. The function creates the child from parent1 and parent2 using the following formula.

```
child = parent1 + rand * Ratio * ( parent2 - parent1)
```

If all the entries of **Ratio** lie in the range [0, 1], the children produced are within the hypercube defined by placing the parents at opposite vertices. If **Ratio** is not in that range, the children might lie outside the hypercube. If **Ratio** is a scalar, then all the children lie on the line between the parents.

To change the default value of **Ratio** at the command line, use the syntax

```
options = gaoptimset('CrossoverFcn', ...
{@crossoverintermediate, ratio});
```

where ratio is the value of **Ratio**.

• Heuristic (@crossoverheuristic) returns a child that lies on the line containing the two parents, a small distance away from the parent with the better fitness value in the direction away from the parent with the worse fitness value. You can specify how far the child is from the better parent by the parameter Ratio, which appears when you select Heuristic. The default value of Ratio is 1.2. If parent1 and parent2 are the parents, and parent1 has the better fitness value, the function returns the child

```
child = parent2 + R * (parent1 - parent2);
```

To change the default value of **Ratio** at the command line, use the syntax

```
options=gaoptimset('CrossoverFcn',...
{@crossoverheuristic,ratio});
```

where ratio is the value of **Ratio**.

- Arithmetic (@crossoverarithmetic) creates children that are the weighted arithmetic mean of two parents. Children are always feasible with respect to linear constraints and bounds.
- Custom enables you to write your own crossover function. To specify the crossover function using the Genetic Algorithm Tool,
 - Set Crossover function to Custom.
 - Set **Function name** to @myfun, where myfun is the name of your function.

If you are using ga, set

```
options = gaoptimset('CrossoverFcn', @myfun);
```

Your selection function must have the following calling syntax.

```
xoverKids = myfun(parents, options, nvars, FitnessFcn,
unused, this Population)
```

The arguments to the function are

- parents Row vector of parents chosen by the selection function
- options options structure
- nvars Number of variables
- FitnessFcn Fitness function
- unused Placeholder not used
- thisPopulation Matrix representing the current population. The number of rows of the matrix is **Population size** and the number of columns is Number of variables.

The function returns xoverKids—the crossover offspring—as a matrix whose rows correspond to the children. The number of columns of the matrix is **Number of variables**.

"Parameterizing Functions Called by patternsearch" on page 5-52 explains how to provide additional parameters to the function.

Migration Options

Migration options specify how individuals move between subpopulations. Migration occurs if you set **Population size** to be a vector of length greater than 1. When migration occurs, the best individuals from one subpopulation replace the worst individuals in another subpopulation. Individuals that migrate from one subpopulation to another are copied. They are not removed from the source subpopulation.

You can control how migration occurs by the following three fields in the **Migration** options pane:

- **Direction** (MigrationDirection) Migration can take place in one or both directions.
 - If you set **Direction** to Forward ('forward'), migration takes place toward the last subpopulation. That is, the nth subpopulation migrates into the (n+1)th subpopulation.
 - If you set **Direction** to Both ('both'), the nth subpopulation migrates into both the (n-1)th and the (n+1)th subpopulation.

Migration wraps at the ends of the subpopulations. That is, the last subpopulation migrates into the first, and the first may migrate into the last.

- Interval (MigrationInterval) Specifies how many generation pass between migrations. For example, if you set Interval to 20, migration takes place every 20 generations.
- **Fraction** (MigrationFraction) Specifies how many individuals move between subpopulations. **Fraction** specifies the fraction of the smaller of the two subpopulations that moves. For example, if individuals migrate from a subpopulation of 50 individuals into a subpopulation of 100 individuals and you set **Fraction** to 0.1, the number of individuals that migrate is 0.1 * 50 = 5.

Algorithm Settings

Algorithm settings define algorithmic specific parameters.

Parameters that can be specified for a nonlinear constraint algorithm include

- **Initial penalty** (InitialPenalty) Specifies an initial value of the penalty parameter that is used by the algorithm. **Initial penalty** must be greater than or equal to 1.
- **Penalty factor** (PenaltyFactor) Increases the penalty parameter when the problem is not solved to required accuracy and constraints are not satisfied. **Penalty factor** must be greater than 1.

Multiobjective Options

Multiobjective options define parameters characteristic of the multiobjective genetic algorithm. You can specify the following parameters:

- DistanceMeasureFcn Defines a handle to the function that computes distance measure of individuals, computed in decision variable or design space (genotype) or in function space (phenotype). For example, the default distance measure function is distancecrowding in function space, or {@distancecrowding,'phenotype'}.
- ParetoFraction Sets the fraction of individuals to keep on the first Pareto front while the solver selects individuals from higher fronts. This option is a scalar between 0 and 1.

Hybrid Function Options

A hybrid function is another minimization function that runs after the genetic algorithm terminates. You can specify a hybrid function in **Hybrid function** (HybridFcn) options. The choices are

- [] No hybrid function
- fminsearch (@fminsearch) Uses the MATLAB function fminsearch to perform unconstrained minimization
- patternsearch (@patternsearch) Uses a pattern search to perform constrained or unconstrained minimization
- fminunc (@fminunc) Uses the Optimization Toolbox function fminunc to perform unconstrained minimization
- fmincon (@fmincon) Uses the Optimization Toolbox function fmincon to perform constrained minimization

See "Using a Hybrid Function" on page 6-54 for an example.

Stopping Criteria Options

Stopping criteria determine what causes the algorithm to terminate. You can specify the following options:

- **Generations** (Generations) Specifies the maximum number of iterations the genetic algorithm will perform. The default is 100.
- **Time limit** (TimeLimit) Specifies the maximum time in seconds the genetic algorithm runs before stopping.
- **Fitness limit** (FitnessLimit) The algorithm stops if the best fitness value is less than or equal to the value of **Fitness limit**.
- **Stall generations** (StallGenLimit) The algorithm stops if the weighted average change in the fitness function value over **Stall generations** is less than **Function tolerance**.
- **Stall time limit** (StallTimeLimit) The algorithm stops if there is no improvement in the best fitness value for an interval of time in seconds specified by **Stall time**.
- Function tolerance (TolFun) The algorithm runs until the cumulative change in the fitness function value over **Stall generations** is less than **Function Tolerance**.
- **Nonlinear constraint tolerance** (TolCon) The **Nonlinear constraint tolerance** is not used as stopping criterion. It is used to determine the feasibility with respect to nonlinear constraints.

See "Setting the Maximum Number of Generations" on page 6-57 for an example.

Output Function Options

Output functions are functions that the genetic algorithm calls at each generation. The following options are available:

History to new window (@gaoutputgen) displays the history of points computed by the algorithm in a new window at each multiple of **Interval** iterations.

Custom enables you to write your own output function. To specify the output function using the Genetic Algorithm Tool,

- Select Custom function.
- Enter @myfun in the text box, where myfun is the name of your function.

If you are using ga, set

```
options = gaoptimset('OutputFcn', @myfun);
```

To see a template that you can use to write your own output functions, enter

```
edit gaoutputfcntemplate
```

at the MATLAB command line.

For information on output function options available with pattern search, see "Output Function Options" on page 8-15 in Pattern Search Options.

Structure of the Output Function

The output function has the following calling syntax.

```
[state, options,optchanged] = myfun(options,state,flag,interval)
```

The function has the following input arguments:

- options Options structure
- state Structure containing information about the current generation. "The State Structure" on page 8-26 describes the fields of state.
- flag String indicating the current status of the algorithm as follows:
 - 'init' Initial stage
 - 'iter' Algorithm running
 - 'interrupt' Intermediate stage
 - 'done' Algorithm terminated
- interval Optional interval argument

[&]quot;Parameterizing Functions Called by patternsearch" on page 5-52 explains how to provide additional parameters to the function.

The output function returns the following arguments to ga:

- state Structure containing information about the current generation
- options Options structure modified by the output function. This argument is optional.
- optchanged Flag indicating changes to options

Display to Command Window Options

Level of display ('Display') specifies how much information is displayed at the command line while the genetic algorithm is running. The available options are

- Off ('off') No output is displayed.
- Iterative ('iter') Information is displayed at each iteration.
- Diagnose ('diagnose') Information is displayed at each iteration. In addition, the diagnostic lists some problem information and the options that have been changed from the defaults.
- Final ('final') The reason for stopping is displayed.

Both Iterative and Diagnose display the following information:

- Generation Generation number
- f-count Cumulative number of fitness function evaluations
- Best f(x) Best fitness function value
- Mean f(x) Mean fitness function value
- Stall generations Number of generations since the last improvement of the fitness function

When a nonlinear constraint function has been specified, Iterative and Diagnose will not display the Mean f(x), but will additionally display:

• Max Constraint — Maximum nonlinear constraint violation

The default value of **Level of display** is

- Off in the Genetic Algorithm Tool
- 'final' in an options structure created using gaoptimset

Vectorize Option

The vectorize option specifies whether the computation of the fitness function is vectorized. Set **Set Objective function is vectorized** to 0n to indicate that the fitness function is vectorized. When **Objective function is** vectorized is Off, the algorithm calls the fitness function on one individual at a time as it loops through the population.

See "Vectorizing the Fitness Function" on page 6-58 for an example.

Simulated Annealing and Threshold Acceptance Algorithm Options

In this section...

"saoptimset At The Command Line" on page 8-45

"Plot Options" on page 8-45

"Temperature Options" on page 8-47

"Algorithm Settings" on page 8-48

"Hybrid Function Options" on page 8-49

"Stopping Criteria Options" on page 8-49

"Output Function Options" on page 8-50

"Display Options" on page 8-51

saoptimset At The Command Line

You specify options by creating an options structure using the function saoptimset, as follows:

```
options = saoptimset('Param1', value1, 'Param2', value2, ...);
```

See "Setting Options for simulannealbnd and threshacceptbnd at the Command Line" on page 7-3 for examples.

Each option in this section is listed by its field name in the options structure. For example, InitialTemperature refers to the corresponding field of the options structure.

Plot Options

Plot options enable you to plot data from the simulated annealing or threshold acceptance solver while it is running. When you specify plot functions and run the algorithm, a plot window displays the plots on separate axes. Right-click on any subplot to view a larger version of the plot in a separate figure window.

PlotInterval specifies the number of iterations between consecutive calls to the plot function.

To display a plot when calling simulannealbnd or threshacceptbnd from the command line, set the PlotFcns field of options to be a function handle to the plot function. You can specify any of the following plots:

- @saplotbestf plots the best objective function value.
- @saplotbestx plots the current best point.
- @saplotf plots the current function value.
- @saplotx plots the current point.
- @saplotstopping plots stopping criteria levels.
- @saplottemperature plots the temperature at each iteration.
- @myfun plots a custom plot function, where myfun is the name of your function. See "Structure of the Plot Functions" on page 8-4 for a description of the syntax.

For example, to display the best objective plot, set options as follows

```
options = saoptimset('PlotFcns', @saplotbestf);
```

To display multiple plots, use the cell array syntax

```
options = saoptimset('PlotFcns', {@plotfun1, @plotfun2, ...});
```

where @plotfun1, @plotfun2, and so on are function handles to the plot functions.

Structure of the Plot Functions

The first line of a plot function has the form

```
function stop = plotfun(options, optimvalues, flag)
```

The input arguments to the function are

options — Options structure created using saoptimset.

- optimvalues Structure containing information about the current state of the solver. The structure contains the following fields:
 - x Current point
 - fval Objective function value at x
 - bestx Best point found so far
 - bestfval Objective function value at best point
 - temperature Current temperature
 - iteration Current iteration
 - funccount Number of function evaluations
 - t0 Start time for algorithm
 - k Annealing parameter
 - tau Threshold acceptance sequence (for threshold acceptance solver only)
- flag Current state in which the plot function is called. The possible values for flag are
 - 'init' Initialization state
 - 'iter' Iteration state
 - 'done' Final state

The output argument stop provides a way to stop the algorithm at the current iteration. stop can have the following values:

- false The algorithm continues to the next iteration.
- $\bullet\,$ true The algorithm terminates at the current iteration.

Temperature Options

Temperature options specify how the temperature will be lowered at each iteration over the course of the algorithm.

InitialTemperature — Initial temperature at the start of the algorithm.
 The default is 100.

- TemperatureFcn Function used to update the temperature schedule.
 The choices are:
 - @temperatureexp The temperature at an iteration is reduced exponentially at each iteration. This is the default.
 - @temperaturefast Uses the fast annealing function.
 - @temperaturebolz Uses the Boltzmann annealing function.
 - @myfun Uses a custom function, myfun, to update temperature. See the functions above for syntax.
- ReannealInterval Number of points accepted before reannealing. The default value is 100.

Algorithm Settings

Algorithm settings define algorithmic specific parameters used in generating new points at each iteration.

Parameters that can be specified for the simulated annealing and threshold acceptance algorithms are:

- AnnealingFcn Function used to generate new points for the next iteration. The choices are:
 - @annealingfast Uses the fast annealing algorithm. This is the default.
 - @annealingbolz Uses the Boltzmann annealing algorithm.
 - @myfun Uses a custom annealing algorithm, myfun. See the functions above for syntax.

AcceptanceFcn — Function used to determine whether a new point is accepted or not. The default function varies depending on which solver/algorithm you are using. The choices are:

- @acceptancesa Simulated annealing acceptance function. The default for simulannealbnd. This function cannot be used with threshacceptbnd.
- @acceptancethresh Threshold acceptance function. The default for threshacceptbnd. This function cannot be used with simulannealbnd.

 @myfun — A custom acceptance function, myfun. See the functions above for syntax.

Hybrid Function Options

A hybrid function is another minimization function that runs during or at the end of iterations of the solver. You can specify a hybrid function using the HybridFcn option. The choices are

- [] No hybrid function
- @fminsearch Uses the MATLAB function fminsearch to perform unconstrained minimization
- @patternsearch Uses patternsearch to perform constrained or unconstrained minimization
- @fminunc Uses the Optimization Toolbox function fminunc to perform unconstrained minimization
- @fmincon Uses the Optimization Toolbox function fmincon to perform constrained minimization

HybridInterval specifies the interval (if not never or end) at which the hybrid function is called.

Stopping Criteria Options

Stopping criteria determine what causes the algorithm to terminate. You can specify the following options:

- TolFun The algorithm runs until the average change in value of the objective function in StallIterLim iterations is less than TolFun. The default value is 1e-6.
- MaxIter The algorithm stops if the number of iterations exceeds this
 maximum number of iterations. You can specify the maximum number of
 iterations as a positive integer or Inf. Inf is the default.
- MaxFunEval specifies the maximum number of evaluations of the objective function. The algorithm stops if the number of function evaluations exceeds the maximum number of function evaluations. The allowed maximum is 3000*numberofvariables.

- TimeLimit specifies the maximum time in seconds the algorithm runs before stopping.
- ObjectiveLimit The algorithm stops if the best objective function value is less than or equal to the value of ObjectiveLimit.

Output Function Options

Output functions are functions that the algorithm calls at each iteration. The default value is to have no output function, []. You must first create an output function using the syntax described in "Structure of the Output Function" on page 8-50. Then, specify your function as @myfun, where myfun is the name of your function.

If you are using simulanneal, set

```
options = saoptimset('OutputFcns', @myfun);
```

To see a template that you can use to write your own output functions, enter

```
edit saoutputfcntemplate
```

at the MATLAB command line.

Structure of the Output Function

The output function has the following calling syntax.

```
[stop, options, optchanged] = myfun(options, optimvalues, flag)
```

The function has the following input arguments:

- options Options structure created using saoptimset.
- optimvalues Structure containing information about the current state of the solver. The structure contains the following fields:
 - x Current point
 - fval Objective function value at x
 - bestx Best point found so far
 - bestfval Objective function value at best point

- temperature Current temperature
- iteration Current iteration
- function Number of function evaluations
- t0 Start time for algorithm
- k Annealing parameter
- tau Threshold acceptance sequence (for threshold acceptance solver only)
- flag Current state in which the output function is called. The possible values for flag are
 - 'init' Initialization state
 - 'iter' Iteration state
 - 'done' Final state

The output function returns the following arguments:

- stop Provides a way to stop the algorithm at the current iteration. stop can have the following values:
 - false The algorithm continues to the next iteration.
 - true The algorithm terminates at the current iteration.
- $\bullet\,$ options Options structure modified by the output function.
- optchanged A boolean flag indicating changes were made to options. This must be set to true if options are changed.

Display Options

Use the Display option to specify how much information is displayed at the command line while the algorithm is running. The available options are

- off No output is displayed. This is the default value for an options structure created using saoptimset.
- iter Information is displayed at each iteration.

- diagnose Information is displayed at each iteration. In addition, the diagnostic lists some problem information and the options that have been changed from the defaults.
- final The reason for stopping is displayed. This is the default.

Both iter and diagnose display the following information:

- Iteration Iteration number
- f-count Cumulative number of objective function evaluations
- Best f(x) Best objective function value
- Current objective function value
- Mean Temperature Mean temperature function value

Functions — By Category

Genetic Algorithm (p. 9-2) Use genetic algorithm and Genetic

Algorithm Tool, and modify genetic

algorithm options

Direct Search (p. 9-2) Use direct search and Pattern Search

Tool, and modify pattern search

options

Simulated Annealing and Threshold

Acceptance Algorithms (p. 9-3)

Use simulated annealing and threshold acceptance algorithms,

and modify algorithm options

Genetic Algorithm

ga Find minimum of function using

genetic algorithm

gamultiobj Find minima of multiple functions

using genetic algorithm

gaoptimget Obtain values of genetic algorithm

options structure

gaoptimset Create genetic algorithm options

structure

gatool Open Genetic Algorithm Tool

Direct Search

patternsearch Find minimum of function using

pattern search

psearchtool Open Pattern Search Tool

psoptimget Obtain values of pattern search

options structure

psoptimset Create pattern search options

structure

Simulated Annealing and Threshold Acceptance Algorithms

saoptimget Values of simulated annealing or

threshold acceptance algorithm

options structure

saoptimset Create simulated annealing

algorithm or threshold acceptance

options structure

simulannealbnd Find unconstrained or

bound-constrained minimum of function of several variables using simulated annealing algorithm

threshacceptbnd Find unconstrained or

bound-constrained minimum of function of several variables using threshold acceptance algorithm

Functions — Alphabetical List

Purpose

Find minimum of function using genetic algorithm

Syntax

```
x = ga(fitnessfcn,nvars)
x = ga(fitnessfcn,nvars,A,b)
x = ga(fitnessfcn,nvars,A,b,Aeq,beq)
x = ga(fitnessfcn,nvars,A,b,Aeq,beq,LB,UB)
x = ga(fitnessfcn,nvars,A,b,Aeq,beq,LB,UB,nonlcon)
x = ga(fitnessfcn,nvars,A,b,Aeq,beq,LB,UB,nonlcon,options)
x = ga(problem)
[x, fval] = ga(...)
[x, fval, exitflag] = ga(...)
```

Description

ga implements the genetic algorithm at the command line to minimize an objective function.

x = ga(fitnessfcn, nvars) finds a local unconstrained minimum, x, to the objective function, fitnessfcn. nvars is the dimension (number of design variables) of fitnessfcn. The objective function, fitnessfcn, accepts a vector x of size 1-by-nvars, and returns a scalar evaluated at x.

Note To write a function with additional parameters to the independent variables that can be called by ga, see the section on "Parameterizing Functions Called by ga" on page 6-65.

x = ga(fitnessfcn, nvars, A, b) finds a local minimum x to fitnessfcn, subject to the linear inequalities $A*x \le b$. fitnessfcn accepts input x and returns a scalar function value evaluated at x.

If the problem has \boldsymbol{m} linear inequality constraints and \boldsymbol{n} variables, then

- A is a matrix of size m-by-n.
- b is a vector of length m.

Note that the linear constraints are not satisfied when the PopulationType option is set to 'bitString' or 'custom'.

x = ga(fitnessfcn,nvars,A,b,Aeq,beq) finds a local minimum x to fitnessfcn, subject to the linear equalities Aeq * x = beq as well as $A * x \le b$. (Set A=[] and b=[] if no inequalities exist.)

If the problem has r linear equality constraints and n variables, then

- Aeg is a matrix of size r-by-n.
- beg is a vector of length r.

Note that the linear constraints are not satisfied when the PopulationType option is set to 'bitString' or 'custom'.

x = ga(fitnessfcn,nvars,A,b,Aeq,beq,LB,UB) defines a set of lower and upper bounds on the design variables, x, so that a solution is found in the range $LB \le x \le UB$. Use empty matrices for LB and UB if no bounds exist. Set LB(i) = -Inf if x(i) is unbounded below; set UB(i) = Inf if x(i) is unbounded above.

x = ga(fitnessfcn,nvars,A,b,Aeq,beq,LB,UB,nonlcon) subjects the minimization to the constraints defined in nonlcon. The function nonlcon accepts x and returns the vectors C and Ceq, representing the nonlinear inequalities and equalities respectively. ga minimizes the fitnessfcn such that $C(x) \le 0$ and Ceq(x) = 0. (Set LB=[] and UB=[] if no bounds exist.)

Note that the nonlinear constraints are not satisfied when the PopulationType option is set to 'bitString' or 'custom'.

x = ga(fitnessfcn,nvars,A,b,Aeq,beq,LB,UB,nonlcon,options) minimizes with the default optimization parameters replaced by values in the structure options, which can be created using the gaoptimset function. See the gaoptimset reference page for details.

x = ga(problem) finds the minimum for problem, where problem is a structure containing the following fields:

fitnessfcn	Fitness function	
nvars	Number of design variables	

options	Options structure created using gaoptimset	
Aineq	A matrix for inequality constraints	
Bineq	b vector for inequality constraints	
Aeq	A matrix for equality constraints	
Beq	b vector for equality constraints	
LB	Lower bound on x	
UB	Upper bound on x	
nonlcon	Nonlinear constraint function	
randstate	Optional field to reset rand state	
randnstate	Optional field to reset randn state	

[x, fval] = ga(...) returns fval, the value of the fitness function at x.

[x, fval, exitflag] = ga(...) returns exitflag, an integer identifying the reason the algorithm terminated. The following lists the values of exitflag and the corresponding reasons the algorithm terminated.

- 1 Average cumulative change in value of the fitness function over options.StallGenLimit generations less than options.TolFun and constraint violation less than options.TolCon.
- 2 Fitness limit reached and constraint violation less than options.TolCon.
- 3 The value of the fitness function did not change in options.StallGenLimit generations and constraint violation less than options.TolCon.
- 4 Magnitude of step smaller than machine precision and constraint violation less than options.TolCon.
- 0 Maximum number of generations exceeded.
- ullet -1 Optimization terminated by the output or plot function.

- -2 No feasible point found.
- -4 Stall time limit exceeded.
- -5 Time limit exceeded.

[x, fval, exitflag, output] = ga(...) returns output, a structure that contains output from each generation and other information about the performance of the algorithm. The output structure contains the following fields:

- randstate The state of rand, the MATLAB random number generator, just before the algorithm started.
- randnstate The state of randn the MATLAB normal random number generator, just before the algorithm started. You can use the values of randstate and randnstate to reproduce the output of ga. See "Reproducing Your Results" on page 6-27.
- generations The number of generations computed.
- function The number of evaluations of the fitness function
- message The reason the algorithm terminated.
- maxconstraint Maximum constraint violation, if any.

[x, fval, exitflag, output, population] = ga(...) returns the matrix, population, whose rows are the final population.

[x, fval, exitflag, output, population, scores] = ga(...) returns scores the scores of the final population.

Note For problems that use the population type Double Vector (the default), ga does not accept functions whose inputs are of type complex. To solve problems involving complex data, write your functions so that they accept real vectors, by separating the real and imaginary parts.

Example

Given the following inequality constraints and lower bounds

$$\begin{bmatrix} 1 & 1 \\ -1 & 2 \\ 2 & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} \leq \begin{bmatrix} 2 \\ 2 \\ 3 \end{bmatrix}$$

$$\begin{bmatrix} 0 \le x_1 \\ 0 \le x_2 \end{bmatrix}$$

the following code finds the minimum of the function, lincontest6, that is provided with the toolbox:

References

[1] Goldberg, David E., Genetic Algorithms in Search, Optimization & Machine Learning, Addison-Wesley, 1989.

[2] A. R. Conn, N. I. M. Gould, and Ph. L. Toint. "A Globally Convergent Augmented Lagrangian Algorithm for Optimization with General

Constraints and Simple Bounds", SIAM Journal on Numerical Analysis, Volume 28, Number 2, pages 545–572, 1991.

[3] A. R. Conn, N. I. M. Gould, and Ph. L. Toint. "A Globally Convergent Augmented Lagrangian Barrier Algorithm for Optimization with General Inequality Constraints and Simple Bounds", *Mathematics of Computation*, Volume 66, Number 217, pages 261–288, 1997.

See Also

 $\label{eq:continuous} ga optim get, ga optim set, ga tool, patternsearch, simulanneal bnd, \\ threshaccept bnd$

Purpose

Find minima of multiple functions using genetic algorithm

Syntax

```
X = gamultiobj(FITNESSFCN,NVARS)
X = gamultiobj(FITNESSFCN,NVARS,A,b)
X = gamultiobj(FITNESSFCN,NVARS,A,b,Aeq,beq)
X = gamultiobj(FITNESSFCN,NVARS,A,b,Aeq,beq,LB,UB)
X = gamultiobj(FITNESSFCN,NVARS,A,b,Aeq,beq,LB,UB,options)
[X,FVAL] = gamultiobj(FITNESSFCN,NVARS, ...)
[X,FVAL,EXITFLAG] = gamultiobj(FITNESSFCN,NVARS, ...)
[X,FVAL,EXITFLAG,OUTPUT] = gamultiobj(FITNESSFCN,NVARS, ...)
[X,FVAL,EXITFLAG,OUTPUT,POPULATION] = gamultiobj(FITNESSFCN, ...)
[X,FVAL,EXITFLAG,OUTPUT,POPULATION,
SCORE] = gamultiobj(FITNESSFCN, ...)
```

Description

gamultiobj implements the genetic algorithm at the command line to minimize a multicomponent objective function.

X = gamultiobj (FITNESSFCN, NVARS) finds a local Pareto set X of the objective functions defined in FITNESSFCN. NVARS is the dimension of the optimization problem (number of decision variables). FITNESSFCN accepts a vector X of size 1-by-NVARS and returns a vector of size 1-by-numberOfObjectives evaluated at a decision variable. X is a matrix with NVARS columns. The number of rows in X is the same as the number of Pareto solutions. All solutions in a Pareto set are equally optimal; it is up to the designer to select a solution in the Pareto set depending on the application.

X = gamultiobj (FITNESSFCN, NVARS, A, b) finds a local Pareto set X of the objective functions defined in FITNESSFCN, subject to the linear inequalities $A*x \le b$. Linear constraints are supported only for the default PopulationType option ('doubleVector'). Other population types, e.g., 'bitString' and 'custom', are not supported.

X = gamultiobj(FITNESSFCN, NVARS, A, b, Aeq, beq) finds a local Pareto set X of the objective functions defined in FITNESSFCN, subject to the linear equalities Aeq *x = beq as well as the linear inequalities

 $A*x \le b$. (Set A=[] and b=[] if no inequalities exist.) Linear constraints are supported only for the default PopulationType option ('doubleVector'). Other population types, e.g., 'bitString' and 'custom', are not supported.

X = gamultiobj(FITNESSFCN, NVARS, A, b, Aeq, beq, LB, UB) defines a set of lower and upper bounds on the design variables X so that a local Pareto set is found in the range $LB \le x \le UB$. Use empty matrices for LB and UB if no bounds exist. Set LB(i) = -Inf if X(i) is unbounded below; set UB(i) = Inf if X(i) is unbounded above. Bound constraints are supported only for the default PopulationType option ('doubleVector'). Other population types, e.g., 'bitString' and 'custom', are not supported.

X = gamultiobj(FITNESSFCN, NVARS, A, b, Aeq, beq, LB, UB, options) finds a Pareto set X with the default optimization parameters replaced by values in the structure options. options can be created with the gaoptimset function.

[X,FVAL] = gamultiobj(FITNESSFCN,NVARS, ...) returns a matrix FVAL, the value of all the objective functions defined in FITNESSFCN at all the solutions in X. FVAL has numberOfObjectives columns and same number of rows as does X.

[X,FVAL,EXITFLAG] = gamultiobj(FITNESSFCN,NVARS, ...) returns EXITFLAG, which describes the exit condition of gamultiobj. Possible values of EXITFLAG and the corresponding exit conditions are listed in this table.

EXITFLAG Value	Exit Condition
1	Average change in value of the spread of Pareto set over options.StallGenLimit generations less than options.TolFun
0	Maximum number of generations exceeded
-1	Optimization terminated by the output or by the plot function

EXITFLAG Value	Exit Condition
-2	No feasible point found
- 5	Time limit exceeded

[X,FVAL,EXITFLAG,OUTPUT] = gamultiobj(FITNESSFCN,NVARS, ...) returns a structure OUTPUT with the following fields:

OUTPUT Field	Meaning
Output.randstate	State of the function rand used before the genetic algorithm started
Output.randnstate	State of the function randn used before the genetic algorithm started
Output.generations	Total number of generations, excluding HybridFcn iterations
Output.funccount	Total number of function evaluations
Output.maxconstraint	Maximum constraint violation, if any
Output.message	gamultiobj termination message

[X,FVAL,EXITFLAG,OUTPUT,POPULATION] = gamultiobj(FITNESSFCN, ...) returns the final POPULATION at termination.

[X,FVAL,EXITFLAG,OUTPUT,POPULATION,SCORE] = gamultiobj(FITNESSFCN, ...) returns the SCORE of the final POPULATION.

Example GA Multiobjective

This example optimizes two objectives defined by Schaffer's second function: a vector-valued function of two components and one input argument. The Pareto front is disconnected. Define this function in an M-file:

```
function y = schaffer2(x) % y has two columns
  % Initialize y for two objectives and for all x
  y = zeros(length(x), 2);
  % Evaluate first objective.
  % This objective is piecewise continuous.
  for i = 1:length(x)
      if x(i) \ll 1
          y(i,1) = -x(i);
      elseif x(i) \le 3
          y(i,1) = x(i) -2;
      elseif x(i) \le 4
          y(i,1) = 4 - x(i);
      else
          y(i,1) = x(i) - 4;
      end
  end
  % Evaluate second objective
  y(:,2) = (x -5).^2;
First, plot the two objectives:
  x = -1:0.1:8;
  y = schaffer2(x);
  plot(x,y(:,1),'.r'); hold on
  plot(x,y(:,2),'.b');
```

The two component functions compete in the range [1, 3] and [4, 5]. But the Pareto-optimal front consists of only two disconnected regions: [1, 2] and [4, 5]. This is because the region [2, 3] is inferior to [1, 2].

Next, impose a bound constraint on x, $-5 \le x \le 10$ setting

```
1b = -5;
ub = 10;
```

The best way to view the results of the genetic algorithm is to visualize the Pareto front directly using the <code>@gaplotpareto</code> option. To optimize Schaffer's function, a larger population size than the default (15) is needed, because of the disconnected front. This example uses 60. Set the optimization options as:

```
options = gaoptimset('PopulationSize',60,'PlotFcns',...
@gaplotpareto);
```

Now call gamultiobj, specifying one independent variable and only the bound constraints:

```
[x,f,exitflag] = gamultiobj(@schaffer2,1,[],[],[],[],...
lb,ub,options);
```

Optimization terminated: average change in the spread of Pareto solutions less than options.TolFun.

```
exitflag
exitflag = 1
```

The vectors x, f(:,1), and f(:,2) respectively contain the Pareto set and both objectives evaluated on the Pareto set.

Demos

The gamultiobjfitness demo solves a simple problem with one decision variable and two objectives.

The gamultiobjoptionsdemo demo shows how to set options for multiobjective optimization.

References

[1] Deb, Kalyanmoy. *Multi-Objective Optimization Using Evolutionary Algorithms*. John Wiley & Sons, 2001.

See Also

ga, gaoptimget, gaoptimset, patternsearch, @ (Special Characters), rand, randn

Purpose Obtain values of genetic algorithm options structure

Syntax val = gaoptimget(options, 'name')

val = gaoptimget(options, 'name', default)

Description

val = gaoptimget(options, 'name') returns the value of the
parameter name from the genetic algorithm options structure options.
gaoptimget(options, 'name') returns an empty matrix [] if the
value of name is not specified in options. It is only necessary to type
enough leading characters of name to uniquely identify it. gaoptimget
ignores case in parameter names.

val = gaoptimget(options, 'name', default) returns the 'name'
parameter, but will return the default value if the name parameter is
not specified (or is []) in options.

See Also

For more about these options, see "Genetic Algorithm Options" on page 8-23.

ga, gamultiobj, gaoptimset, gatool

Purpose

Create genetic algorithm options structure

Syntax

```
gaoptimset
```

options = gaoptimset

options = gaoptimset('param1',value1,'param2',value2,...)

options = gaoptimset(oldopts, 'param1', value1,...)

options = gaoptimset(oldopts,newopts)

Description

gaoptimset with no input or output arguments displays a complete list of parameters with their valid values.

options = gaoptimset (with no input arguments) creates a structure called options that contains the options, or *parameters*, for the genetic algorithm and sets parameters to [], indicating default values will be used.

options = gaoptimset('param1',value1,'param2',value2,...) creates a structure options and sets the value of 'param1' to value1, 'param2' to value2, and so on. Any unspecified parameters are set to their default values. It is sufficient to type only enough leading characters to define the parameter name uniquely. Case is ignored for parameter names.

options = gaoptimset(oldopts, 'param1', value1,...) creates a copy of oldopts, modifying the specified parameters with the specified values.

options = gaoptimset(oldopts, newopts) combines an existing options structure, oldopts, with a new options structure, newopts. Any parameters in newopts with nonempty values overwrite the corresponding old parameters in oldopts.

Options

The following table lists the options you can set with gaoptimset. See "Genetic Algorithm Options" on page 8-23 for a complete description of these options and their values. Values in {} denote the default value. You can also view the optimization parameters and defaults by typing gaoptimset at the command line.

Option	Description	Values
CreationFcn	Handle to the function that creates the initial population	{@gacreationuniform}
CrossoverFcn	Handle to the function that the algorithm uses to create crossover children	<pre>@crossoverheuristic {@crossoverscattered} @crossoverintermediate @crossoversinglepoint @crossovertwopoint @crossoverarithmetic</pre>
CrossoverFraction	The fraction of the population at the next generation, not including elite children, that is created by the crossover function	Positive scalar {0.8}
Display	Level of display	'off' 'iter' 'diagnose' {'final'}
DistanceMeasureFcn	Handle to the function that computes distance measure of individuals, computed in decision variable or design space (genotype) or in function space (phenotype)	{@distancecrowding, 'phenotype'}
EliteCount	Positive integer specifying how many individuals in the current generation are guaranteed to survive to the next generation	Positive integer {2}
FitnessLimit	Scalar. If the fitness function attains the value of FitnessLimit, the algorithm halts.	Scalar {-Inf}

gaoptimset

Option	Description	Values
FitnessScalingFcn	Handle to the function that scales the values of the fitness function	@fitscalingshiftlinear @fitscalingprop @fitscalingtop {@fitscalingrank}
Generations	Positive integer specifying the maximum number of iterations before the algorithm halts	Positive integer {100}
HybridFcn	Handle to a function that continues the optimization after ga terminates	Function handle @fminsearch @patternsearch @fminunc @fmincon {[]}
InitialPenalty	Initial value of penalty parameter	Positive scalar {10}
InitialPopulation	Initial population used to seed the genetic algorithm; can be partial	Matrix {[]}
InitialScores	Initial scores used to determine fitness; can be partial	Column vector {[]}
MigrationDirection	Direction of migration	'both' {'forward'}
MigrationFraction	Scalar between 0 and 1 specifying the fraction of individuals in each subpopulation that migrates to a different subpopulation	Scalar {0.2}
MigrationInterval	Positive integer specifying the number of generations that take place between migrations of individuals between subpopulations	Positive integer {20}

Option	Description	Values
MutationFcn	Handle to the function that produces mutation children	@mutationuniform @mutationadaptfeasible {@mutationgaussian}
OutputFcns	Functions that ga calls at each iteration	@gaoutputgen {[]}
ParetoFraction	Scalar between 0 and 1 specifying the fraction of individuals to keep on the first Pareto front while the solver selects individuals from higher fronts	Scalar {0.35}
PenaltyFactor	Penalty update parameter	Positive scalar {100}
PlotFcns	Array of handles to functions that plot data computed by the algorithm	@gaplotbestf @gaplotbestindiv @gaplotdistance @gaplotexpectation @gaplotgeneology @gaplotselection @gaplotrange @gaplotscorediversity @gaplotscores @gaplotstopping {[]}
PlotInterval	Positive integer specifying the number of generations between consecutive calls to the plot functions	Positive integer {1}
PopInitRange	Matrix or vector specifying the range of the individuals in the initial population	Matrix or vector [0;1]
PopulationSize	Size of the population	Positive integer {20}

gaoptimset

Option	Description	Values
PopulationType	String describing the data type of the population	'bitstring' 'custom' {'doubleVector'}
		Note that linear and nonlinear constraints are not satisfied when PopulationType is set to 'bitString' or 'custom'.
SelectionFcn	Handle to the function that selects parents of crossover and mutation children	@selectionremainder @selectionuniform {@selectionstochunif} @selectionroulette @selectiontournament
StallGenLimit	Positive integer. The algorithm stops if there is no improvement in the objective function for StallGenLimit consecutive generations.	Positive integer {50}
StallTimeLimit	Positive scalar. The algorithm stops if there is no improvement in the objective function for StallTimeLimit seconds.	Positive scalar {20}
TimeLimit	Positive scalar. The algorithm stops after running for TimeLimit seconds.	Positive scalar {Inf}
TolCon	Positive scalar. TolCon is used to determine the feasibility with respect to nonlinear constraints.	Positive scalar {1e-6}

Option	Description	Values
TolFun	Positive scalar. The algorithm runs until the cumulative change in the fitness function value over StallGenLimit is less than TolFun.	Positive scalar {1e-6}
Vectorized	String specifying whether the computation of the fitness function is vectorized	'on' {'off'}

See Also

For more about these options, see "Genetic Algorithm Options" on page 8-23.

ga, gamultiobj, gaoptimget, gatool

gatool

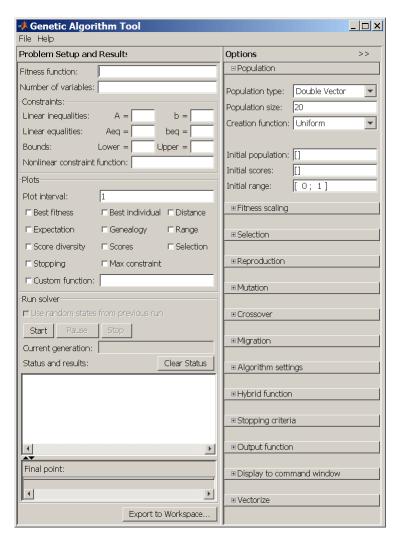
Purpose Open Genetic Algorithm Tool

Syntax gatool

gatool(optstruct)

Description gatool opens the Genetic Algorithm Tool, a graphical user interface

(GUI) to the genetic algorithm, as shown here.



gatool(optstruct) starts the Genetic Algorithm Tool with optstruct, which can be either a genetic algorithm options structure or genetic algorithm problem structure. An options structure can be created using gaoptimset.

gatool

gatool can run the genetic algorithm solver, ga on optimization problems, and it allows you to modify several ga options at run time, while you watch your results. See "Using the Genetic Algorithm Tool" on page 3-4 for a complete description of the tool.

See Also

ga, gaoptimget, gaoptimset, psearchtool

Purpose

Find minimum of function using pattern search

Syntax

```
x = patternsearch(@fun,x0)
x = patternsearch(@fun,x0,A,b)
x = patternsearch(@fun,x0,A,b,Aeq,beq)
x = patternsearch(@fun,x0,A,b,Aeq,beq,LB,UB)
x = patternsearch(@fun,x0,A,b,Aeq,beq,LB,UB,nonlcon)
x = patternsearch(@fun,x0,A,b,Aeq,beq,LB,UB,nonlcon,options)
x = patternsearch(problem)
[x, fval] = patternsearch(@fun,x0, ...)
[x, fval, exitflag] = patternsearch(@fun,x0, ...)
[x, fval, exitflag, output] = patternsearch(@fun,x0, ...)
```

Description

patternsearch finds the minimum of a function using a pattern search.

x = patternsearch(@fun,x0) finds the local minimum, x, to the MATLAB function, fun, that computes the values of the objective function f(x), and x0 is an initial point for the pattern search algorithm. The function patternsearch accepts the objective function as a function handle of the form @fun. The function fun accepts a vector input and returns a scalar function value.

Note To write a function with additional parameters to the independent variables that can be called by patternsearch, see the section on "Parameterizing Functions Called by patternsearch" on page 5-52.

x = patternsearch(@fun, x0, A, b) finds a local minimum x to the function fun, subject to the linear inequality constraints represented in matrix form by $Ax \le b$.

If the problem has m linear inequality constraints and n variables, then

- A is a matrix of size m-by-n.
- b is a vector of length m.

x = patternsearch(@fun, x0, A, b, Aeq, beq) finds a local minimum x to the function fun, starting at x0, and subject to the constraints

 $Ax \leq b$

Aeq * x = beq

where Aeq*x = beq represents the linear equality constraints in matrix form. If the problem has r linear equality constraints and n variables, then

- Aeq is a matrix of size r-by-n.
- beg is a vector of length r.

If there are no inequality constraints, pass empty matrices, [], for A and b.

x = patternsearch(@fun,x0,A,b,Aeq,beq,LB,UB) defines a set of lower and upper bounds on the design variables, x, so that a solution is found in the range $LB < \le x < \le UB$. If the problem has n variables, LB and UB are vectors of length n. If LB or UB is empty (or not provided), it is automatically expanded to -Inf or Inf, respectively. If there are no inequality or equality constraints, pass empty matrices for A, b, Aeq and beq.

x = patternsearch(@fun,x0,A,b,Aeq,beq,LB,UB,nonlcon) subjects the minimization to the constraints defined in nonlcon, a nonlinear constraint function. The function nonlcon accepts x and returns the vectors C and Ceq, representing the nonlinear inequalities and equalities respectively. fmincon minimizes fun such that $C(x) \le 0$ and Ceq(x)=0. (Set LB=[] and UB=[] if no bounds exist.)

x =

patternsearch(@fun,x0,A,b,Aeq,beq,LB,UB,nonlcon,options) minimizes fun with the default optimization parameters replaced by values in options. The structure options can be created using psoptimset.

x = patternsearch(problem) finds the minimum for problem, where problem is a structure containing the following fields:

- objective Objective function
- X0 Starting point
- Aineq Matrix for the inequality constraints
- Bineq Vector for the inequality constraints
- Aeq Matrix for the equality constraints
- Beq Vector for the equality constraints
- LB Lower bound for x
- UB Upper bound for x
- nonlcon Nonlinear constraint function
- options Options structure created with psoptimset
- randstate Optional field to reset the state of rand
- randnstate Optional field to reset the state of randn

You can create the structure problem by exporting a problem from the Pattern Search Tool, as described in "Importing and Exporting Options and Problems" on page 5-15.

Note problem must have all the fields as specified above.

[x, fval] = patternsearch(@fun,x0, ...) returns the value of the objective function fun at the solution x.

[x, fval, exitflag] = patternsearch(@fun,x0, ...) returns exitflag, which describes the exit condition of patternsearch. Possible values of exitflag and the corresponding conditions are

patternsearch

- 1 Magnitude of mesh size is less than specified tolerance and constraint violation less than options. TolCon.
- 2 Change in x less than the specified tolerance and constraint violation less than options. TolCon.
- 4 Magnitude of step smaller than machine precision and constraint violation less than options.TolCon.
- Maximum number of function evaluations or iterations reached.
- -1 Optimization terminated by the output or plot function.
- -2 No feasible point found.

[x, fval, exitflag, output] = patternsearch(@fun,x0, ...) returns a structure output containing information about the search. The output structure contains the following fields:

- function Objective function
- problemtype Type of problem: unconstrained, bound constrained or linear constrained
- pollmethod Polling technique
- searchmethod Search technique used, if any
- iteration Total number of iterations
- function Total number of function evaluations
- meshsize Mesh size at x
- maxconstraint Maximum constraint violation, if any
- message Reason why the algorithm terminated

Note patternsearch does not accepts functions whose inputs are of type complex. To solve problems involving complex data, write your functions so that they accept real vectors, by separating the real and imaginary parts.

Example

Given the following constraints

$$\begin{bmatrix} 1 & 1 \\ -1 & 2 \\ 2 & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} \le \begin{bmatrix} 2 \\ 2 \\ 3 \end{bmatrix}$$

$$\begin{bmatrix} 0 \le x_1 \\ 0 \le x_2 \end{bmatrix}$$

the following code finds the minimum of the function, lincontest6, that is provided with the toolbox:

exitflag =

1

References

- [1] Torczon, Virginia, "On the Convergence of Pattern Search Algorithms", *SIAM Journal on Optimization*, Volume 7, Number 1, pages 1–25, 1997.
- [2] Lewis, Robert Michael and Virginia Torczon, "Pattern Search Algorithms for Bound Constrained Minimization", *SIAM Journal on Optimization*, Volume 9, Number 4, pages 1082–1099, 1999.
- [3] Lewis, Robert Michael and Virginia Torczon, "Pattern Search Methods for Linearly Constrained Minimization", SIAM Journal on Optimization, Volume 10, Number 3, pages 917–941, 2000.
- [4] Audet, Charles and J. E. Dennis Jr., "Analysis of Generalized Pattern Searches", *SIAM Journal on Optimization*, Volume 13, Number 3, pages 889–903, 2003.
- [5] Lewis, Robert Michael and Virginia Torczon, "A Globally Convergent Augmented Lagrangian Pattern Search Algorithm for Optimization with General Constraints and Simple Bounds", SIAM Journal on Optimization, Volume 12, Number 4, pages 1075–1089, 2002.
- [6] A. R. Conn, N. I. M. Gould, and Ph. L. Toint. "A Globally Convergent Augmented Lagrangian Pattern Search Algorithm for Optimization with General Constraints and Simple Bounds", *SIAM Journal on Numerical Analysis*, Volume 28, Number 2, pages 545–572, 1991.
- [7] A. R. Conn, N. I. M. Gould, and Ph. L. Toint. "A Globally Convergent Augmented Lagrangian Pattern Search Algorithm for Optimization with General Constraints and Simple Bounds", *Mathematics of Computation*, Volume 66, Number 217, pages 261–288, 1997.

patternsearch

See Also

 ${\tt psearchtool}, \, {\tt psoptimget}, \, {\tt psoptimset}, \, {\tt ga}, \, {\tt simulannealbnd}, \\ {\tt threshacceptbnd}$

psearchtool

Purpose Open Pattern Search Tool

Syntax psearchtool

psearchtool(optstruct)

Description psearchtool opens the Pattern Search Tool, a graphical user interface

(GUI) for performing pattern searches, as shown in the figure below. You can use the Pattern Search Tool to run a pattern search on optimization problems and display the results. See "Using the Pattern Search Tool"

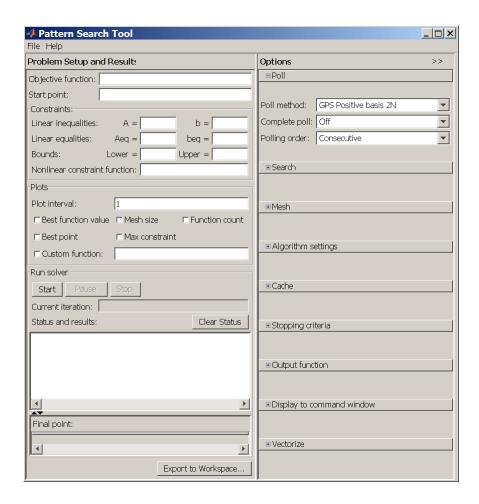
on page 2-3 for a complete description of the tool.

psearchtool(optstruct) starts the Pattern Search tool using optstruct, which can be a Pattern Search options structure or Pattern Search problem structure. An options structure can be created using

psoptimset.

 ${\tt psearch tool\ runs\ the\ Pattern\ Search\ Algorithm\ solver,\ patternsearch,}$

on optimization problems, and it allows you to modify several patternsearch options at run time, while you watch your results.



See Also

patternsearch, psoptimget, psoptimset, gatool

psoptimget

Purpose Obtain values of pattern search options structure

Syntax val = psoptimget(options, 'name')

val = psoptimget(options, 'name', default)

Description

val = psoptimget(options, 'name') returns the value of the parameter name from the pattern search options structure options. psoptimget(options, 'name') returns an empty matrix [] if the value of name is not specified in options. It is only necessary to type enough leading characters of name to uniquely identify it. psoptimget ignores case in parameter names.

val = psoptimget(options, 'name', default) returns the value of the
parameter name from the pattern search options structure options, but
returns default if the parameter is not specified (as in []) in options.

Example

```
val = psoptimget(opts, 'TolX', 1e-4);
```

returns val = 1e-4 if the TolX property is not specified in opts.

See Also

For more about these options, see "Pattern Search Options" on page 8-2.

psoptimset, patternsearch

Purpose

Create pattern search options structure

Syntax

```
psoptimset
```

```
options = psoptimset
```

options = psoptimset('param1',value1,'param2',value2,...)

options = psoptimset(oldopts, 'param1', value1,...)

options = psoptimset(oldopts,newopts)

Description

psoptimset with no input or output arguments displays a complete list of parameters with their valid values.

options = psoptimset (with no input arguments) creates a structure called options that contains the options, or *parameters*, for the pattern search and sets parameters to their default values.

options = psoptimset('param1',value1,'param2',value2,...) creates a structure options and sets the value of 'param1' to value1, 'param2' to value2, and so on. Any unspecified parameters are set to their default values. It is sufficient to type only enough leading characters to define the parameter name uniquely. Case is ignored for parameter names.

options = psoptimset(oldopts, 'param1', value1,...) creates a copy of oldopts, modifying the specified parameters with the specified values.

options = psoptimset(oldopts, newopts) combines an existing options structure, oldopts, with a new options structure, newopts. Any parameters in newopts with nonempty values overwrite the corresponding old parameters in oldopts.

Options

The following table lists the options you can set with psoptimset. See "Pattern Search Options" on page 8-2 for a complete description of the options and their values. Values in {} denote the default value. You can also view the optimization parameters and defaults by typing psoptimset at the command line.

Option	Description	Values
Cache	With Cache set to 'on', patternsearch keeps a history of the mesh points it polls and does not poll points close to them again at subsequent iterations. Use this option if patternsearch runs slowly because it is taking a long time to compute the objective function. If the objective function is stochastic, it is advised not to use this option.	'on' {'off'}
CacheSize	Size of the history	Positive scalar {1e4}
CacheTol	Positive scalar specifying how close the current mesh point must be to a point in the history in order for patternsearch to avoid polling it. Use if 'Cache' option is set to 'on'.	Positive scalar {eps}
CompletePoll	Complete poll around current iterate	'on' {'off'}
CompleteSearch	Complete poll around current iterate	'on' {'off'}
Display	Level of display	'off' 'iter' 'diagnose' {'final'}
InitialMeshSize	Initial mesh size for pattern algorithm	Positive scalar {1.0}
InitialPenalty	Initial value of the penalty parameter	Positive scalar {10}

Option	Description	Values
MaxFunEvals	Maximum number of objective function evaluations	Positive integer {2000*numberOfVariables}
MaxIter	Maximum number of iterations	Positive integer {100*numberOfVariables}
MaxMeshSize	Maximum mesh size used in a poll/search step	Positive scalar {Inf}
MeshAccelerator	Accelerate convergence near a minimum	'on' {'off'}
MeshContraction	Mesh contraction factor, used when iteration is unsuccessful	Positive scalar {0.5}
MeshExpansion	Mesh expansion factor, expands mesh when iteration is successful	Positive scalar {2.0}
MeshRotate	Rotate the pattern before declaring a point to be optimum	'on' {'off'}
OutputFon	Specifies a user-defined function that an optimization function calls at each iteration	<pre>@psoutputhistory {[]}</pre>
PenaltyFactor	Penalty update parameter	Positive scalar {100}
PlotFcn	Specifies plots of output from the pattern search	<pre>@psplotbestf @psplotmeshsize @psplotfuncount @psplotbestx {[]}</pre>
PlotInterval	Specifies that plot functions will be called at every interval	{1}

<u>psop</u>timset

Option	Description	Values
PollingOrder	Order of poll directions in pattern search	'Random' 'Success' {'Consecutive'}
PollMethod	Polling strategy used in pattern search	{'GPSPositiveBasis2N'} 'GPSPositiveBasisNp1' 'MADSPositiveBasis2N' 'MADSPositiveBasisNp1'
ScaleMesh	Automatic scaling of variables	{'on'} 'off'
SearchMethod	Type of search used in pattern search	'GPSPositiveBasisNp1' 'GPSPositiveBasis2N' 'MADSPositiveBasisNp1' 'MADSPositiveBasis2N' @searchga @searchlhs @searchneldermead {[]}
TimeLimit	Total time (in seconds) allowed for optimization	Positive scalar {Inf}
TolBind	Binding tolerance	Positive scalar {1e-3}
TolCon	Tolerance on constraints	Positive scalar {1e-6}
TolFun	Tolerance on function	Positive scalar {1e-6}
TolMesh	Tolerance on mesh size	Positive scalar {1e-6}
TolX	Tolerance on variable	Positive scalar {1e-6}
Vectorized	Specifies whether functions are vectorized	'on' {'off'}

See Also patternsearch, psoptimget

Purpose

Find unconstrained or bound-constrained minimum of function of several variables using simulated annealing algorithm

Syntax

```
x = simulannealbnd(fun,x0)
x = simulannealbnd(fun,x0,lb,ub)
x = simulannealbnd(fun,x0,lb,ub,options)
[x,fval] = simulannealbnd(...)
[x,fval,exitflag] = simulannealbnd(...)
[x,fval,exitflag,output] = simulannealbnd(fun,...)
```

Description

x = simulannealbnd(fun, x0) starts at x0 and finds a local minimum x to the objective function specified by the function handle fun. The objective function accepts input x and returns a scalar function value evaluated at x. x0 may be a scalar or a vector.

x = simulannealbnd(fun, x0, 1b, ub) defines a set of lower and upper bounds on the design variables, x, so that a solution is found in the range $1b \le x \le ub$. Use empty matrices for 1b and ub if no bounds exist. Set 1b(i) to -Inf if x(i) is unbounded below; set ub(i) to Inf if x(i) is unbounded above.

x = simulannealbnd(fun,x0,lb,ub,options) minimizes with the default optimization parameters replaced by values in the structure options, which can be created using the saoptimset function. See the saoptimset reference page for details.

[x,fval] = simulannealbnd(...) returns fval, the value of the objective function at x.

[x,fval,exitflag] = simulannealbnd(...) returns exitflag, an integer identifying the reason the algorithm terminated. The following lists the values of exitflag and the corresponding reasons the algorithm terminated:

- 1 Average change in the value of the objective function over options. StallIterLimit iterations is less than options. TolFun.
- 5 options.ObjectiveLimit limit reached.
- 0 Maximum number of function evaluations or iterations exceeded.

simulannealbnd

- -1 Optimization terminated by the output or plot function.
- -2 No feasible point found.
- -5 Time limit exceeded.

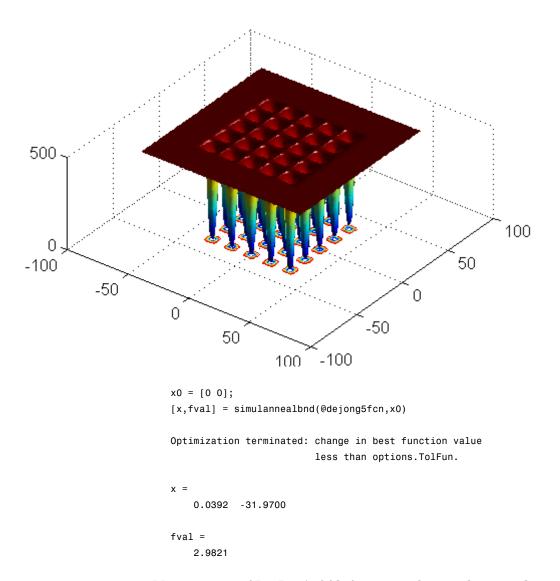
[x,fval,exitflag,output] = simulannealbnd(fun,...) returns output, a structure that contains information about the problem and the performance of the algorithm. The output structure contains the following fields:

- problemtype Type of problem: unconstrained or bound constrained.
- iterations The number of iterations computed.
- function. The number of evaluations of the objective function.
- message The reason the algorithm terminated.
- temperature Temperature when the solver terminated.
- totaltime Total time for the solver to run.
- randstate The state of rand, the MATLAB random number generator, just before the algorithm started.
- randnstate The state of randn the MATLAB normal random number generator, just before the algorithm started. You can use the values of randstate and randnstate to reproduce the output of simulannealbnd. See "Reproducing Your Results" on page 7-5.

Examples

Minimization of De Jong's fifth function, a two-dimensional function with many local minima:

dejong5fcn



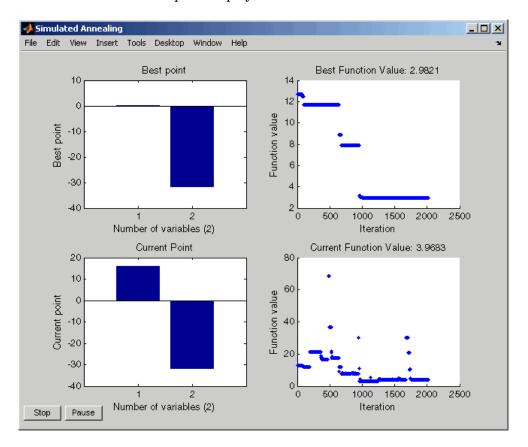
Minimization of De Jong's fifth function subject to lower and upper bounds:

The objective can also be an anonymous function:

Minimization of De Jong's fifth function while displaying plots:

ans = 0.0230 -31.9806

The plots displayed are shown below.



See Also ga, patternsearch, saoptimget, saoptimset, threshacceptbnd

Purpose

Find unconstrained or bound-constrained minimum of function of several variables using threshold acceptance algorithm

Syntax

```
x = threshacceptbnd(fun,x0)
x = threshacceptbnd(fun,x0,1b,ub)
x = threshacceptbnd(fun,x0,1b,ub,options)
[x,fval] = threshacceptbnd(...)
[x,fval,exitflag] = threshacceptbnd(...)
[x,fval,exitflag,output] = threshacceptbnd(...)
```

Description

x = threshacceptbnd(fun,x0) starts at x0 and finds a local minimum x to the objective function specified by the function handle fun. The objective function accepts input x and returns a scalar function value evaluated at x. x0 may be a scalar or a vector.

x = threshacceptbnd(fun, x0, 1b, ub) defines a set of lower and upper bounds on the design variables, x, so that a solution is found in the range $1b \le x \le ub$. Use empty matrices for 1b and ub if no bounds exist. Set 1b(i) to -Inf if x(i) is unbounded below; set ub(i) to -Inf if x(i) is unbounded above.

x = threshacceptbnd(fun,x0,1b,ub,options) minimizes with the default optimization parameters replaced by values in the structure options, which can be created using the saoptimset function. See the saoptimset reference page for details.

[x,fval] = threshacceptbnd(...) returns fval, the value of the objective function at x.

[x,fval,exitflag] = threshacceptbnd(...) returns exitflag, an integer identifying the reason the algorithm terminated. The following lists the values of exitflag and the corresponding reasons the algorithm terminated:

- 1 Average change in the value of the objective function over options. StallIterLimit iterations is less than options. TolFun.
- 5 options.ObjectiveLimit limit reached.
- 0 Maximum number of function evaluations or iterations exceeded.

- -1 Optimization terminated by the output or plot function.
- -2 No feasible point found.
- -5 Time limit exceeded.

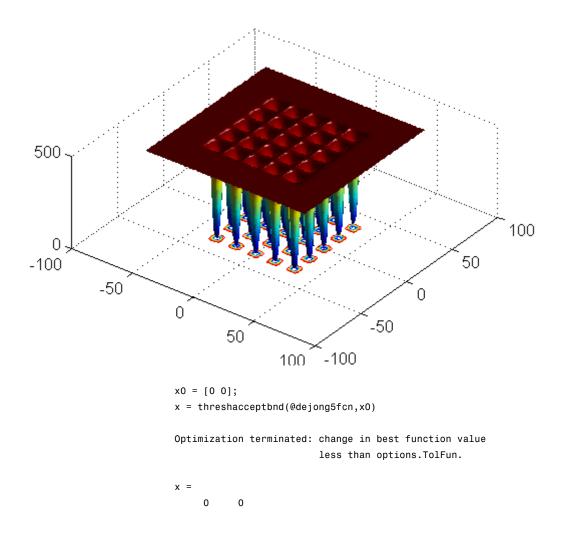
[x,fval,exitflag,output] = threshacceptbnd(...) returns output, a structure that contains information about the problem and the performance of the algorithm. The output structure contains the following fields:

- problemtype Type of problem: unconstrained or bound constrained.
- iterations The number of iterations computed.
- function. The number of evaluations of the objective function.
- message The reason the algorithm terminated.
- temperature Temperature when the solver terminated.
- totaltime Total time for the solver to run.
- randstate The state of rand, the MATLAB random number generator, just before the algorithm started.
- randnstate The state of randn, the MATLAB normal random number generator, just before the algorithm started. You can use the values of randstate and randnstate to reproduce the output of simulannealbnd. See "Reproducing Your Results" on page 7-5.

Examples

Minimizing De Jong's fifth function, a two-dimensional function with many local minima:

dejong5fcn

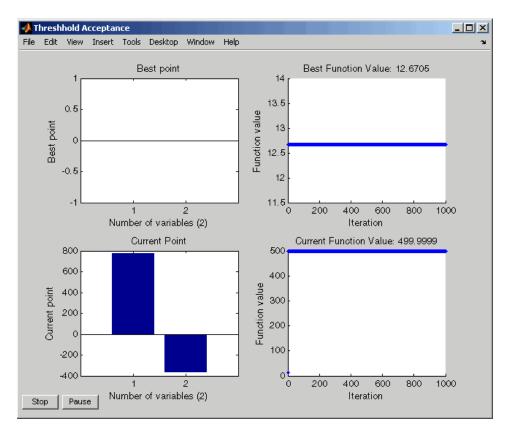


Minimization of De Jong's fifth function subject to lower and upper bounds:

```
x0 = [0 0];
1b = [-64 -64]; ub = [64 64];
```

Minimization of De Jong's fifth function while displaying plots:

The plots displayed are shown below.



See Also saoptimget, saoptimset, threshacceptbnd, patternsearch, ga

Purpose

Values of simulated annealing or threshold acceptance algorithm

options structure

Syntax

```
val = saoptimget(options, 'name')
val = saoptimget(options, 'name', default)
```

Description

val = saoptimget(options, 'name') returns the value of the
parameter name from the simulated annealing or threshold acceptance
algorithm options structure options. saoptimget(options, 'name')
returns an empty matrix [] if the value of name is not specified in
options. It is only necessary to type enough leading characters of
name to uniquely identify the parameter. saoptimget ignores case in
parameter names.

val = saoptimget(options, 'name', default) returns the 'name'
parameter, but returns the default value if the 'name' parameter is
not specified (or is []) in options.

Example

```
opts = saoptimset('TolFun',1e-4);
val = saoptimget(opts,'TolFun');
```

returns val = 1e-4 for TolFun.

See Also

For more about these options, see "Simulated Annealing and Threshold Acceptance Algorithm Options" on page 8-45.

saoptimset, simulannealbnd, threshacceptbnd

Purpose

Create simulated annealing algorithm or threshold acceptance options structure

Syntax

```
saoptimset
options = saoptimset
options = saoptimset('param1',value1,'param2',value2,...)
options = saoptimset(oldopts,'param1',value1,...)
options = saoptimset(oldopts,newopts)
options = saoptimset(optimfunction)
```

Description

saoptimset with no input or output arguments displays a complete list of parameters with their valid values.

options = saoptimset (with no input arguments) creates a structure called options that contains the options, or *parameters*, for the simulated annealing or threshold acceptance algorithm with all parameters set to [].

options = saoptimset('param1', value1, 'param2', value2,...) creates a structure options and sets the value of 'param1' to value1, 'param2' to value2, and so on. Any unspecified parameters are set to []. It is sufficient to type only enough leading characters to define the parameter name uniquely. Case is ignored for parameter names. Note that for string values, correct case and the complete string are required.

options = saoptimset(oldopts, 'param1', value1,...) creates a copy of oldopts, modifying the specified parameters with the specified values.

options = saoptimset(oldopts, newopts) combines an existing options structure, oldopts, with a new options structure, newopts. Any parameters in newopts with nonempty values overwrite the corresponding old parameters in oldopts.

options = saoptimset(optimfunction) creates an options structure with all the parameter names and default values relevant to the optimization function optimfunction. optimfunction can be either 'simulannealbnd' or 'threshacceptbnd'. For example,

```
saoptimset('threshacceptbnd')
ans =
          AnnealingFcn: @annealingfast
        TemperatureFcn: @temperatureexp
         AcceptanceFcn: @acceptancethresh
                TolFun: 1.0000e-006
        StallIterLimit: '500*numberofvariables'
           MaxFunEvals: '3000*numberofvariables'
             TimeLimit: Inf
               MaxIter: Inf
        ObjectiveLimit: -Inf
               Display: 'final'
       DisplayInterval: 10
             HybridFcn: []
        HybridInterval: 'end'
              PlotFcns: []
          PlotInterval: 1
            OutputFcns: []
    InitialTemperature: 100
      ReannealInterval: 100
              DataType: 'double'
```

Options

The following table lists the options you can set with saoptimset. See Chapter 8, "Options Reference" for a complete description of these options and their values. Values in {} denote the default value. You can also view the options parameters by typing saoptimset at the command line.

saoptimset

Option	Description	Values
AcceptanceFcn	Handle to the function the algorithm uses to determine if a new point is accepted	Function handle @acceptancethresh {@acceptancesa} for simulannealbnd or {@acceptancethresh} for threshacceptbnd
AnnealingFcn	Handle to the function the algorithm uses to generate new points	Function handle @annealingboltz {@annealingfast}
DataType	Type of decision variable	'custom' {'double'}
Display	Level of display	'off' 'iter' 'diagnose' {'final'}
DisplayInterval	Interval for iterative display	Positive integer {10}
HybridFcn	Automatically run HybridFcn (another optimization function) during or at the end of iterations of the solver	@fminsearch @patternsearch @fminunc @fmincon {[]}
HybridInterval	Interval (if not 'end' or 'never') at which HybridFcn is called	Positive integer 'never' {'end'}
InitialTemperature	Initial value of temperature	Positive integer {100}
MaxFunEvals	Maximum number of objective function evaluations allowed	Positive scalar {3000*numberOfVariables}
MaxIter	Maximum number of iterations allowed	Positive scalar {Inf}
ObjectiveLimit	Minimum objective function value desired	Scalar {Inf}

Option	Description	Values
OutputFcns	Function(s) get(s) iterative data and can change options at run time	Function handle or cell array of function handles {[]}
PlotFcns	Plot function(s) called during iterations	Function handle or cell array of function handles @saplotbestf @saplotbestx @saplotf @saplotstopping @saplottemperature {[]}
PlotInterval	Plot functions are called at every interval	Positive integer {1}
ReannealInterval	Reannealing interval	Positive integer {100}
StallIterLimit	Number of iterations over which average change in fitness function value at current point is less than options.TolFun	Positive integer {500*numberOfVariables}
TemperatureFcn	Function used to update temperature schedule	Function handle @temperatureboltz @temperaturefast @dtemperatureexp}
TimeLimit	The algorithm stops after running for TimeLimit seconds	Positive scalar {Inf}
TolFun	Termination tolerance on function value	Positive scalar {1e-6}

See Also

For more about these options, see "Simulated Annealing and Threshold Acceptance Algorithm Options" on page 8-45.

saoptimget, simulannealbnd, threshacceptbnd

saoptimset



Examples

Use this list to find examples in the documentation.

Pattern Search

"Example: Finding the Minimum of a Function Using the GPS Algorithm" on page 2-6

"Example — A Linearly Constrained Problem" on page 5-5

"Example — Working with a Custom Plot Function" on page 5-10

"Example — Using a Complete Poll in a Generalized Pattern Search" on page 5-28

"Example — Setting Bind Tolerance" on page 5-44

Genetic Algorithm

"Example: Rastrigin's Function" on page 3-7

"Example — Creating a Custom Plot Function" on page 6-9

"Example — Resuming the Genetic Algorithm from the Final Population" on page 6-18

"Global vs. Local Minima" on page 6-50

GA Multiobjective on page 10-10

Simulated Annealing and Threshold Acceptance Algorithms

"Example: Minimizing De Jong's Fifth Function" on page 4-4

A	from Pattern Search Tool 5-15
accelerator mesh 5-40	F
algorithm genetic 3-19 pattern search 2-13 simulated annealing 4-8 threshold acceptance 4-8 annealing 4-6	fitness function 3-16 vectorizing 6-58 writing M-files 1-3 fitness scaling 6-37
annealing schedule 4-6	G
cache 5-41 children crossover 3-21 elite 3-21 in genetic algorithms 3-18 mutation 3-21 crossover 6-41 children 3-21 fraction 6-44	ga function 10-2 gamultiobj function 10-8 gaoptimget function 10-13 gaoptimset function 10-14 gatool function 10-20 generations 3-17 genetic algorithm description 3-19 nonlinear constraint algorithm, ALGA 3-26 options 8-23 overview 3-2 setting options at command line 6-24 stopping criteria 3-23 using from command line 6-23
direct search 2-2 diversity 3-17 E elite children 3-21 example genetic algorithm 3-7 6-9 6-18 GPS algorithm 2-6 5-5 simulated annealing algorithm 4-4 7-7 threshold acceptance algorithm 7-7 expansion	Genetic Algorithm Tool 6-2 defining problems 6-3 displaying plots 6-7 exporting options and problems 6-15 importing problems 6-18 opening 6-2 pausing and stopping 6-5 running 6-4 setting options 6-13 global and local minima 6-50 GPS 2-2
mesh 5-35	н
exporting problems from Genetic Algorithm Tool 6-15	hybrid function 6-54

	simulated annealing algorithm 8-45
importing problems	threshold acceptance algorithm 8-45
to Genetic Algorithm Tool 6-18	
to Pattern Search Tool 5-18	P
individuals	-
applying the fitness function 3-16	parents in genetic algorithms 3-18
initial population 3-20	pattern search
initial population 5-20	description 2-13
	nonlinear constraint algorithm, ALPS 2-22
M	options 8-2
M-files	overview 2-2
writing 1-3	setting options at command line 5-21
MADS 2-2	terminology 2-10
maximizing functions 1-4	using from command line 5-19
mesh 2-11	Pattern Search Tool 5-2
accelerator 5-40	defining problems 5-3
expansion and contraction 5-35	displaying plots 5-8
minima	exporting options and problems 5-15
global 6-50	importing problems 5-18
local 6-50	opening 5-2
minimizing functions 1-4	pausing and stopping 5-8
mutation 6-41	running 5-4
options 6-42	setting options 5-14
•	patternsearch function 10-23
N.I.	plots
N	genetic algorithm 6-7
nonlinear constraint	pattern search 5-8
genetic algorithm 6-6	poll 2-11
pattern search 5-20	complete 5-27
nonlinear constraint algorithms	method 5-25
ALGA 3-26	population 3-17
ALPS 2-22	initial 3-20
	initial range 6-33
0	options 6-32
	size 6-36
objective function 4-6	psearchtool function 10-30
objective functions	psoptimget function 10-32
writing M-files 1-3	psoptimset function 10-33
options	
genetic algorithm 8-23	

R setting options at command line 7-3 stopping criteria 4-9 Rastrigin's function 3-7 using from command line 7-2 reannealing 4-6 stopping criteria reproduction options 6-41 pattern search 2-19 S T saoptimget function 10-47 temperature 4-6 saoptimset function 10-48 threshacceptbnd function 10-42 scaling threshold acceptance fitness 6-37 description 4-8 search method 5-32 overview 4-2 selection function 6-40 threshold acceptance algorithm setting options options 8-45 genetic algorithm 6-32 setting options at command line 7-3 pattern search 5-25 stopping criteria 4-9 simulannealbnd function 10-37 using from command line 7-2 simulated annealing description 4-8 overview 4-2 simulated annealing algorithm vectorizing fitness functions 6-58 options 8-45